

29/9/2021

20XC18 - APPLIED PHYSICS LAB
EXP 2 : SPRING MASS SYSTEMS

S. Vasan
D21PC35

AIM:

1. To find out spring constant, k of springs
2. To find frequency of oscillation of spring mass system

APPARATUS:

Springs of different spring constants, weight hanger, slotted weights, stop watch.

FORMULA:

$$\text{Spring constant, } k = \frac{\text{Restoring force}}{\text{Extension}} \text{ N/m}$$

$$\text{Time period, } T = 2\pi\sqrt{m/k}$$

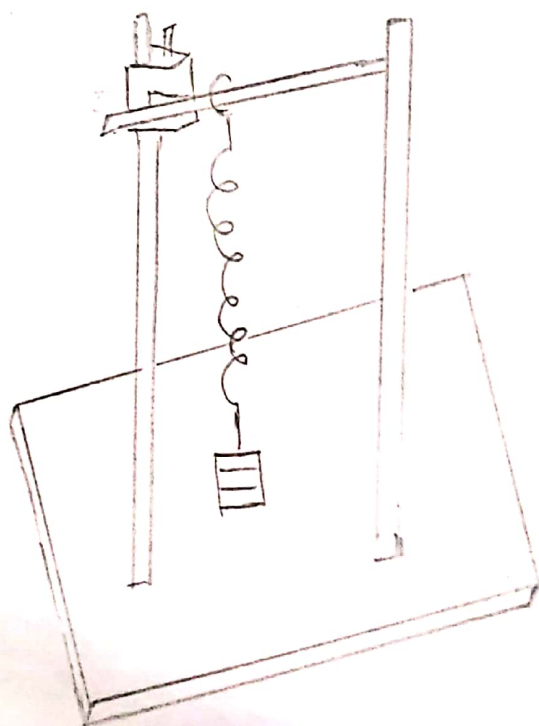
where,

m = mass (kg)

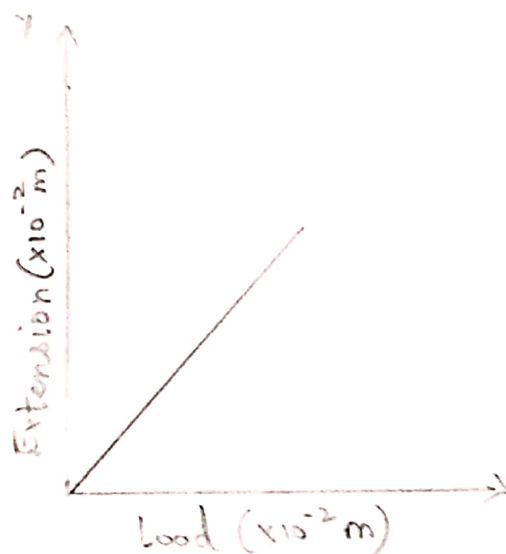
k = spring constant (N/m)

$$\text{Frequency, } F = \frac{1}{T} \text{ Hz}$$

DIAGRAM:



MODEL GRAPH:



PROCEDURE : (To calculate spring constant)

- The spring is suspended vertically from the rigid support.
- A meter scale is kept vertically parallel to the spring.
- A dead weight (W_0) is suspended to the spring and the reading on the meter scale is noted.
- Now slotted weights (50g) are loaded one by one and the loading reading is noted for each case.
- Weights are added till maximum load is reached.
- Now, weights are removed one by one and the unload reading is noted for each case.
- The mean is calculated for noted readings.
- Extension ' x ' is calculated by subtracting reading of dead weight from reading of corresponding slotted mass.
- For each case, spring constant ' k ' is calculated.
- Their average gives the spring constant in (N/m).
- A graph is drawn with load along x axis and extension along y-axis. The inverse of slope of graph gives k .

