

EOM =

$$D[\chi, \{t, 2\}] == \left(\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -\alpha \end{pmatrix} \begin{pmatrix} 1 - \frac{1}{A} \end{pmatrix} \right) \cdot \mathcal{V}_1 + \left(\kappa \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -\alpha \end{pmatrix} \begin{pmatrix} 1 - \frac{1}{B} \mathcal{L} \end{pmatrix} \right) \cdot \mathcal{V}_2 - \begin{pmatrix} 0 \\ \gamma \\ 0 \end{pmatrix} // \text{Flatten};$$

$$\{x_1[t] = y_1[t] = y_2[t] = 0, x_2[t] = 2 w_p,$$

$$\theta_p[t] \rightarrow 0\} : \{x_p[t] \rightarrow w_p, y_p[t] \rightarrow \frac{1}{2} (-2 - \gamma - 2 h_p)\}$$

perturbations :

$$\text{In[385]:= EquilibriumPoint} = \{\theta_{p0} \rightarrow 0, x_{p0} \rightarrow w_p, y_{p0} \rightarrow -\left(\frac{1}{2} \gamma + h_p + 1\right)\}$$

$$\text{GivenEquibPoints} = \{x_1[t] \rightarrow 0, y_1[t] \rightarrow 0, y_2[t] \rightarrow 0, x_2[t] \rightarrow 2 w_p\}$$

perturb = {

$$\theta_p[t] \rightarrow \theta_{p0} + \delta\theta[t],$$

$$x_p[t] \rightarrow x_{p0} + \delta x[t],$$

$$y_p[t] \rightarrow y_{p0} + \delta y[t]$$

}

perturbD2 = {

$$D[\theta_p[t], \{t, 2\}] \rightarrow D[\delta\theta[t], \{t, 2\}],$$

$$D[x_p[t], \{t, 2\}] \rightarrow D[\delta x[t], \{t, 2\}],$$

$$D[y_p[t], \{t, 2\}] \rightarrow D[\delta y[t], \{t, 2\}]$$

}

$$\text{Out[385]= } \{\theta_{p0} \rightarrow 0, x_{p0} \rightarrow w_p, y_{p0} \rightarrow -1 - \frac{\gamma}{2} - h_p\}$$

$$\text{Out[386]= } \{x_1[t] \rightarrow 0, y_1[t] \rightarrow 0, y_2[t] \rightarrow 0, x_2[t] \rightarrow 2 w_p\}$$

$$\text{Out[387]= } \{\theta_p[t] \rightarrow \theta_{p0} + \delta\theta[t], x_p[t] \rightarrow x_{p0} + \delta x[t], y_p[t] \rightarrow y_{p0} + \delta y[t]\}$$

$$\text{Out[388]= } \{\theta_p''[t] \rightarrow \delta\theta''[t], x_p''[t] \rightarrow \delta x''[t], y_p''[t] \rightarrow \delta y''[t]\}$$

$$\text{In[445]:= } D[\chi, \{t, 2\}] /. \text{perturbD2}$$

$$\text{Out[445]= } \{\{\delta x''[t]\}, \{\delta y''[t]\}, \{\delta\theta''[t]\}\}$$

$$\text{In[286]:= } \mathbf{Aw} = \mathbf{A} /. \text{nameChange}$$

$$\text{Out[286]= } \sqrt{\left((\sin[\theta_p[t]] h_p + \cos[\theta_p[t]] w_p + x_1[t] - x_p[t])^2 + (-\cos[\theta_p[t]] h_p + \sin[\theta_p[t]] w_p + y_1[t] - y_p[t])^2 \right)}$$

$$\text{In[320]:= } \mathbf{Bw} = \mathbf{B} /. \text{nameChange}$$

$$\text{Out[320]= } \sqrt{\left((\sin[\theta_p[t]] h_p - \cos[\theta_p[t]] w_p + x_2[t] - x_p[t])^2 + (-\cos[\theta_p[t]] h_p - \sin[\theta_p[t]] w_p + y_2[t] - y_p[t])^2 \right)}$$

$$\text{In[343]:= } \text{smallAngleRule} = \{\cos[\delta\theta[t]] \rightarrow 1, \sin[\delta\theta[t]] \rightarrow \delta\theta[t]\}$$

$$\text{Out[343]= } \{\cos[\delta\theta[t]] \rightarrow 1, \sin[\delta\theta[t]] \rightarrow \delta\theta[t]\}$$

```
In[425]:= (v1 = v1 /. nameChange /. perturb /. EquilibriumPoint /. smallAngleRule) //
TraditionalForm
(v2 = v2 /. nameChange /. perturb /. EquilibriumPoint /. smallAngleRule) //
TraditionalForm
```

