

Roll No.:.....

# National Institute of Technology, Delhi

Name of the Examination: B.Tech. (End-Sem)

Branch : EEE+ECE

Semester : I

Title of the Course : Electromagnetics and

Course Code : PHL100

Quantum Physics

Time: 3 Hours

Maximum Marks: 50

Note : This question paper divided into three sections A, B and C and each section must be solved with rules given as follows:

Section A: Contains Ten (10) questions of 01 mark each and all questions are compulsory.

Section B: Contains Five (05) questions of 5 marks each and any four (04) are to be attempted.

Section C: Contains Three (03) questions of ten (10) marks each and any two (02) are to be attempted.

Assume suitable data, if found missing.

Used symbols have their usual meaning.

## Section A

- Q1: Write down the solenoidal condition for a vector field.  
Q2: Write down the integral form of the electrostatic potential.  
Q3: Why is the wave nature of matter less apparent in our daily observations?  
Q4: What is the physical significance of the numerical aperture in optical fiber?  
Q5: Quantum mechanical operator of kinetic energy is.....  
Q6: The best suited rays for the study of Compton effect is .....  
Q7: Calculate the coherence length for a light source whose line 1/1000 of its wavelength.  
Q8: What is difference between phenomena of interference and diffraction of light wave?  
Q9: What is the value of ground state energy of a quantum particle in an infinite potential well?  
Q10: The uncertainty in the location of a particle is equal to its de Broglie wavelength. The uncertainty in its velocity is .....

## Section B

- Q1: Given the total electromagnetic energy  $W = \frac{1}{2} \int (E \cdot D + H \cdot B) dv$  show from Maxwell's equations that  $\frac{\partial W}{\partial t} = -\oint (E \times H) ds - \int E \cdot J dv$ . (5)
- Q2:[a]: Distinguish between temporal coherence and spatial coherence. Discuss why two independent sources of light of the same wavelength cannot produce interference fringes. (2)  
[b]: An optical fiber is 1.5 m long and has a diameter of 20  $\mu m$ . If a ray of light is incident on one end of fiber at an angle  $30^\circ$ , how many reflections does it undergo before emerging from the other end? Refractive index of the fiber is 1.3. (3)
- Q3: Given a vector field  $D = r \sin \varphi \mathbf{a}_r - \frac{1}{r} \sin \theta \cos \varphi \mathbf{a}_\theta + r^2 \mathbf{a}_\varphi$ . Determine, (i)-  $D$  at point  $P (10, 150^\circ, 330^\circ)$ , (ii)-The component of  $D$  tangential to the spherical surface  $r = 10$  at  $P$  and (iii)- A unit vector at  $P$  perpendicular to  $D$  and tangential to the cone,  $\theta = 150^\circ$  (5)

**Q:4.** Derive the expression for Compton shift. Why is it not observable in the visible region of electromagnetic radiation? (5)

**Q:5. [a]** White light is incident on a soap film at an angle  $\sin^{-1}(4/5)$  and the reflected light on examination by a spectroscope shows dark bands. Two consecutive dark bands correspond to wavelength  $6.1 \times 10^{-5}$  cm and  $6 \times 10^{-5}$  cm. If refractive index of the film be  $4/3$ , calculate its thickness. (3)

[b] What do you understand by quarter wave plate and half wave plate. (2)

### Section C

**Q1: [a]:** Write down the Schrodinger's time dependent and independent wave equations of matter wave. Explain, why: (i) the wave function  $\Psi$  must be single valued and continuous function of position. (ii) the integral of  $|\Psi|^2$  overall space must be equal to unity. (5)

[b]: Calculate the wavelength of incident x-ray photon which produces recoil electron of energy  $4.0 \text{ KeV}$  in Compton effect. The electron recoils in the direction of incident photon and photon is scattered at an angle of  $180^\circ$ . (3)

[c]: Find the maximum energy of the photoelectron, the work function and threshold frequency, if the potassium surface is illuminated by a light of wavelength  $5893 \text{ \AA}$ . The stopping potential for the emitted electron is  $0.36 \text{ V}$ . (2)

**Q2: [a]:** What are the characteristics of de-Broglie wave? Show that group velocity of the de-Broglie wave associated with a microscopic particle is equal to the particle velocity itself. (5)

[b]: Explain 'absorption', 'spontaneous', and 'stimulated' emission of radiation. Obtain relation between transition probabilities of spontaneous and stimulated emission. (3)

[c]: What are the characteristics of laser beam. (2)

**Q3: [a]:** Consider a particle whose normalized wave function is: (5)

$$\psi(x) = 2\alpha\sqrt{\alpha} x e^{-\alpha x}; \quad x > 0 \\ = 0; \quad x < 0$$

(i) For what value of  $x$  does probability take peak?

(ii) What is the probability that the particle is found between  $x = 0$  and  $x = 1/\alpha$ ?

(iii) Calculate the wave function in momentum space.

[b]: Show that double slit Fraunhofer diffraction provides the intensity four times of the one obtained by single slit. (3)

[c]: In a grating spectrum, which spectral line in  $4^{\text{th}}$  order will overlap with  $3^{\text{rd}}$  order line of  $5491 \text{ \AA}$ ? (2)

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