

National Institute of Technology, Delhi

Name of the Examination: End Sem Exam (Nov-Dec 2019)

Branch : B.Tech (ECE)

Semester : III

Title of the Course : ELECTROMAGNETIC THEORY

Course Code : ECL 203

Time: 3 Hours

Maximum Marks: 50

Section A (10 x 1 = 10 marks)

All questions are compulsory.

- A.1 What is cylindrical co-ordinate system?
- A.2 Transform the Cartesian point (1,2,3) in spherical co-ordinate.
- A.3 Find displacement current density if $\mathbf{E} = 200 \sin 10^{10} t \text{ V/m}$.
- A.4 Find the curl of $\mathbf{B} = 2xy\hat{\mathbf{a}}_x + x^2z\hat{\mathbf{a}}_y + z^3\hat{\mathbf{a}}_z$
- A.5 Find the laplacian of $W = e^{-z} \sin(2x) \cosh y$
- A.6 Write down the formula for electric flux density for finite volume charge and finite surface charge.
- A.7 What is Gaussian surface? Write down the properties of Gaussian surface.
- A.8 Calculate the field intensity at a point on a sphere of radius 3 m, if a positive charge of $2 \mu\text{C}$ is placed at the original of sphere.
- A.9 State and explain Bio severt law.
- A.10 Write down the Maxwell's equations in point form as well as in integral form.

Section B (4 x 5 = 20 marks)

Attempt any four questions.

- B.1 Calculate the circulation of vector field $\mathbf{F} = r^2 \cos(\phi) \hat{\mathbf{a}}_r + z \sin(\phi) \hat{\mathbf{a}}_z$ around the path L defined by $0 \leq r \leq 3$, $0 \leq \phi \leq 60^\circ$ and $z = 0$.
- B.2 A circular ring of charge with radius 5 m lies in $z = 0$ plane with centre at origin. If the $\rho_L = 10 \text{ nC/m}$, find the point charge Q place at the origin which will produce same \mathbf{E} at the point (0,0,5) m.
- B.3 Three concentric spherical surfaces have radii $r = 3, 5$ and 7 cm respectively and have uniform charge densities of 200, -50 and $\rho_x \mu\text{C/m}^2$ respectively. Find
 - (a) \mathbf{D} and \mathbf{E} at $r = 2 \text{ cm}$, 4 cm and 6 cm
 - (b) Find ρ_x if $\mathbf{D} = 0$ at $r = 7.32 \text{ cm}$.
- B.4 In the region $0 \leq r \leq 0.5 \text{ m}$, in cylindrical co-ordinates, the current density is $\mathbf{J} = 4.5 e^{-2r} \hat{\mathbf{a}}_z \text{ A/m}^2$ and $\mathbf{J} = 0$ elsewhere. Use Amperes circuital law to find \mathbf{H} .
- B.5 Find the amplitude of the displacement current density,
 - (a) In the air near car antenna where the field strength of FM signal is $\mathbf{E} = 80 \cos (6.277 \times 10^8 t - 2.092y) \hat{\mathbf{a}}_z \text{ V/m}$.
 - (b) Inside a capacitor where $\epsilon_r = 600$ and $\mathbf{D} = 3 \times 10^{-6} \sin (6 \times 10^6 t - 0.3464x) \hat{\mathbf{a}}_z \text{ C/m}^2$.

Section C (2 x 10 = 20 marks)

Attempt any two questions.

- C.1 (a)** Derive the Maxwell's equation from Ampere's circuital law in point and integral form.
- (b)** A dipole having moment $\mathbf{P} = 3\hat{\mathbf{a}}_x - 5\hat{\mathbf{a}}_y + 10\hat{\mathbf{a}}_z$ nCm is located at $Q(1,2,-4)$ in free space. Find V at $(P,3,4)$.
- C.2 (a)** Find electric boundary conditions between two perfect dielectrics.
- (b)** A potential field is given as $V = 100 e^{-5x} \sin(3y)\cos(4z)$ V. If point $P(0.1, \pi/12, \pi/24)$ is located at a conductor free space boundary. At point P , find V , E , E_T , E_N , \mathbf{D} , \mathbf{D}_N , ρ_s .
- C.3 (a)** Derive the expression for the general wave equation.
- (b)** A lossy dielectric is characterized by $\epsilon_r = 2.5$, $\mu_r = 4$ and $\sigma = 10^{-3}$ mho/m at a frequency 10MHz. Find Propagation constant, attenuation constant, phase constant, phase velocity, wavelength and intrinsic impedance.