Out[425]//TraditionalForm=

$$\begin{pmatrix} -\delta x(t) + h_p \delta \theta(t) + x_1(t) \\ \frac{\gamma}{2} - \delta y(t) + w_p \delta \theta(t) + y_1(t) + 1 \\ w_p \left(\frac{\gamma}{2} + h_p - \delta y(t) - \delta \theta(t) (-w_p - \delta x(t) + x_1(t) + y_1(t) + 1) + h_p (-w_p - \delta x(t) + x_1(t) + \delta \theta(t) \left(\frac{\gamma}{2} + h_p - \delta y(t) + y_1(t) + 1 \right)) \right) \end{pmatrix}$$

Out[426]//TraditionalForm=

$$\begin{pmatrix} -2 w_p - \delta x(t) + h_p \delta \theta(t) + x_2(t) \\ \frac{\gamma}{2} - \delta y(t) - w_p \delta \theta(t) + y_2(t) + 1 \\ w_p \left(-\frac{\gamma}{2} - h_p + \delta y(t) + \delta \theta(t) (-w_p - \delta x(t) + x_2(t) - y_2(t) - 1) + h_p (-w_p - \delta x(t) + x_2(t) + \delta \theta(t) \left(\frac{\gamma}{2} + h_p - \delta y(t) + y_2(t) + 1 \right)) \right) \end{pmatrix}$$

```
In[427]:= v1 /. GivenEquibPoints // Simplify
v2 /. GivenEquibPoints // Simplify
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Out[427]= $\left\{ \{-\delta x[t] + h_p \delta \theta[t]\}, \left\{ 1 + \frac{\gamma}{2} - \delta y[t] + w_p \delta \theta[t] \right\}, \right.$

$$\left. \left\{ \frac{1}{2} \left(2 w_p^2 \delta \theta[t] + w_p (2 + \gamma - 2 \delta y[t] + 2 \delta x[t] \delta \theta[t]) + h_p (-2 \delta x[t] + (2 + \gamma + 2 h_p - 2 \delta y[t]) \delta \theta[t]) \right) \right\} \right\}$$

Out[428]= $\left\{ \{-\delta x[t] + h_p \delta \theta[t]\}, \left\{ \frac{1}{2} (2 + \gamma - 2 \delta y[t] - 2 w_p \delta \theta[t]) \right\}, \right.$

$$\left. \left\{ w_p^2 \delta \theta[t] - \frac{1}{2} w_p (2 + \gamma - 2 \delta y[t] + 2 \delta x[t] \delta \theta[t]) + \frac{1}{2} h_p (-2 \delta x[t] + (2 + \gamma + 2 h_p - 2 \delta y[t]) \delta \theta[t]) \right\} \right\}$$

```
In[315]:= (*D[Aw, x_p[t]]
D[Aw, y_p[t]]
D[Aw, theta_p[t]] *)
temp = {x_p[t] -> x_p0, y_p[t] -> y_p0, theta_p[t] -> theta_p0};
"derivatives of 'A' in the 0 point:"
D[Aw^2, x_p[t]] /. temp /. EquilibriumPoint
D[Aw^2, y_p[t]] /. temp /. EquilibriumPoint
D[Aw^2, theta_p[t]] /. temp /. EquilibriumPoint
```

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In[321]:= "derivatives of 'B' in the 0 point:"
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```
D[Bw2, xp[t]] /. temp /. EquilibriumPoint
```

```
D[Bw2, yp[t]] /. temp /. EquilibriumPoint
```

```
D[Bw2, θp[t]] /. temp /. EquilibriumPoint
```

```
Out[321]= derivatives of 'B' in the 0 point:
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```
Out[322]= -2 (-2 wp + x2[t])
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```
Out[323]= -2 (1 +  $\frac{\gamma}{2}$  + y2[t])
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```
Out[324]= 2 hp (-2 wp + x2[t]) - 2 wp (1 +  $\frac{\gamma}{2}$  + y2[t])
```

