

National Institute of Technology, Delhi

Name of the Examination: B. Tech.

Branch	: ECE	Semester	: 3rd
Title of the Course	: Electromagnetic Theory	Course Code	: ECL203
Time: 2 Hours		Maximum Marks: 25	

Note : All questions are compulsory

Section A (Attempt all questions. All questions have 1 mark each)

1. Plane wave in a dielectric show that:
 - (a) The electric and magnetic vectors are both perpendicular to the direction of propagation
 - (b) The electric and magnetic vectors are in phase
 - (c) Both (a) and (b)
 - (d) None of these
2. Ampere's circuital law is valid for
 - (a) Varying current only
 - (b) steady current only
 - (c) alternative current only
 - (d) none of these
3. $\nabla \cdot \mathbf{B} = 0$ signifies that
 - (a) B is a conservative field
 - (b) magnetic monopole doesn't exist
 - (c) $B=0$
 - (d) there exists a magnetic monopole
4. In a dielectric medium, the phase difference between E and B is
 - (a) zero
 - (b) $\pi/2$
 - (c) π
 - (d) any non zero value
5. The equation of continuity explains
 - (a) non-conservative nature of charge
 - (b) conservation of charge for a static electric field
 - (c) conservation of charge for a non-static electric field
 - (d) non-destructive nature of charge
6. The capacitance of a capacitor filled by a linear dielectric is independent of the charge on the plates and the potential difference between the plates.
 - (a) True
 - (b) False
7. Seawater has $\epsilon_r = 80$. Its permittivity is
 - (a) 81
 - (b) 79
 - (c) 5.162×10^{-10} F/m
 - (d) 7.074×10^{-10} F/m
8. Find the angle between the face diagonals of a cube.
9. Define the terms of gradient, divergence, and curl.

Section B (Attempt all questions. Each question carries 2 marks each)

10. Determine the dot product of the position vectors of the following two points: A(5, 53.13°, 1) and B(2, 90°, -5).
11. A charge distribution with spherical symmetry has density

$$\rho_v = \begin{cases} \frac{\rho_0 r}{R}, & 0 \leq r \leq R \\ 0, & r > R \end{cases}$$

Determine E everywhere.

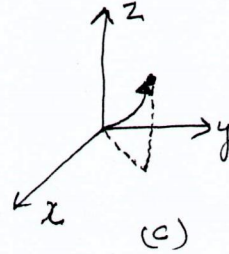
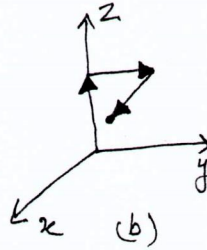
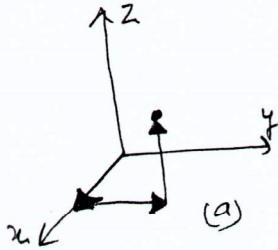
12. Two extensive homogeneous isotropic dielectrics meet on plane $z = 0$. For $z > 0$, $\epsilon_{r1} = 4$ and for $z < 0$, $\epsilon_{r2} = 3$. A uniform electric field $E_1 = 5a_x - 2a_y + 3a_z$ kV/m exists for $z \geq 0$. Find

- E_2 for $z \leq 0$
- The angles E_1 and E_2 make with the interface
- The energy densities (in J/m³) in both dielectrics
- The energy within a cube of side 2m centered at (3, 4, -5)

13. Semi infinite conducting planes at $\phi = 0$ and $\phi = \pi/6$ are separated by an infinitesimal insulating gap. If $V(\phi = 0) = 0$ and $V(\phi = \pi/6) = 100V$, calculate V and E in the region between the planes.

14. Check the fundamental theorem for gradients, using $T = x^2 + 4xy + 2yz^3$, the points $a = (0,0,0)$, $b = (1,1,1)$ and the three paths

- $(0,0,0) \rightarrow (1,0,0) \rightarrow (1,1,0) \rightarrow (1,1,1)$
- $(0,0,0) \rightarrow (0,0,1) \rightarrow (0,1,1) \rightarrow (1,1,1)$
- the parabolic path $z = x^2$; $y = x$



Section C (Attempt all questions. Each question carries 3 marks each)

15. Explain the term polarization. Derive the expression for the potential in-terms of volume bound charge density and surface bound charge density.

16. A hollow spherical shell carries charge density $\rho = k/r^2$ in the region $a \leq r \leq b$. Find the electric field in the three regions: (i) $r < a$, (ii) $a < r < b$ (iii) $r > b$. Plot $|E|$ as a function of 'r'.