PSG COLLEGE OF TECHNOLOGY

DEPARTMENT OF APPLIED MATHEMATICS AND COMPUTATIONAL SCIENCES M.Sc (CS), 20XC16 MATHEMATICAL FOUNDATIONS LAB

PROBLEM SHEET - 1

Solve the following problems by writing commands in the Command Window.

Calculate:

(a)
$$\frac{(14.8^2 + 6.5^2)}{3.8^2} + \frac{55}{\sqrt{2} + 14}$$

(b)
$$(-3.5)^3 + \frac{e^6}{\ln 524} + 206^{1/3}$$

Calculate:

(a)
$$\frac{16.5^2(8.4-\sqrt{70})}{4.3^2-17.3}$$

(b)
$$\frac{5.2^3 - 6.4^2 + 3}{1.6^8 - 2} + \left(\frac{13.3}{5}\right)^{1.5}$$

Calculate:

(a)
$$15\left(\frac{\sqrt{10} + 3.7^2}{\log_{10}(1365) + 1.9}\right)$$

(b)
$$\frac{2.5^3 \left(16 - \frac{216}{22}\right)}{1.7^4 + 14} + \sqrt[4]{2050}$$

4. Calculate:

(a)
$$\frac{2.3^2 \cdot 1.7}{\sqrt{(1 - 0.8^2)^2 + (2 - \sqrt{0.87})^2}}$$

(b)
$$2.34 + \frac{1}{2}2.7(5.9^2 - 2.4^2) + 9.8 \ln 51$$

Calculate:

(a)
$$\frac{\sin\left(\frac{7\pi}{9}\right)}{\cos^2\left(\frac{5}{7}\pi\right)} + \frac{1}{7}\tan\left(\frac{5}{12}\pi\right)$$

(b)
$$\frac{\tan 64^{\circ}}{\cos^2 14^{\circ}} - \frac{3\sin 80^{\circ}}{\sqrt[3]{0.9}} + \frac{\cos 55^{\circ}}{\sin 11^{\circ}}$$

6. Define the variable x as x = 2.34, then evaluate:

(a)
$$2x^4 - 6x^3 + 14.8x^2 + 9.1$$

(b)
$$\frac{e^{2x}}{\sqrt{14+x^2-x}}$$

7. Define the variable t as t = 6.8, then evaluate:

(a)
$$\ln(|t^2-t^3|)$$

(b)
$$\frac{75}{2t}\cos(0.8t-3)$$

8. Define the variables x and y as x = 8.3 and y = 2.4, then evaluate:

(a)
$$x^2 + y^2 - \frac{x^2}{y^2}$$

(b)
$$\sqrt{xy} - \sqrt{x+y} + \left(\frac{x-y}{x-2y}\right)^2 - \sqrt{\frac{x}{y}}$$

9. Define the variables a, b, c, and d as:

$$a = 13$$
, $b = 4.2$, $c = (4b)/a$, and $d = \frac{abc}{a+b+c}$, then evaluate:

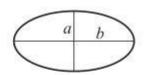
(a)
$$a \frac{b}{c+d} + \frac{da}{cb} - (a-b^2)(c+d)$$

(a)
$$a \frac{b}{c+d} + \frac{da}{cb} - (a-b^2)(c+d)$$
 (b) $\frac{\sqrt{a^2+b^2}}{(d-c)} + \ln(|b-a+c-d|)$

Given: $\int \cos^2(ax)dx = \frac{1}{2}x - \frac{\sin 2ax}{4a}$. Use MATLAB to calculate the following

definite integral: $\int_{\frac{\pi}{0}}^{\frac{3\pi}{5}} \cos^2(0.5x) dx$.

11. The perimeter *P* of an ellipse with semi-minor axes *a* and *b* is given approximately by: $P = 2\pi \sqrt{\frac{1}{2}(a^2 + b^2)}$.

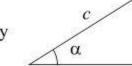


- (a) Determine the perimeter of an ellipse with a = 9 in. and b = 3 in.
- (b) An ellipse with b = 2a has a perimeter of P = 20 cm. Determine a and b.
- 12. Two trigonometric identities are given by:

(a)
$$\sin 4x = 4 \sin x \cos x - 8 \sin^3 x \cos x$$
 (b) $\cos 2x = \frac{1 - \tan^2 x}{1 + \tan^2 x}$

For each part, verify that the identity is correct by calculating the values of the left and right sides of the equation, substituting $x = \frac{\pi}{9}$.

13. In the right triangle shown a = 16 cm and c = 50 cm. Define a and c as variables, and then:



a

- (a) Using the Pythagorean Theorem, calculate b by typing one line in the Command Window.
- (b) Using b from part (a) and the acosd function, calculate the angle α in degrees by typing one line in the Command Window.

14. The distance d from a point (x_0, y_0, z_0) to a plane Ax + By + Cz + D = 0 is given by:

$$d = \frac{|Ax_0 + By_0 + Cz_0 + D|}{\sqrt{A^2 + B^2 + C^2}}$$

Determine the distance of the point (8, 3, -10) from the plane 2x + 23y + 13z - 24 = 0. First define the variables A, B, C, D, x_0 , y_0 , and z_0 , and then calculate d.