In[407]:= **n = 1; Ataylor = Series[Aw /. GivenEquibPoints,**

{x_p[t], x_{p0}, n}, {y_p[t], y_{p0}, n}, {θ_p[t], θ_{p0}, n}] /. EquilibriumPoint

$$\text{Out[407]} = \left(\left(\sqrt{\left(-1 - \frac{\gamma}{2} - h_p\right)^2 + 2 \left(-1 - \frac{\gamma}{2} - h_p\right) h_p + h_p^2} - \frac{\left(-1 - \frac{\gamma}{2} - h_p\right) w_p + h_p w_p}{\sqrt{\left(-1 - \frac{\gamma}{2} - h_p\right)^2 + 2 \left(-1 - \frac{\gamma}{2} - h_p\right) h_p + h_p^2}} \theta_p[t] + \right. \\ \left. O[\theta_p[t]]^2 \right) + \left(\frac{-1 - \frac{\gamma}{2}}{\sqrt{\left(-1 - \frac{\gamma}{2} - h_p\right)^2 + 2 \left(-1 - \frac{\gamma}{2} - h_p\right) h_p + h_p^2}} + \right. \\ \left(-\frac{w_p}{\sqrt{\left(-1 - \frac{\gamma}{2} - h_p\right)^2 + 2 \left(-1 - \frac{\gamma}{2} - h_p\right) h_p + h_p^2}} + \frac{\left(-1 - \frac{\gamma}{2}\right) \left(-1 - \frac{\gamma}{2} - h_p\right) w_p + h_p w_p}{\left(\left(-1 - \frac{\gamma}{2} - h_p\right)^2 + 2 \left(-1 - \frac{\gamma}{2} - h_p\right) h_p + h_p^2\right)^{3/2}} \right) \\ \left. \theta_p[t] + O[\theta_p[t]]^2 \right) \left(y_p[t] + 1 + \frac{\gamma}{2} + h_p \right) + O\left[y_p[t] + 1 + \frac{\gamma}{2} + h_p\right]^2 \Bigg) + \\ \left(\left(-\frac{h_p \theta_p[t]}{\sqrt{\left(-1 - \frac{\gamma}{2} - h_p\right)^2 + 2 \left(-1 - \frac{\gamma}{2} - h_p\right) h_p + h_p^2}} + O[\theta_p[t]]^2 \right) + \right. \\ \left(\frac{\left(-1 - \frac{\gamma}{2}\right) h_p \theta_p[t]}{\left(\left(-1 - \frac{\gamma}{2} - h_p\right)^2 + 2 \left(-1 - \frac{\gamma}{2} - h_p\right) h_p + h_p^2\right)^{3/2}} + O[\theta_p[t]]^2 \right) \left(y_p[t] + 1 + \frac{\gamma}{2} + h_p \right) + \\ \left. O\left[y_p[t] + 1 + \frac{\gamma}{2} + h_p\right]^2 \right) \left(x_p[t] - w_p \right) + O[x_p[t] - w_p]^2 \Bigg)$$

In[411]:= **perturb**

Out[411]= {θ_p[t] → θ_{p0} + δθ[t], x_p[t] → x_{p0} + δx[t], y_p[t] → y_{p0} + δy[t]}

In[326]:= **n = 1; Series[Bw, {x_p[t], x_{p0}, n}, {y_p[t], y_{p0}, n}, {θ_p[t], θ_{p0}, n}] /. EquilibriumPoint**

In[367]:= % // Simplify // TraditionalForm

Out[367]//TraditionalForm=

$$\begin{aligned} & \left(\left(\frac{1}{2} \sqrt{(\gamma+2)^2} + \frac{(\gamma+2) w_p \theta_p(t)}{\sqrt{(\gamma+2)^2}} + O(\theta_p(t)^2) \right) + \right. \\ & \quad \left. \left(\frac{\gamma}{2} + h_p + y_p(t) + 1 \right) \left(\frac{-\gamma-2}{\sqrt{(\gamma+2)^2}} + O(\theta_p(t)^2) \right) + O\left(\left(\frac{\gamma}{2} + h_p + y_p(t) + 1 \right)^2 \right) \right) (x_p(t) - w_p) \\ & \quad \left(\left(-\frac{2 h_p \theta_p(t)}{\sqrt{(\gamma+2)^2}} + O(\theta_p(t)^2) \right) + \left(-\frac{4 h_p \theta_p(t)}{(\gamma+2) \sqrt{(\gamma+2)^2}} + O(\theta_p(t)^2) \right) \left(\frac{\gamma}{2} + h_p + y_p(t) + 1 \right) + O\left(\left(\frac{\gamma}{2} + h_p + y_p(t) + 1 \right)^2 \right) \right) + O(\\ & \quad (x_p(t) - w_p)^2) \end{aligned}$$

