



# Data Structures & Algorithms



**Tree**

# Tree

A tree is a data structure consisting of finite non-empty set of nodes organized as a hierarchy, with a designated root node (have no parent) and its children (zero or more) represented as a set of linked nodes, where each node is consisting of a value, together with a list of references to nodes (the "children") which are called subtrees of the root.

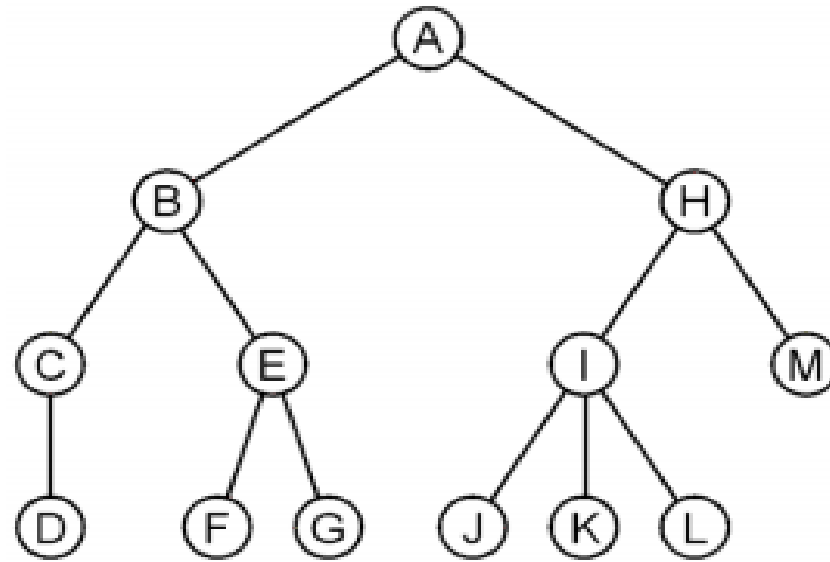


Figure A tree with a root storing the value 'A'.

# Tree

## Terminologies

**Siblings** : Two nodes that are children of the same parent.

**The degree of a node** : the number of children a particular node has.

**Leaf nodes/external node/terminal node** : Nodes of degree zero. A node that has no child nodes.

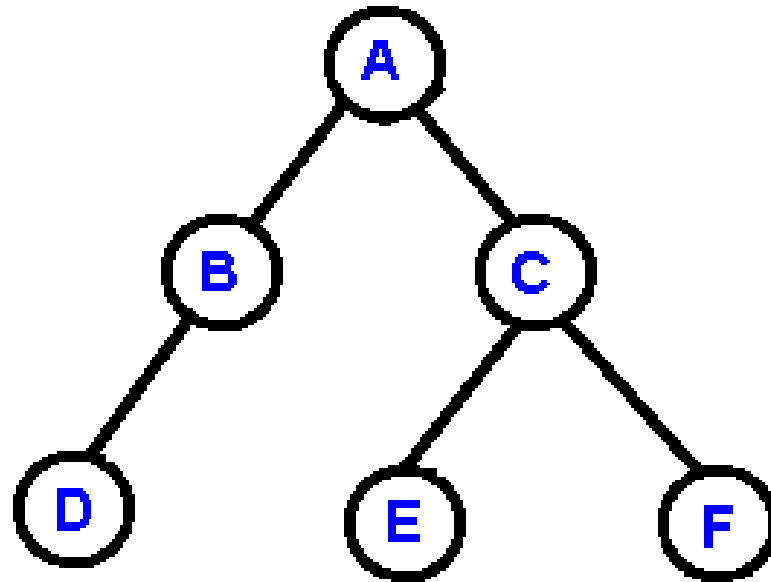
**Non leaf/internal nodes** : All internal nodes which are not leaf nodes. An internal node has at least one child.

For example,

In the previous Figure, the degree of node E is 2, its children are F and G, and its parent is node B. The nodes D, F, G, J, K, L, and M are leaf nodes, while nodes A, B, H, C, E, and I are non leaf nodes.

# Binary Tree

In a binary tree each internal node can have at most/maximum of two child nodes connected to it, i.e. all the nodes have maximum two children, which are referred to as the left child and the right child.



