

Question 1 (12 points)

Consider the following splay tree:

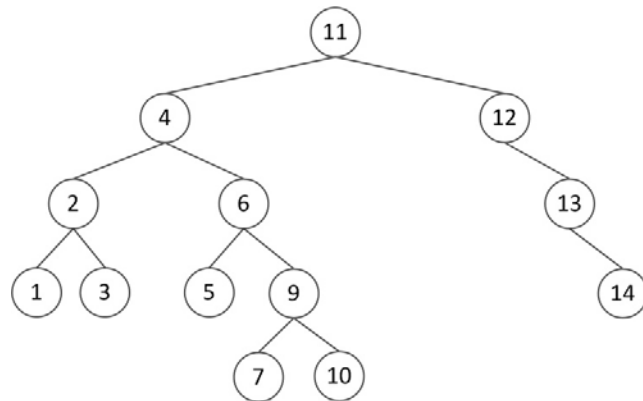
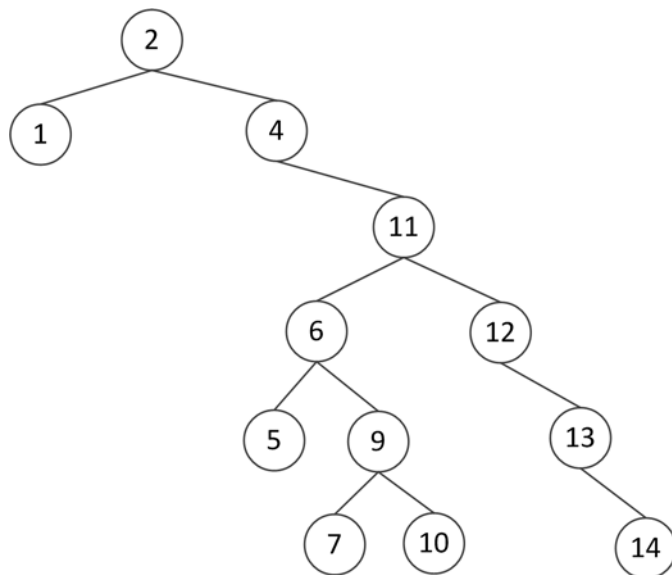


Figure 1

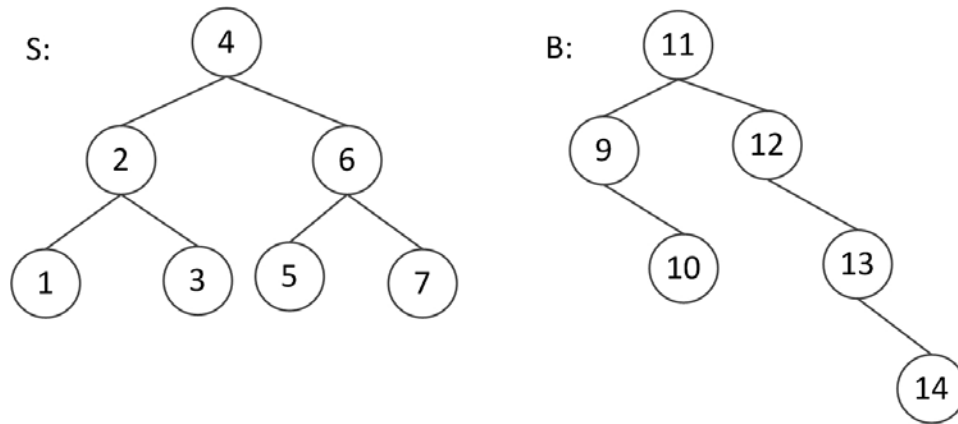
- 1) Perform a *delete* for the key 3 under the assumption that this is a *bottom-up* splay tree. Show each step. (6 points)

Answer:



- 2) Perform a *split* from the tree of Figure 1 (not the resulting tree of part 1)) for the key 8 under the assumption that this is a *top-down* splay tree. Show each step. (6 points)

Answer:

