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Assignment 1

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Abstract—This document solves a problem from Points and Vectors, where it finds the angle between a given Force and displacement vector

Download all python codes from

https://github.com/

and latex-tikz codes from

https://github.com/

Substituting these values in Equation 2.0.1,

$$\cos(\theta) = \frac{16}{(5\sqrt{2})(5\sqrt{2})} = \frac{8}{25}$$

$$\implies \theta = \arccos(\frac{8}{25})$$

$$\implies \theta \approx 71.3^{\circ}$$

Thus, the angle between **F** and **d** is approximately 71.3°

1 Problem

Find the angle between the force $\mathbf{F} = \begin{pmatrix} 3 \\ 4 \\ -5 \end{pmatrix}$ and

displacement $\mathbf{d} = \begin{pmatrix} 5 \\ 4 \\ 3 \end{pmatrix}$

2 EXPLANATION

Let the angle between **F** and $\mathbf{d} = \theta$

$$\cos(\theta) = \frac{\mathbf{F} \cdot \mathbf{d}}{\|\mathbf{F}\| \|\mathbf{d}\|}$$
 (2.0.1)

Here, the scalar product of the vectors \mathbf{F} and \mathbf{d} can be given as,

$$\mathbf{F} \cdot \mathbf{d} = \mathbf{F}^T \mathbf{d} \tag{2.0.2}$$

3 Solution

Using Equation 2.0.2 and substituting the values,

$$\mathbf{F} \cdot \mathbf{d} = \begin{pmatrix} 3 \\ 4 \\ -5 \end{pmatrix}^T \begin{pmatrix} 5 \\ 4 \\ 3 \end{pmatrix}$$

$$\implies \mathbf{F} \cdot \mathbf{d} = \begin{pmatrix} 3 & 4 & -5 \end{pmatrix} \begin{pmatrix} 5 \\ 4 \\ 3 \end{pmatrix} = 16$$

$$\|\mathbf{F}\| = \sqrt{3^2 + 4^2 + (-5)^2} = 5\sqrt{2}$$

$$\|\mathbf{d}\| = \sqrt{5^2 + 4^2 + 3^2} = 5\sqrt{2}$$