

31/5/22.

Seminar.

21PC07,
A. Bhadani

1) Compute:

$$15 \times 59 \text{ modulo } 75$$

$$15 \times 59 = 3 \times 5 \times 59$$

$$59 \equiv$$

$$\text{Note that } 59 \equiv -16 \pmod{75}$$

$$\text{Hence } 15 \times 59 \equiv 3 \times 5 \times -16 \pmod{75}$$

$$15 \times 59 \equiv 3 \times -80 \pmod{75}$$

$$15 \times 59 \equiv 3 \times -5$$

$$\boxed{15 \times 59 \text{ modulo } 75 = -15} = \underline{\underline{-15}}$$

2) , Compute $25 \div 16$ modulo 79.

$$\frac{25}{16} \equiv ? \pmod{79}$$

$$\text{Note: } 16 \times 5 = 80 \equiv 1 \pmod{79}$$

$$16 \times 5 \equiv 1 \pmod{79}$$

$$\frac{1}{16} \times \frac{16}{5} \equiv \frac{1}{5} \pmod{79}$$

$$5 \equiv \frac{1}{16} \pmod{79}$$

$$\frac{1}{16} \equiv 5 \pmod{79}$$

$$\frac{25}{16} \equiv 25 \pmod{79}$$

$$\frac{25}{16} \equiv (25 \pmod{79})$$

$$= 46$$

$$\left| \frac{25}{16} \pmod{79} \right| = 46$$