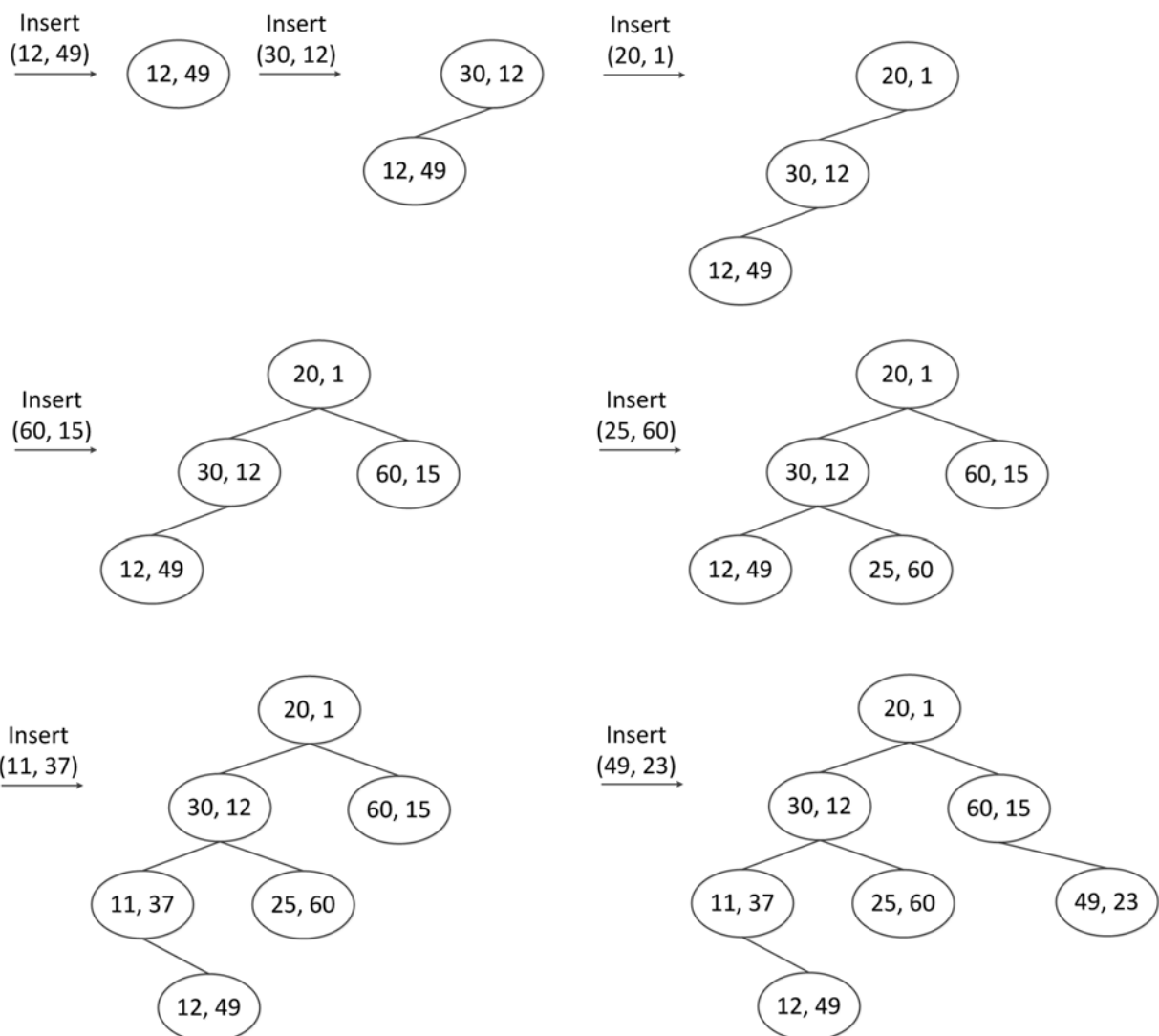


Question 2 (14 points)

A min radix priority search tree (RPST) can be defined as a set of pairs (x, y) over $[0 \dots 63]$ of integers. Construct a min RPST by inserting the following pairs in the given order. Show the min RPST after each insertion.