PROCEDURE : (To calculate frequency of oscillations)

- Note initial position of spring using a meter scale when a dead weight is hanged.
- Pull the string downwards and note the final position and let it oscillate.
- Using a stopwatch, note time taken by the spring for a fixed number of oscillations.
- Repeat the same procedure for various slotted weights and note it in the table and calculate frequency of oscillations.

TABULATION :

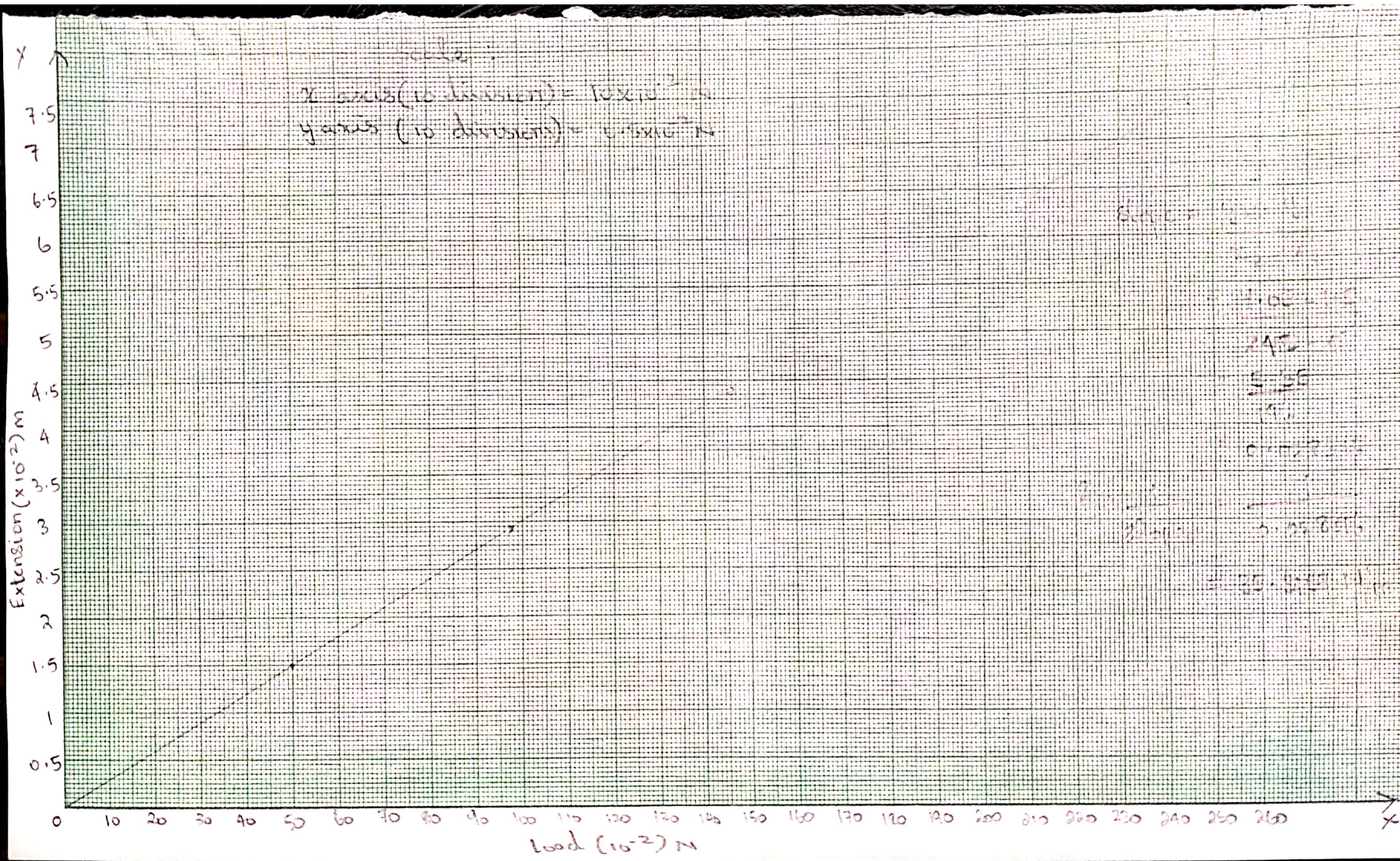
Determination of spring constant :

