

# National Institute of Technology, Delhi

Name of the Examination: B. Tech.

Branch : ECE

Semester : III

Title of the Course : Electromagnetic Theory

Course Code : ECL 203

Time: 2 Hours

Maximum Marks: 25

**Note :** All questions are compulsory. Figure in right hand margin indicates full marks for the question.

- Q1. Write short note on cylindrical coordinate system. [1.5 Marks]
- Q2. Given  $\mathbf{A} = 5\hat{\mathbf{a}}_x$  and  $\mathbf{B} = 4\hat{\mathbf{a}}_x + B_y \hat{\mathbf{a}}_y$ , then find  $B_y$  such that the angle between  $\mathbf{A}$  and  $\mathbf{B}$  is  $45^\circ$ . If  $\mathbf{B}$  also has a term  $B_z \hat{\mathbf{a}}_z$ , what relationship must exist between  $B_y$  and  $B_z$ ? [1.5 Marks]
- Q3. Discuss the following terms [2 Marks]  
 (a) Divergence  
 (b) Curl  
 (c) Gradient  
 (d) Laplacian
- Q4. State and prove Stoke's theorem. [2 Marks]
- Q5. Express vector  $\mathbf{A} = 2xyz\hat{\mathbf{a}}_x - 5(x + y + z)\hat{\mathbf{a}}_z$  in Cylindrical coordinate (variables and components). [2 Marks]
- Q6.  $Q_1$  and  $Q_2$  are the point charges located at (0, -4, 3) and (0, 1, 1). If  $Q_1$  is  $2\text{nC}$ , find  $Q_2$  such that the force on a test charge  $Q$  at (0, -3, 4) has no  $z$  component. [3 Marks]
- Q7. Find  $\mathbf{E}$  at  $P(1, 5, 2)$  m in free space if a point charge of  $6\mu\text{C}$  is located at (0, 0, 1), the uniform line charge with density  $\rho_L = 180 \text{ nC/m}$  along  $x$  axis and uniform sheet of charge with charge density  $\rho_s = 25 \text{ nC/m}^2$  over the plane  $z = -1$ . [3 Marks]
- Q8. Given a vector field  $\mathbf{F} = 30e^{-r}\hat{\mathbf{a}}_r - 2z\hat{\mathbf{a}}_z$  in cylindrical co-ordinates. [3 Marks]  
 (a) Find the total flux due to this field from the closed surface of the cylinder  $r = 3$ ,  $z = 0$  and  $z = 4$ .  
 (b) Verify the divergence theorem.
- Q9. A closed surface is defined in spherical coordinates by  $3 < r < 5$ ,  $0.1\pi < \theta < 0.3\pi$ ,  $1.2\pi < \phi < 1.6\pi$ . [3 Marks]  
 (a) Find the volume enclosed  
 (b) Find distance from  $P_1(r=3, \theta=0.1\pi, \phi=1.2\pi)$  to  $P_2(r=5, \theta=0.3\pi, \phi=1.6\pi)$   
 (c) Find the total surface area.
- Q10. What is Gauss's law? What are the properties of Gaussian surface? Derive the expressions for electric field intensity and electric flux density due to infinite line charge of density  $\rho_l \text{ C/m}$  lying along  $z$ -axis using Gauss's law. [4 Marks]