

National Institute of Technology, Delhi

Name of the Examination: B. Tech: Mid Semester (Autumn 2019-2020) Examination

Branch : ECE

Semester : III

Title of the Course : Solid State Devices

Course Code : ECB 201

Time: 2 Hours

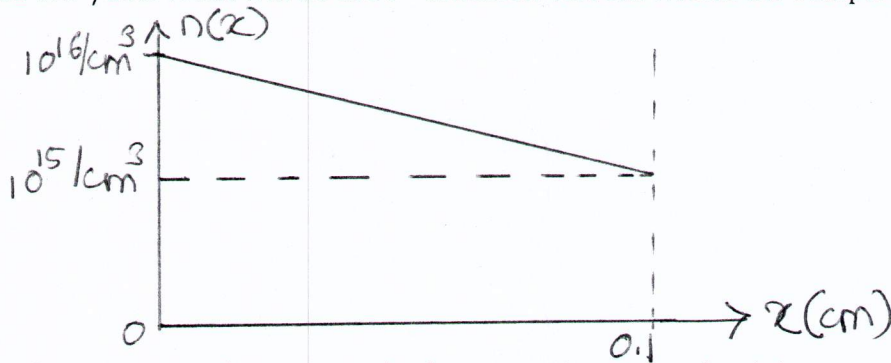
Maximum Marks: 25

Note:

- Questions are printed on BOTH sides. Answers should be CLEAR AND TO THE POINT.
- All parts of a single question must be answered together and in the same sequence as given in question paper. ELSE QUESTION SHALL NOT BE EVALUATED.
- Use following data if not given in a problem: $\epsilon_0 = 8.85 \times 10^{-14} \text{ F/cm}$, $\epsilon_r (\text{SiO}_2) = 3.9$, $\epsilon_r (\text{Si}) = 11.8$, At room temperature for Si [$\mu_n = 1350 \text{ cm}^2/\text{V}\cdot\text{S}$, $\mu_p = 480 \text{ cm}^2/\text{V}\cdot\text{S}$, $n_i = 1.5 \times 10^{10}/\text{cm}^3$, $E_g = 1.12 \text{ eV}$], $k = 8.62 \times 10^{-5} \text{ eV/K}$, $\tau_n = \tau_p = 1 \mu\text{s}$, $E_g(\text{Ge}) = 0.7 \text{ eV}$, $n_i(\text{Ge}) = 2.5 \times 10^{13}/\text{cm}^3$.

Q1. Calculate the position of the intrinsic Fermi level w.r.t. the center of the bandgap in Si at 300 K. The density of states effective carriers masses in Si are, $m_n^* = 1.08 m_0$ and $m_p^* = 0.56 m_0$. **[2 M]**

Q2. The e^- concentration decreases as shown in the plot, within a Si sample. **[2 M]**
The cross-sectional area of the sample is 0.05 cm^2 and D_n for Si = $25 \text{ cm}^2/\text{sec}$. What will be the e^- diffusion current within the sample?



Q3. Show that a semiconductor sample shows maximum conductivity at any given temperature when carrier concentrations are, $n = n_i \sqrt{\mu_h/\mu_e}$ and $p = p_i \sqrt{\mu_e/\mu_h}$, where symbols have their usual meanings. **[2 M]**

Q4. Determine the values of n_0 and p_0 for Si at $T = 300 \text{ K}$, if the Fermi energy level is 0.22 eV above the valence band energy. [$N_v = 1.04 \times 10^{19}/\text{cm}^3$, $N_c = 2.8 \times 10^{19}/\text{cm}^3$ and $E_{g,\text{Si}} = 1.12 \text{ eV}$ at 300 K]. **[2 M]**