S.NO	Mass (g)	Mass (kg)m	Load mg(N)	Pointer Reader 'x' cm	Pointer Reading 'y' cm	Mean $Z = \frac{x+y}{2}$	Extension 'l' in cm	Extension 'l' in m	Spring Constant $k = mg/l$ (N/m)
1.	No	0	0	1.5	1.4	1.45	0	0	0
2.	W ₀ +50	0.05	0.49	2.9	3	2.95	1.5	0.015	32.667
3.	W ₀ +100	0.1	0.98	4.3	4.3	4.3	2.85	0.0285	34.386
4.	W ₀ +150	0.15	1.47	5.7	5.7	5.7	4.25	0.0425	34.588
5.	W ₀ +200	0.2	1.96	7.1	7.2	7.15	5.7	0.057	34.386
6.	W ₀ +250	0.25	2.45	8.5	8.5	8.5	7.05	0.0705	34.752

Mean spring constant = 34.1558 N/m

To determine frequency of oscillation of spring mass system :

S.NO	Mass (kg)	Time Period for 20 oscillations			Time period for 1 oscillation (s)	Time Period for 1 oscillation $T = 2\pi\sqrt{\frac{m}{k}}$ (s)	Frequency of oscillations $F = 1/T$ Hz
		Trial 1	Trial 2	Mean			
Spring 1	1	14.7	14.7	14.7	0.735	0.7398	1.3517
Spring 2	1	12.6	12.6	12.6	0.63	0.6312	1.5842
Spring in series	1	19.3	19.3	19.3	0.965	0.9724	1.0283



CALCULATION:

Determine spring constant:

