

### Linear Algebra Questions – Summary of Answers

- Q1. Dimension of row space and column space → Same always (C)
- Q2. Gram–Schmidt result → Orthogonal vectors spanning same space (a)
- Q3. Trace and determinant → 6 and 6 (c)
- Q4. Max linearly independent vectors → 5 (a)
- Q5. Eigenvector for eigenvalue  $-1$  → Option (b)
- Q6. Matrix defining inner product → Symmetric positive definite (d)
- Q7. Matrix in RREF → Option (b)
- Q8. Frobenius norm squared → 30 (a)
- Q9. Given vectors → Linearly dependent (d)
- Q10. Given vectors → Orthonormal set (b)
- Q11. Positive definite matrix eigenvalues → All positive (a)
- Q12. Characteristic equation →  $\lambda^3 - 27\lambda^2 + 167\lambda - 285 = 0$  (c)
- Q13. Values of a, b, c →  $-6, -4, -9$  (b)
- Q14. Value of  $p + q + pq$  →  $-5$  (c)
- Q15. Not an orthogonal matrix → Option (b)
- Q16. Order of  $(10A - 5B) \blacksquare$  →  $m \times 4$  (a)
- Q17. Value of m → 5 (c)
- Q18. Not a subspace →  $\{(x,y): x \geq 0, y \geq 0\}$  (d)
- Q19. Distance between  $x^2$  and  $x$  →  $4\sqrt{15} / 15$  (d)
- Q20. Vector in span →  $(3,7,11)$  (c)