- Q5. The bandgap (E_g) of GaAsP is 1.95 eV. Determine the wavelength of EM [2 M]
radiation that is emitted upon direct recombination of electrons and holes in the GaAsP sample. What will be the color of emitted radiation?
- Q6. Estimate the expressions for developed electric field of a Si pn junction [3 M]
where the space charge profile at depletion region is given as,
 $p(x) = qh(2x+3)$ where, x is distance of the device from physical contact
at $x = 0$ and h = Plank's constant.
- Q7. A Si sample is doped with 10^{16} cm^{-3} donor impurity is exposed by light at [2+3+2 M]
 $x = 0$ to generate excess EHP of amount $10^{14}/\text{cm}^3$. Excess carriers travel
1 cm distance in 0.4 ms time under a field of 2 V/cm.
- (a) Calculate $p(x)$ and $n(x)$ at $x = 2L_p$.
 - (b) Calculate diffusion current density at $x = 0, L_p$, and $2L_p$.
 - (c) Calculate mobility for majority and minority carriers.
- [$D_p = 25 \text{ cm}^2/\text{sec}$, $D_n = 50 \text{ cm}^2/\text{sec}$, $\tau_n = \tau_p = 10 \text{ ns}$]
- Q8. Answer the changes in each of the following parameters in terms of [5x1 M]
increasing/decreasing only as the case may be when *temperature increases*. [no explanation required]
- (a) Conductivity of the semiconductor
 - (b) Reverse saturation current in p-n Junction
 - (c) Junction Width
 - (d) Mobility due to impurity'
 - (e) Avalanche breakdown.
-

Useful Equations

$$r = \frac{h^2 \epsilon_0 n^2}{\pi m q^4} \quad KE = h \nu_0 - \frac{ch}{\lambda_0} \quad \rho = \frac{R.A}{L}$$

$$f(E) = \frac{1}{1 + \exp\left(\frac{E - E_F}{KT}\right)}$$

$$\text{At Equilibrium, } n_0 = \int_{E_c}^{\infty} f(E) N(E) dE = N_c f(E_c) = N_c e^{-(E_c - E_F)/kT}$$

$$N_c = 2 \left(\frac{2\pi m_n^* kT}{h^2} \right)^{3/2} \quad n_0 = n_i e^{(E_F - E_i)/kT}$$

$$N_v = 2 \left(\frac{2\pi m_p^* kT}{h^2} \right)^{3/2} \quad p_0 = n_i e^{(E_i - E_F)/kT}; \quad n_0 p_0 = n_i^2$$

$$p_0 = N_v [1 - f(E_v)] = N_v e^{-(E_F - E_v)/kT}$$

$$n_i = N_c e^{-(E_c - E_i)/kT}$$

$$p_i = N_v e^{-(E_i - E_F)/kT} \quad n_i = \sqrt{N_c N_v} e^{-(E_g)/2kT} = 2 \left(\frac{2\pi kT}{h^2} \right)^{3/2} (m_n^* m_p^*)^{3/4} e^{-(E_g)/2kT}$$

$$n = N_c e^{-(E_c - F_n)/kT} = n_i e^{(F_n - E_i)/kT} \quad p = N_v e^{-(F_p - E_i)/kT} = n_i e^{(E_i - F_p)/kT}$$

$$np = n_i^2 e^{(F_n - F_p)/kT}$$

$$\frac{d\xi(x)}{dx} = \frac{d^2 V(x)}{dx^2} = \frac{\rho(x)}{\epsilon} = \frac{q}{\epsilon} (p - n + N_d^+ - N_a^-)$$

$$\xi(x) = -\frac{dV(x)}{dx} = \frac{1}{q} \frac{dE_i}{dx} \quad \frac{I_x}{A} = J_x = q(n\mu_n + p\mu_p)\xi_x = \sigma \xi_x \quad L = \sqrt{D\tau} \quad \frac{D}{\mu} = \frac{kT}{q}$$

$$\frac{\partial p(x,t)}{\partial t} = \frac{\partial \delta p}{\partial t} = -\frac{1}{q} \frac{\partial J_p}{\partial x} - \frac{\delta p}{\tau_p}$$

$$\frac{\partial \delta n}{\partial t} = \frac{1}{q} \frac{\partial J_n}{\partial x} - \frac{\delta n}{\tau_n}$$

$$\frac{d^2 \delta n}{dx^2} = \frac{\delta n}{D_n \tau_n} = \frac{\delta n}{L_n^2} \quad \frac{d^2 \delta p}{dx^2} = \frac{\delta p}{L_p^2}$$

$$\frac{I_x}{A} = J_x = q(n\mu_n + p\mu_p)\mathcal{E}_x = \sigma\mathcal{E}_x$$

Diffusion length: $L = \sqrt{D\tau}$ Einstein relation: $\frac{D}{\mu} = \frac{kT}{q}$