In[429]:= **Ataylored** = $1 + \frac{\gamma}{2} - \delta y[t] + w \delta \theta[t]$

Btaylored = $1 + \frac{\gamma}{2} - \delta y[t] - w \delta \theta[t]$

Vtaylored₁ = **v1** /. **GivenEquibPoints**

Vtaylored₂ = **v2** /. **GivenEquibPoints**

Out[429]= $1 + \frac{\gamma}{2} - \delta y[t] + w \delta \theta[t]$

Out[430]= $1 + \frac{\gamma}{2} - \delta y[t] - w \delta \theta[t]$

Out[431]= $\left\{ \{-\delta x[t] + h_p \delta \theta[t]\}, \left\{ 1 + \frac{\gamma}{2} - \delta y[t] + w_p \delta \theta[t] \right\}, \right.$
 $\left. \left\{ w_p \left(1 + \frac{\gamma}{2} + h_p - \delta y[t] - (-w_p - \delta x[t]) \delta \theta[t] \right) + h_p \left(-w_p - \delta x[t] + \left(1 + \frac{\gamma}{2} + h_p - \delta y[t] \right) \delta \theta[t] \right) \right\} \right\}$

Out[432]= $\left\{ \{-\delta x[t] + h_p \delta \theta[t]\}, \left\{ 1 + \frac{\gamma}{2} - \delta y[t] - w_p \delta \theta[t] \right\}, \right.$
 $\left. \left\{ w_p \left(-1 - \frac{\gamma}{2} - h_p + \delta y[t] + (w_p - \delta x[t]) \delta \theta[t] \right) + h_p \left(w_p - \delta x[t] + \left(1 + \frac{\gamma}{2} + h_p - \delta y[t] \right) \delta \theta[t] \right) \right\} \right\}$

```
In[390]:= EOM[*,D[X,{t,2}]]==
$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -\alpha \end{pmatrix} \left(1 - \frac{1}{A}\right) \cdot \mathcal{V}_1 + \left(\kappa \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -\alpha \end{pmatrix} \left(1 - \frac{1}{B} \mathcal{L}\right)\right) \cdot \mathcal{V}_2 - \begin{pmatrix} 0 \\ \gamma \\ 0 \end{pmatrix} *$$

(* /.perturbD2*) // TraditionalForm
```

Out[390]//TraditionalForm=

$$\begin{pmatrix} x_p''(t) \\ y_p''(t) \\ \theta_p''(t) \end{pmatrix} = \begin{pmatrix} (\sin(\theta_p(t)) h_p + \cos(\theta_p(t)) l_p + x_1(t) - x_p(t)) \\ -\gamma + \left(1 - \frac{1}{\sqrt{(\sin(\theta_p(t)) h_p + \cos(\theta_p(t)) l_p + x_1(t) - x_p(t))^2 + (-\cos(\theta_p(t)) h_p + \sin(\theta_p(t)) l_p + y_1(t) - y_p(t))^2}}\right) \\ -\alpha (l_p (\cos(\theta_p(t)) (y_1(t) - y_p(t)) - \sin(\theta_p(t)) (x_1(t) - x_p(t))) + h_p (\cos(\theta_p(t)) (x_1(t) - x_p(t)) + \sin(\theta_p(t)) (y_1(t) - y_p(t))) \end{pmatrix}$$

```
(* (EOMrephrase=D[X,{t,2}]]==
$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -\alpha \end{pmatrix} \left(\frac{A-1}{A}\right) \cdot \mathcal{V}_1 + \left(\kappa \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -\alpha \end{pmatrix} \left(\frac{B-\mathcal{L}}{B}\right)\right) \cdot \mathcal{V}_2 - \begin{pmatrix} 0 \\ \gamma \\ 0 \end{pmatrix}$$

(* //Flatten*) //Simplify//TraditionalForm*)
```

```
In[433]:= EOMrephrase = D[X, {t, 2}] A B ==
```

$$B \left(\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -\alpha \end{pmatrix} (A - 1) \right) \cdot \mathcal{V}_1 + A \left(\kappa \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -\alpha \end{pmatrix} (B - \mathcal{L}) \right) \cdot \mathcal{V}_2 - A B \begin{pmatrix} 0 \\ \gamma \\ 0 \end{pmatrix} // \text{TraditionalForm}$$

