

Roll No.:.....

# National Institute of Technology, Delhi

Name of the Examination: B.Tech.(Makeup- 2018)

Branch :CSE+ECE+EEE

Semester :I+II

Title of the Course :Electromagnetics and  
Quantum Physics

Course Code :PHL100

Time: 3 Hours

Maximum Marks: 50

Note : This question paper divided into three sections A, B and C and each section must be solved with rules given as follows:

Section A: Contains Ten (10) questions of 01 mark each and all questions are compulsory.

Section B: Contains Five (05) questions of 5 marks each and any four (04) are to be attempted.

Section C: Contains Three (03) questions of ten (10) marks each and any two (02) are to be attempted.

Assume suitable data, if found missing.

Used symbols have their usual meaning.

## Section A

Q1: A vector field  $\mathbf{A}$  is said to be solenoidal, if.....

Q2: Magnetic vector potential is expressed as.....

Q3: In a single slit diffraction pattern for a slit width ( $d$ ) and wavelength ( $\lambda$ ), the separation between the central maximum and the first minimum is .....

Q4: The expectation value of momentum of a particle of mass  $m$  moving freely between  $x = 0$  and  $x = L$  inside an infinite square well potential is .....

Q5: The Laser beam is made of .....

Q6: The basic mechanism responsible for the emission of light in semiconductor diode laser is .....

Q7: de-Broglie wavelength in terms of applied electric potential is expressed as .....

Q8: The two sources of light are said to be....., if they emit continuously the wave either in the same phase or with a constant phase difference.

Q9: Single mode property can be realized in a multimode fibre by ..... the value of fractional refractive index change.

Q10: Momentum of the photon whose total energy is  $E$  will be .....

## Section B

**Q1:** Write down the Maxwell's equations for the linear, isotropic, homogeneous and charge free dielectric medium and show that wave phase speed in such a medium is equal to  $\frac{1}{\sqrt{\frac{\epsilon\mu}{2} \left[ \sqrt{1 + \left[ \frac{\sigma}{\omega\epsilon} \right]^2} + 1 \right]}}$ . (5)

**Q2:[a]:** What is acceptance angle of the optical fibre? Show that in a step index optical fibre acceptance angle is approximated by  $\delta = \sin^{-1}[\sqrt{n_1^2 - n_2^2}]$ , where  $n_1$  and  $n_2$  are the refractive indices of core and cladding respectively. (2)

**[b]:** What do you understand the phenomenon of pulse dispersion in optical fibre communication system? A step-index fibre is with a core of refractive index 1.55 and cladding of refractive index 1.51. Compute the intermodal dispersion per kilometer of length of the fibre and the total dispersion in a 15 km length of the fibre. (3)

**Q: 3-[a]:** Express the vector  $\mathbf{V} = \frac{1.0}{r} \mathbf{a}_r + r \cos\theta \mathbf{a}_\theta + \mathbf{a}_\phi$  in the cylindrical coordinate and find out the value of  $\mathbf{V} \left( 5, \frac{\pi}{2}, -2 \right)$ . (3)

**[b]:** What do you understand by the processes of spontaneous and stimulated emissions? Why is the laser action not feasible in two levels pumping scheme? (2)

**Q4.** Obtain Heisenberg's uncertainty principle by using deBroglie's wave concept and further show the non-existence of electron inside the nucleus by this principle. (5)

**Q5.** What are the main differences exist between interference and diffraction? For a plane transmission grating with 5000 lines/cm:

- (i)-What is the highest order of spectrum observable with light of  $6000 \text{ \AA}$  and
- (ii)-If the width of the opacity is twice that of transparency, find the absent orders of spectra. (5)

(a) In the case of negative energies, show that this particle has only one bound state; find the binding energy and wavefunction.

(b) Calculate the probability of the finding the particle in the interval  $-a \leq x \leq a$ .

(5)

[b]: What do you mean by normalized wave function? Find out the expressions of the first three lower energy state wavefunctions and energies for a particle when is confined in an infinite potential well.

(5)

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### Section C

**Q1:-[a]:** A circular disk of radius  $r$  is uniformly charged with  $\rho_s \text{ C/m}^2$ . The disk lies on the  $z = 0$  plane with its axis along the  $z$ -axis.

(i) – Find the value of the electric field ( $\mathbf{E}$ ) at point,  $(0, 0, h)$ ,

(ii) If  $r \ll h$ , show that  $\mathbf{E}$  is similar to the field due to a point charge. (5)

**[b]:** Calculate the wavelength of incident  $x$ -ray photon which produces recoil electron of energy  $4.0 \text{ KeV}$  in Compton effect. The electron recoils in the direction of incident photon and photon is scattered at an angle of  $180^\circ$ . (3)

**[c]:** For an ordinary light source, the coherence time is  $10^{-10} \text{ s}$ . Obtain the degree of monochromaticity for the wavelength of  $6000 \text{ \AA}$ . (2)

**Q2:[a]:** Consider a one-dimensional particle which is confined within the region  $0 \leq x \leq a$  and whose wavefunction is  $\Psi(x, t) = \sin(\pi x/a) \exp(-i\omega t)$ .

(a) Find the potential  $V(x)$ .

(b) Calculate the probability of finding the particle in the interval  $a/4 \leq x \leq 3a/4$ . (5)

**[b]:** Suppose two identical conducting wires, lying along the  $x$ -axis are separated by an air gap of thickness  $L = 1 \text{ nm}$ . An electron is moving inside either conductor has potential energy zero, whereas in the gap its potential energy  $U > 0$ . Thus, the gap is a kind of barrier. The electron approaches the barrier from the left with energy such that  $U - E = 1 \text{ eV}$ , below the top of the barrier. Find the probability of the electron emerging on the side of the barrier? If the barrier is twice as wide how the probability changes? (5)

**Q3:[a]:** Consider a particle of mass  $m$  subject to an attractive delta potential  $V(x) = -V_0 \delta(x)$ , where  $V_0 > 0$ , ( $V_0$  has the dimension of energy  $\times$  distance).