# Binary Tree

## Structure of binary tree nodes

```
typedef struct BinaryTreeNode
{
    struct BinaryTreeNode *left; // Left child
    int data; // The data in the node
    struct BinaryTreeNode *right; // Right child
} BTreeNode;

BTreeNode *root;

root = NULL; // Empty tree
```

## Create a node in a binary tree

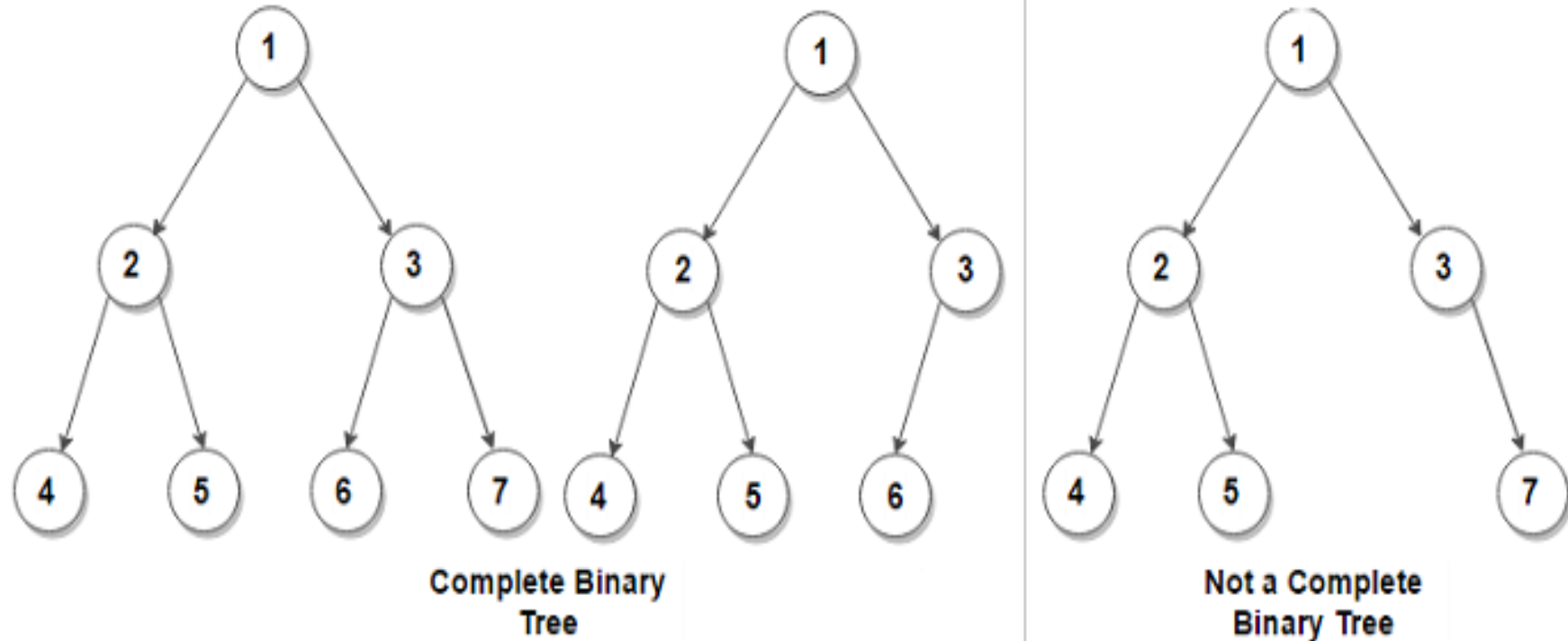
```
new_node = (BTreeNode *) malloc(sizeof(BTreeNode));
root ->data = item;
root ->left = NULL;
root ->right = NULL;
root = new_node;
```

# Variations of Binary Tree

A full binary tree (a.k.a proper binary tree/2-tree) is a tree in which every node other than the leaves has 2 children.

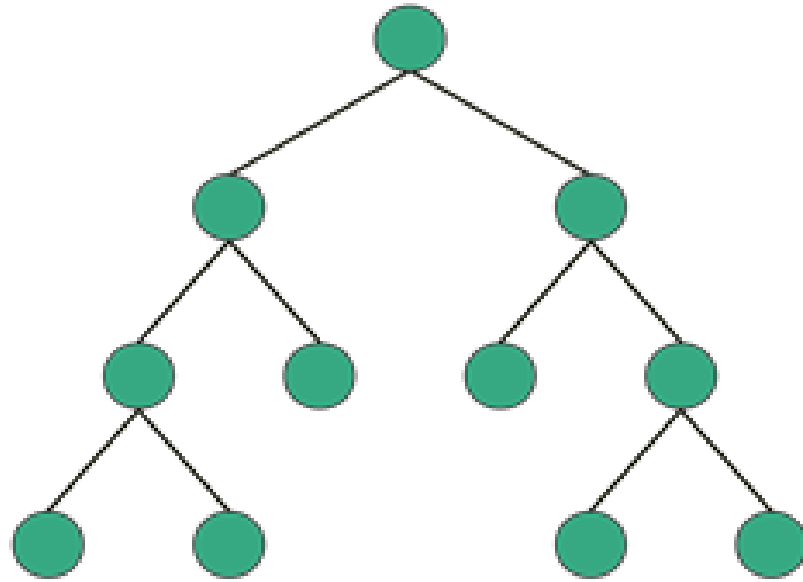
In a **complete** binary tree every level, except possibly the last/bottom, is completely filled, and all nodes in the last level are as far left as possible (filled from left to right).