Out[433]//TraditionalForm=

$$\begin{pmatrix} \sqrt{(\sin(\theta_p(t)) h_p + \cos(\theta_p(t)) l_p + x_1(t) - x_p(t))^2 + (-\cos(\theta_p(t)) h_p + \sin(\theta_p(t)) l_p + y_1(t) - y_p(t))^2} \sqrt{(\sin(\theta_p(t)) h_p - \cos(\theta_p(t)) l_p} \\ \sqrt{(\sin(\theta_p(t)) h_p + \cos(\theta_p(t)) l_p + x_1(t) - x_p(t))^2 + (-\cos(\theta_p(t)) h_p + \sin(\theta_p(t)) l_p + y_1(t) - y_p(t))^2} \sqrt{(\sin(\theta_p(t)) h_p - \cos(\theta_p(t)) l_p} \\ \sqrt{(\sin(\theta_p(t)) h_p + \cos(\theta_p(t)) l_p + x_1(t) - x_p(t))^2 + (-\cos(\theta_p(t)) h_p + \sin(\theta_p(t)) l_p + y_1(t) - y_p(t))^2} \sqrt{(\sin(\theta_p(t)) h_p - \cos(\theta_p(t)) l_p} \end{pmatrix}$$

```
In[447]:= EOMLinearized = (D[X, {t, 2}] /. perturbD2) Ataylored Btaylored ==
```

$$\begin{pmatrix} B_{\text{taylored}} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -\alpha \end{pmatrix} (A_{\text{taylored}} - 1) \\ A_{\text{taylored}} \kappa \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -\alpha \end{pmatrix} (B_{\text{taylored}} - \mathcal{L}) \end{pmatrix} \cdot \mathcal{V}_{\text{taylored}_2} - A_{\text{taylored}} B_{\text{taylored}} \begin{pmatrix} 0 \\ \gamma \\ 0 \end{pmatrix} // \text{TraditionalForm}$$

Out[447]//TraditionalForm=

$$\begin{pmatrix} \left(\frac{\gamma}{2} - \delta y(t) - w \delta \theta(t) + 1\right) \left(\frac{\gamma}{2} - \delta y(t) + w \delta \theta(t) + 1\right) \delta x''(t) \\ \left(\frac{\gamma}{2} - \delta y(t) - w \delta \theta(t) + 1\right) \left(\frac{\gamma}{2} - \delta y(t) + w \delta \theta(t) + 1\right) \delta y''(t) \\ \left(\frac{\gamma}{2} - \delta y(t) - w \delta \theta(t) + 1\right) \left(\frac{\gamma}{2} - \delta y(t) + w \delta \theta(t) + 1\right) \delta \theta''(t) \end{pmatrix} = \begin{pmatrix} -\gamma \left(\frac{\gamma}{2} - \delta y(t) - w \delta \theta(t) + 1\right) \left(\frac{\gamma}{2} - \delta y(t) + w \delta \theta(t) + 1\right) \\ -\alpha \left(\frac{\gamma}{2} - \delta y(t) - w \delta \theta(t) + 1\right) \left(\frac{\gamma}{2} - \delta y(t) + w \delta \theta(t) + 1\right) \left(w_p \left(\frac{\gamma}{2} + h_p - \right.\right. \end{pmatrix}$$

```
In[461]:= EOMLinearized //. (1 +  $\frac{\gamma}{2} \rightarrow \gamma_{12}$ ) //. (-1 -  $\frac{\gamma}{2} \rightarrow -\gamma_{12}$ ) // TraditionalForm
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```
Out[461]//TraditionalForm=
```