Continuity: $\frac{\partial p(x,t)}{\partial t} = \frac{\partial \delta p}{\partial t} = -\frac{1}{q} \frac{\partial J_p}{\partial x} - \frac{\delta p}{\tau_p}$ $\frac{\partial \delta n}{\partial t} = \frac{1}{q} \frac{\partial J_n}{\partial x} - \frac{\delta n}{\tau_n}$

For steady state diffusion: $\frac{d^2 \delta n}{dx^2} = \frac{\delta n}{D_n \tau_n} = \frac{\delta n}{L_n^2}$ $\frac{d^2 \delta p}{dx^2} = \frac{\delta p}{L_p^2}$

Equilibrium: $V_0 = \frac{kT}{q} \ln \frac{p_p}{p_n} = \frac{kT}{q} \ln \frac{N_a}{n_i^2/N_d} = \frac{kT}{q} \ln \frac{N_a N_d}{n_i^2}$ $\frac{p_p}{p_n} = \frac{n_p}{n_n} = e^{qV_0/kT}$ $W = \left[\frac{2\epsilon(V_0 - V)}{q} \left(\frac{N_a + N_d}{N_a N_d} \right) \right]^{1/2}$

Junction Depletion: $C_j = \epsilon A \left[\frac{q}{2\epsilon(V_0 - V)} \frac{N_a N_d}{N_a + N_d} \right]^{1/2} = \frac{\epsilon A}{W}$

One-sided abrupt p^+n : $x_{rel} = \frac{WN_d}{N_a + N_d} \approx W$ $V_0 = \frac{qN_d W^2}{2\epsilon}$

$$\Delta p_n = p(x_{rel}) - p_n = p_n(e^{qV_0/kT} - 1)$$

$$\delta p(x_n) = \Delta p_n e^{-x_n/L_p} = p_n(e^{qV_0/kT} - 1)e^{-x_n/L_p}$$

Ideal diode: $I = qA \left(\frac{D_p}{L_p} p_n + \frac{D_n}{L_n} n_p \right) (e^{qV_0/kT} - 1) = I_0 (e^{qV_0/kT} - 1)$

Stored charge exp. hole dist.: $Q_p = qA \int_0^\infty \delta p(x_n) dx_n = qA \Delta p_n \int_0^\infty e^{-x_n/L_p} dx_n = qAL_p \Delta p_n$

$$I_p(x_n = 0) = \frac{Q_p}{\tau_p} = qA \frac{L_p}{\tau_p} \Delta p_n = qA \frac{D_p}{L_p} p_n (e^{qV_0/kT} - 1)$$

$$I_{E_T} = qA \frac{D_p}{L_p} \left(\Delta p_E \tanh \frac{W_b}{L_p} - \Delta p_C \operatorname{csch} \frac{W_b}{L_p} \right)$$

$$I_C = qA \frac{D_p}{L_p} \left(\Delta p_E \operatorname{csch} \frac{W_b}{L_p} - \Delta p_C \tanh \frac{W_b}{L_p} \right)$$
 Substrate bias: $\Delta V_T \approx \frac{\sqrt{2\epsilon_s q N_d}}{C_i} (-V_B)^{1/2}$

Oxide: $C_i = \frac{\epsilon_i}{d}$ Depletion: $C_d = \frac{\epsilon_s}{W}$ MOS: $C = \frac{C_i C_d}{C_i + C_d}$

Inversion: $\phi_s(\text{inv.}) = 2\phi_F = 2 \frac{kT}{q} \ln \frac{N_a}{n_i}$ (6-15) $W = \left[\frac{2\epsilon_s \phi_s}{q N_d} \right]^{1/2}$