$$W_0 = 0 \text{ kg} ; \quad mg = 9.8 \text{ m/s}^2$$

$$\text{i) Load} = mg$$

$$= (0 \times 9.8) \text{ kg m/s}^2 \text{ or N}$$

$$= 0 \text{ N}$$

$$\text{Mean} = \frac{x+y}{2} = \frac{1.5+1.4}{2} = 1.45 \text{ cm}$$

$$\text{ii) } W_0 + 50 = 0.05 \text{ kg}$$

$$\text{Load} = (0.05 \times 9.8) = 0.49 \text{ N}$$

$$\text{Mean} = \frac{x+y}{2} = \frac{2.9+3}{2} = 2.95 \text{ cm}$$

$$l = 2.95 - 1.45 = 1.5 \text{ cm} = 0.015 \text{ m}$$

$$k = 0.49 / 0.015 = 32.667 \text{ N/m}$$

$$\text{iii) } W_0 + 100 = 0.1 \text{ kg}$$

$$\text{Load} = mg = 0.98 \text{ N}$$

$$\text{Mean} = \frac{x+y}{2} = \frac{4.3+4.3}{2} = 4.3 \text{ cm}$$

$$l = 4.3 - 1.45 = 2.85 \text{ cm} = 0.0285 \text{ m}$$

$$k = mg/l = 0.98 / 0.0285 = 34.386 \text{ N/m}$$

$$\text{iv) } W_0 + 150 = 0.15 \text{ kg}$$

$$\text{Load} = mg = 1.47 \text{ N}$$

$$\text{Mean} = \frac{x+y}{2} = \frac{5.7+5.7}{2} = 5.7 \text{ cm}$$

$$l = 5.7 - 1.45 = 4.25 \text{ cm} = 0.0425 \text{ m}$$

$$k = mg/l = 1.47 / 0.0425 = 34.588 \text{ N/m}$$

$$v) W_0 + 200 = 0.2 \text{ kg}$$

$$\text{load} = mg = 1.96 \text{ N}$$

$$\text{Mean} = \frac{x+y}{2} = \frac{7.1+7.2}{2} = 7.15 \text{ cm}$$

$$l = 7.15 - 1.45 = 5.7 \text{ cm} = 0.057 \text{ m}$$

$$k = mg/l = 1.96/0.057 = 34.386$$

$$vi) W_0 + 250 = 0.25 \text{ kg}$$

$$\text{Load} = 2.45 \text{ N}$$

$$\text{Mean} = \frac{x+y}{2} = \frac{8.5+8.5}{2} = 8.5 \text{ cm}$$

$$l = 8.5 - 1.45 = 7.05 \text{ cm} = 0.0705 \text{ m}$$

$$k = mg/l = 2.45/0.0705 = 34.752 \text{ N/m}$$

Mean spring constant =

$$\frac{32.667 + 34.386 + 34.588 + 34.386 + 34.752}{5} = 34.1558 \text{ N/m}$$

To determine frequency of oscillation of spring mass system

Spring 1 :

$$i) m_1 = 1 \text{ kg} ;$$

$$\text{Time period for one oscillation} = \frac{14.7}{20} = 0.735 \text{ s}$$

$$l = 13.6 \text{ cm} = 0.136 \text{ m}$$

$$k = \frac{mg}{l} = \frac{9.8}{0.136} = 72.0588 \text{ N/m}$$

$$\text{Time period for 1 oscillation} = 2\pi\sqrt{\frac{m}{k}} = 2 \times 3.14 \times \sqrt{\frac{1}{72.0588}}$$

$$= 6.28 \times 0.1178$$

$$= 0.7398 \text{ s}$$

$$\text{Frequency} = \frac{1}{T} = \frac{1}{0.7398} = 1.3517 \text{ Hz}$$

Spring 2 :

$$\text{Time period for 1 oscillation} = \frac{12.6}{20} = 0.63 \text{ s}$$

$$l = 9.9 \text{ cm} = 0.099 \text{ m}$$

$$k = mg/l = \frac{9.8}{0.099} = 98.9898 \text{ N/m}$$

$$\begin{aligned} \text{Time period for 1 oscillation} &= 2\pi \sqrt{\frac{m}{k}} = 2 \times 3.14 \times \sqrt{\frac{1}{98.9898}} \\ &= 6.28 \times 0.1005 \\ &= 0.6312 \text{ s} \end{aligned}$$

$$\text{Frequency} = 1/T = \frac{1}{0.6312} = 1.5842 \text{ Hz}$$

Both in series :

$$\text{Time period for 1 oscillation} = \frac{19.3}{20} = 0.965 \text{ s}$$

$$l = 23.5 \text{ cm} = 0.235 \text{ m}$$

$$k = mg/l = \frac{9.8}{0.235} = 41.7021 \text{ N/m}$$

$$\text{Time period for 1 oscillation} = 2\pi \sqrt{\frac{m}{k}} = 6.28 \times \sqrt{\frac{1}{41.7021}}$$

$$= 6.28 \times 0.1548 = 0.97248$$

$$\text{Frequency} = 1/T = \frac{1}{0.9724} = 1.0283 \text{ Hz}$$

\therefore Experimental value of m_1, m_2, m_3 = Theoretical value of time period.

RESULT :

Mean spring constant of spring = 34.1558 N/m

Theoretical value of spring constant is approximately equal to the experimental value.

Spring 1:

Time period for 1 oscillation = 0.7398 s

0.7398 s is approximately equal to experimental value

0.735 s .

Frequency of spring 1 = 1.3517 Hz

Spring 2:

Time period of 1 oscillation = ~~0.9724 s~~ 0.6312

0.6312 is approximately equal to experimental value ~~0.4658~~ 0.638

Frequency of spring 2 = 1.5842 Hz .

Both in series:

Time period for 1 oscillation = 0.9724 s .

0.9724 s is approximately equal to experimental value 0.9658

Frequency of both springs in series = 1.0283 Hz .