

# National Institute of Technology, Delhi

Name of the Examination: B. Tech.

Branch : Electrical & Electronics Engg.

Semester : 3<sup>rd</sup>

Title of the Course : Electromagnetic Field Theory

Course Code : EEL 203

Time: 2 Hours

Maximum Marks: 25

**Note :** 1. Answer all the questions.

2. Do not write anything on the question paper except Roll number

3. Assume any data suitably if found missing

**Q.1.** Find in cylindrical coordinates (a) a unit vector  $\mathbf{P}(\rho=5, \phi=53.13^\circ, z=-2)$  in the direction of

$\bar{\mathbf{F}} = \rho z \cos \phi \hat{\mathbf{a}}_\rho - \rho z \sin \phi \hat{\mathbf{a}}_\phi + \rho \hat{\mathbf{a}}_z$ ; (b) a unit vector at  $P$  parallel to  $\hat{\mathbf{a}}_x$ ; (c) unit vector at

$Q(\rho=5, \phi=-36.87, z=-2)$  parallel to  $\hat{\mathbf{a}}_x$ ; (d)  $\bar{\mathbf{G}} = 2\hat{\mathbf{a}}_x - 4\hat{\mathbf{a}}_y + 4\hat{\mathbf{a}}_z$  at  $P$  [4]

**Q.2.** Determine the divergence and curl of the following vector fields: (a)  $\bar{\mathbf{G}} = yz\hat{\mathbf{a}}_x + 4xy\hat{\mathbf{a}}_y + y\hat{\mathbf{a}}_z$ ; (b)

$\bar{\mathbf{A}} = r^2 z \hat{\mathbf{a}}_r + r^3 \hat{\mathbf{a}}_\phi + 3rz^2 \hat{\mathbf{a}}_z$ ; (c)  $\bar{\mathbf{A}} = \frac{1}{\rho^2} \cos \theta \hat{\mathbf{a}}_\rho + \rho \sin \theta \cos \phi \hat{\mathbf{a}}_\theta + \cos \theta \hat{\mathbf{a}}_\phi$  [6]

**Q.3.** A sheet of charge  $\rho_s = 2nC/m^2$  is on the plane  $x=2$  in free space and a line charge

$\rho_l = 20nC/m$  is located at  $x=1, z=4$ . Find (a) the electric field at  $P(0,0,0)$ ; (b)  $\bar{\mathbf{E}}$  and direction

of  $\bar{\mathbf{E}}$  at  $(4,5,6)$ ; (c) What is the force per unit length on the line charge? [4]

**Q.4.** Given the potential field  $V = 50xyz$  volts in free space, find the total energy stored within the cube

$0 < x, y, z < 2$ ; (b) what value would be obtained by assuming a uniform energy density equal to the

value at the centre of the cube? [4]

**Q.5.** A point charge of  $6\mu C$  is located at the origin, a uniform line charge density of  $180nC/m$  lies

along the  $x$ -axis, and a uniform sheet charge of  $25nC/m^2$  lies in the  $z=0$  plane. (a) find  $\bar{\mathbf{D}}$  at

$A(1,2,4)$ ; (b) calculate the total electric flux leaving the surface of sphere of  $4m$  radius centered at

the origin. [4]

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Q.6. A field is given in spherical coordinated at  $P(r=5, \theta=30^\circ, \phi=60^\circ)$  as  $\vec{E} = 20\hat{a}_r - 30\hat{a}_\theta + 60\hat{a}_\phi \text{ V/m}$ . Find the incremental work done in moving a  $10\mu\text{C}$  charge a distance of  $0.8\mu\text{m}$  in the direction (a)  $\hat{a}_r$ ; (b)  $\vec{G} = 2\hat{a}_x + 4\hat{a}_y - 3\hat{a}_z$  [3]