# Full Binary Tree vs. Complete Binary Tree

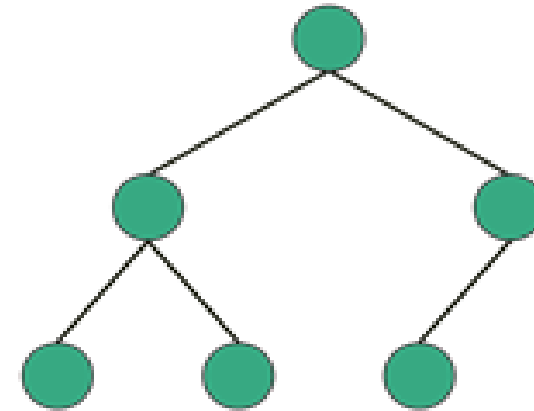




# Full Binary Tree vs Complete Binary Tree

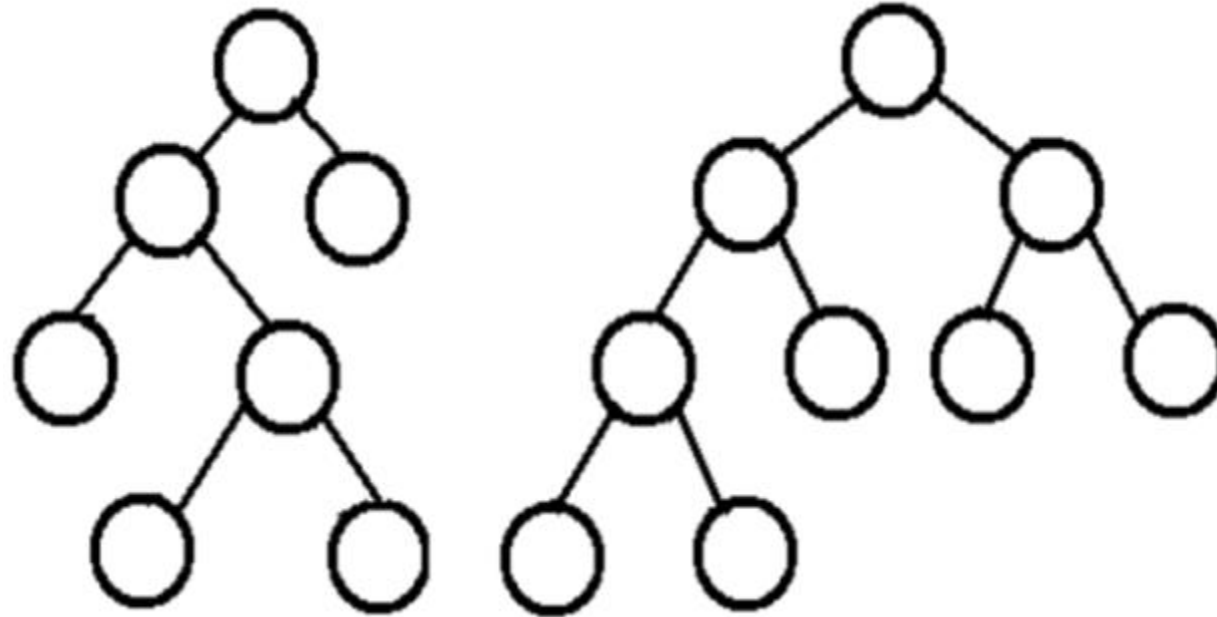


Full



Complete

# Full Binary Tree vs Complete Binary Tree



# Binary Tree

## **Representation/Implementation**

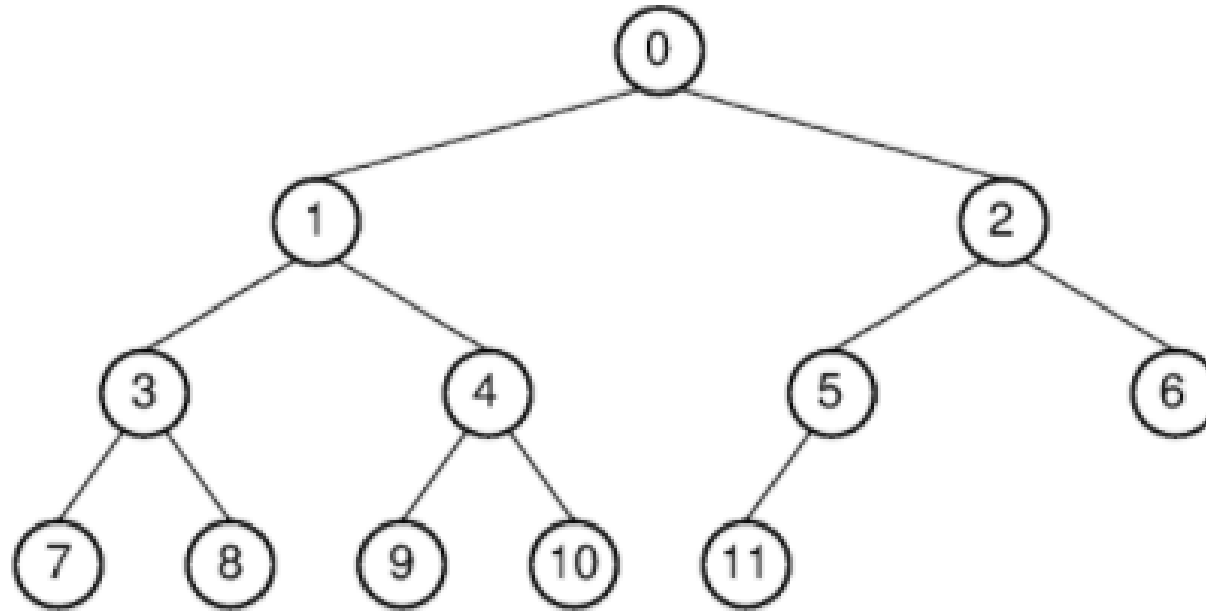
Binary trees can be implemented in two ways:

- a) as one dimensional arrays and
- b) as doubly linked list

# Binary Tree

## An Array Representation of binary tree

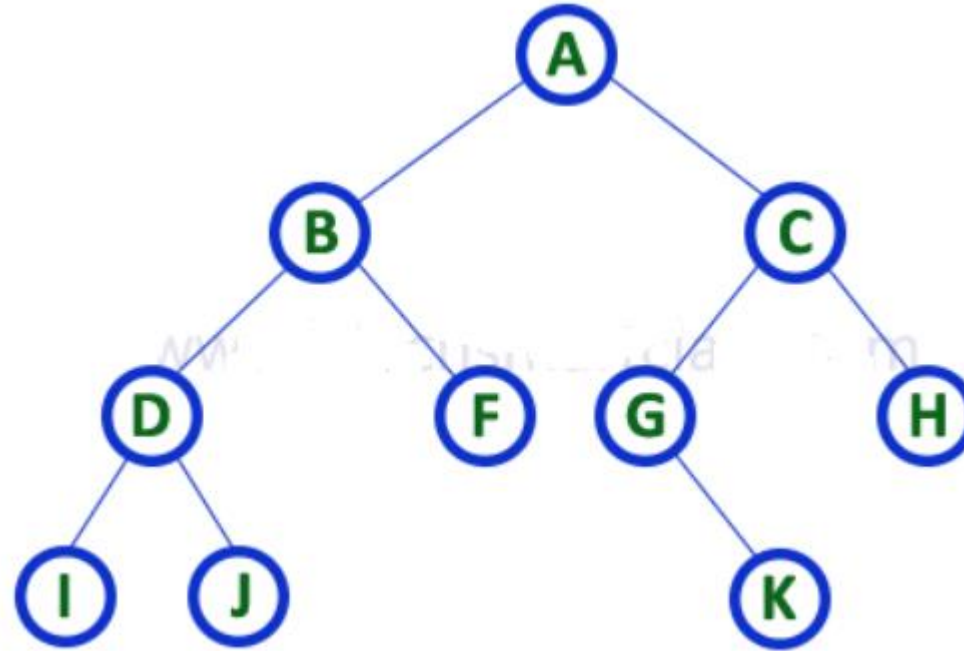
The left child of the node at index  $i$  is at index  $\text{left}(i) = 2i+1$  and the right child of the node at index  $i$  is at index  $\text{right}(i) = 2i+2$ . The parent of the node at index  $i$  is at index  $\text{parent}(i) = (i-1)/2$ .



Position	0	1	2	3	4	5	6	7	8	9	10	11
Parent	--	0	0	1	1	2	2	3	3	4	4	5
Left Child	1	3	5	7	9	11	--	--	--	--	--	--
Right Child	2	4	6	8	10	--	--	--	--	--	--	--

# Binary Tree

## Represent the following binary tree using an array

[illegible]

# Binary Tree

A linked list Representation of binary tree

The previous example of the binary tree represented using Linked list is shown as follows

