

function $x = f(n)$

$x = 1;$

for $i = 1:n$

for $j = 1:n$

$x = x + 1;$

1 Ans:- Inner loop:-

It executes n times for each phase in outer loop.

$\therefore n$ executions for inner loop

Outer loop:-

It executes n times from $i = 1$ to $i = n$

$\therefore n$ executions for outer loop

$$\text{Total executions} = \sum_{i=1}^n \sum_{j=1}^n 1$$

$$= \sum_{i=1}^n n$$

$$= n \times n$$

$$= n^2$$

\therefore The total runtime of the algo is $O(n^2)$

3 Ans:- Big-O - Notation (Upper bound)

$O(n^2)$ - function does not grow faster than quadratic

Big-Omega

$\Omega(n^2)$ - function does not grow slower than quadratic

Big-Theta

$\Theta(n^2)$ - function grows asymptotically as n^2

4Ans:- $y = i + j$, actual time taken by the modified function will be slightly longer due to it.
 $\therefore O(n^2)$ is the time complexity.

5Ans:- It doesn't effect much in the time complexity.

$$\begin{aligned}
 & \left(\frac{n}{2} \times \frac{n}{2} \right) + \left(\frac{n}{2} \times \frac{n}{2} \right) \\
 &= \frac{n^2}{4} + \frac{n^2}{4} \\
 &= \frac{n^2}{2} \\
 &= O(n^2)
 \end{aligned}$$

(Ans) It is also a similar lot of it.

(Answer) It is also a similar lot of it.