$(12, 49), (30, 12), (20, 1), (60, 15), (25, 60), (11, 37), (49, 23)$

Answer:



Question 3 (10 points)

You are given a Bloom filter that consists of $m = 11$ memory bits and two hash functions $f_1()$ and $f_2()$ defined as below:

$$f_1(k) = (3 * k) \bmod m$$

$$f_2(k) = (2 * k) \bmod m$$

where k is a given key. Assume that all m bits of the Bloom filter are initially set to 0.

- 1) Show the Bloom filter bits following the insertion of the key 7, 12, 9. Show result after each insertion. (6 points)

Answer:

Insert key 7, $f_1(7) = 10$, $f_2(7) = 3$.

0	1	2	3	4	5	6	7	8	9	10
0	0	0	1	0	0	0	0	0	0	1

Insert key 12, $f_1(12) = 3$, $f_2(12) = 2$.

0	1	2	3	4	5	6	7	8	9	10
0	0	1	1	0	0	0	0	0	0	1

Insert key 9, $f_1(9) = 5$, $f_2(9) = 7$.

0	1	2	3	4	5	6	7	8	9	10
0	0	1	1	0	1	0	1	0	0	1

- 2) How can the resulting filter return a "maybe" for a key that was not inserted? (4 points)

Answer:

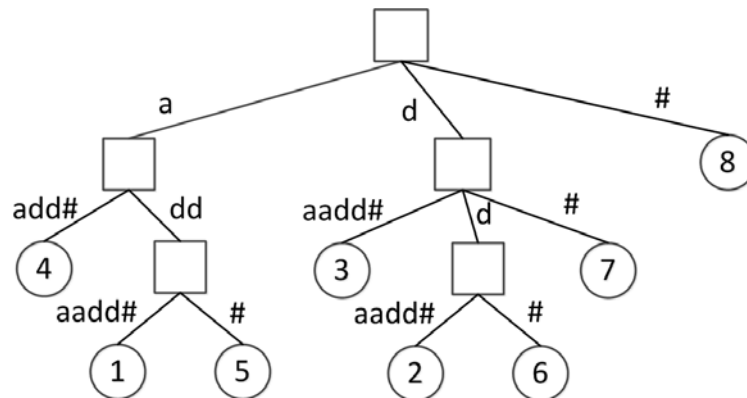
Let key = k , $f_1(k) = i_1$, $f_2(k) = i_2$. If the value at i_1 and i_2 are both already set to "1", a "maybe" is returned.

Question 4 (14 points)

1) Draw a clearly labeled suffix tree for the string *addaadd#*. (8 points)

Answer:

a	d	d	a	a	d	d	#
1	2	3	4	5	6	7	8



2) For R-Tree which is usually used as a spatial database index:

a) Briefly describe how to insert a node into R-Tree. (3 points)

Answer:

(*Leaf selection*) Follow the path from root to leaf, then insert node into subtree whose MBR is increasing least with the new inserted new rectangle.

(*Consider when to split*) If capacity exceeded, split set of $M + 1$ rectangles / MBRs into 2 sets A and B.

b) How does Quadratic Split Method work? Show it with an example. (3 points)

Answer:

Let S be the set of $M + 1$ rectangles to be partitioned.

(1) Find (a,b) in S so that $\text{area}(\text{MBR}(a,b)) - \text{area}(a) - \text{area}(b)$ is maximized.

(2) Assign remaining unassigned rectangles. Find an unassigned rectangle C to maximize:
 $|\text{area}(\text{MBR}(A,c)) - \text{area}(\text{MBR}(A)) - (\text{area}(\text{MBR}(B,c)) - \text{area}(\text{MBR}(B)))|$

(3) Assign c to partition whose area increases least.

(4) Continue assigning in this way until all remaining rectangles must necessarily be assigned to one of the two partitions for that partition to have m rectangles.