

Sample solution for COP 5536/ AD 711R \\
Make-up Exam, Spring 2005
}
\end{center}

\begin{enumerate}

\item(10) See attached sheet.

\item(10)

Note that we need 2 dummy runs (run length is zero)
for optimal 4-way merge which must merged first to be optimal. \\

\begin{itemize}

\item 4-way merge : \\

step 1: $(0, 0, 100, 200) = 300$ \\

step 2: $(300, 300, 400, 500) = 1500$ \\

step 3: $(1500, 600, 700, 800) = 3600$ \\

\item 8-way merge : \\

$(100, 200, 300, 400, 500, 600, 700, 800) = 3600$

\end{itemize}

\begin{enumerate}

\item Number of comparisons \\

In 4-way scheme: For each step,

loser tree initialization needs 3 comparisons (one record produced)

and then each record needs 2 comparisons to output. \\

So, the total number of comparisons in the 4-way scheme is

$3 + (300-1)*2 + 3 + (1500-1)*2 + 3 + (3600-1)*2 = 10803$ \\

In 8-way scheme: $7 + (3600-1)*3 = 10804$. \\

\item Number of disk I/Os \\

Each merge step need 2 disk I/Os: one for input and one for output.

4-way scheme needs $3*2 + 15*2 + 36*2 = 108$ and 8-way scheme $36*2 = 72$.

\item 8-way merge is better scheme than 4-way merge scheme

due to the number of disk I/Os.

\end{enumerate}

\item (10)

\begin{enumerate}

\item (4)

\begin{verbatim}

```

          3              3              3(2)
swap      /  \      swap /  \      swap /  \
==>      4    5      ==> 4    5      ==> 5(2)  4(1)
          /  \          /  \          /  \
          9    8          8    9          8(2)  9(1)
          /  \ /  \      /  \ /  \      /  \ /  \
        15 13 21      13 21 15      13(1) 21(1) 15(1)

```

\end{verbatim}

\item (6) Meld right subtree with smaller root and all of the other tree.

\begin{verbatim}

```

meld[ 6 ,      3 ]      meld[ 5,  6 ]      5
  /  \    /  \      ==>  /  /  \      ==> /  \
14 13  7    5      12 14 13      12    6
      /  \ /      /  \
      10  9 12      14 13

```

```

swap      5              3
==>      /  \      ==> /  \
        6    12        7    5
        /  \        /  \ /  \
       14 13       10  9  6    12
                /  \
                14 13

```

```

==>      2
        /  \
       4    3
      /  \ /  \
     8    9 7    5
        / /  \ /  \
       17 10 9  6    12
            /  \
            14 13

```

```

swap
==>      2
        /  \
       3    4

```

```

      /      \      /      \
      7        5      8        9
    /  \      /  \      /
   10  9    6      12    17
      /  \
     14  13
\end{verbatim}
\end{enumerate}

```

```

\item (10)
\begin{enumerate}
\item (4) $Insert$ does not need pairwise combine.
\begin{verbatim}

```

```

                min
                |
                V
      7 - 12 - 4 - 23 - 3 - 24 - 13 - 20 - 19 - 5
\end{verbatim}

```

```

\item (6)
\begin{verbatim}

```

```

meld(7, 12)  7      ==>  meld(4, 23)  7      4
           |           |           |
           12          12      23

```

```

      meld(7, 4)           4      meld(24, 13)  13
==>    |  |  ==>    /  |  ==>           |
      12 23           7  23           24
           |
          12

```

```

      meld(19, 5)  5      meld(13, 5)           5
==>           |  ==>    |  |           /  |
           19      24 19      13  19
                   |
                  24

```

```

      meld(4, 5)           4
==>           /  /  |
           5  7  23
         /  |  |
       13 19 12
         |
        24

```

```

                                min
                                |
                                v
meld(4,20)                    4-----20
==>
    / / |
    5 7 23
    / | |
    13 19 12
    |
    24
\end{verbatim}
\end{enumerate}

\end{enumerate}
\end{document}

```