$$\begin{pmatrix} (\gamma_{12} - \delta y(t) - w \delta \theta(t)) (\gamma_{12} - \delta y(t) + w \delta \theta(t)) \delta x''(t) \\ (\gamma_{12} - \delta y(t) - w \delta \theta(t)) (\gamma_{12} - \delta y(t) + w \delta \theta(t)) \delta y''(t) \\ (\gamma_{12} - \delta y(t) - w \delta \theta(t)) (\gamma_{12} - \delta y(t) + w \delta \theta(t)) \delta \theta''(t) \end{pmatrix} = \begin{pmatrix} -\gamma (\gamma_{12} - \delta y(t) - w \delta \theta(t)) \\ -\alpha (\gamma_{12} - \delta y(t) - w \delta \theta(t)) \left(\frac{\gamma}{2} - \delta y(t) + w \delta \theta(t) \right) (w_p (\gamma_{12} + h_p - \delta y$$

```
In[462]:= EOMLinearized //. (1 +  $\frac{\gamma}{2} \rightarrow \gamma_{12}$ ) //. (-1 -  $\frac{\gamma}{2} \rightarrow -\gamma_{12}$ )
```

```
Out[462]= { { (\gamma_{12} - \delta y[t] - w \delta \theta[t]) (\gamma_{12} - \delta y[t] + w \delta \theta[t]) \delta x''[t] },
  { (\gamma_{12} - \delta y[t] - w \delta \theta[t]) (\gamma_{12} - \delta y[t] + w \delta \theta[t]) \delta y''[t] },
  { (\gamma_{12} - \delta y[t] - w \delta \theta[t]) (\gamma_{12} - \delta y[t] + w \delta \theta[t]) \delta \theta''[t] } } ==
{ { (\gamma_{12} - \delta y[t] - w \delta \theta[t]) \left( \frac{\gamma}{2} - \delta y[t] + w \delta \theta[t] \right) (-\delta x[t] + h_p \delta \theta[t]) +
  \kappa (-\mathcal{L} + \gamma_{12} - \delta y[t] - w \delta \theta[t]) (\gamma_{12} - \delta y[t] + w \delta \theta[t]) (-\delta x[t] + h_p \delta \theta[t]) },
  { -\gamma (\gamma_{12} - \delta y[t] - w \delta \theta[t]) (\gamma_{12} - \delta y[t] + w \delta \theta[t]) +
  \kappa (-\mathcal{L} + \gamma_{12} - \delta y[t] - w \delta \theta[t]) (\gamma_{12} - \delta y[t] + w \delta \theta[t]) (\gamma_{12} - \delta y[t] - w_p \delta \theta[t]) +
  (\gamma_{12} - \delta y[t] - w \delta \theta[t]) \left( \frac{\gamma}{2} - \delta y[t] + w \delta \theta[t] \right) (\gamma_{12} - \delta y[t] + w_p \delta \theta[t]) },
  { -\alpha (\gamma_{12} - \delta y[t] - w \delta \theta[t]) \left( \frac{\gamma}{2} - \delta y[t] + w \delta \theta[t] \right)
  (w_p (\gamma_{12} + h_p - \delta y[t] - (-w_p - \delta x[t]) \delta \theta[t]) +
  h_p (-w_p - \delta x[t] + (\gamma_{12} + h_p - \delta y[t]) \delta \theta[t])) - \alpha \kappa (-\mathcal{L} + \gamma_{12} - \delta y[t] - w \delta \theta[t])
  (\gamma_{12} - \delta y[t] + w \delta \theta[t]) (w_p (-\gamma_{12} - h_p + \delta y[t] + (w_p - \delta x[t]) \delta \theta[t]) +
  h_p (w_p - \delta x[t] + (\gamma_{12} + h_p - \delta y[t]) \delta \theta[t])) } }
```

```
In[457]:= EOMLinearized /. (1 +  $\frac{\gamma}{2}$  →  $\gamma_{12}$ )
```

```
Out[457]= {{ (  $\gamma_{12} - \delta y[t] - w \delta \theta[t]$  ) (  $\gamma_{12} - \delta y[t] + w \delta \theta[t]$  )  $\delta x''[t]$  },
  { (  $\gamma_{12} - \delta y[t] - w \delta \theta[t]$  ) (  $\gamma_{12} - \delta y[t] + w \delta \theta[t]$  )  $\delta y''[t]$  },
  { (  $\gamma_{12} - \delta y[t] - w \delta \theta[t]$  ) (  $\gamma_{12} - \delta y[t] + w \delta \theta[t]$  )  $\delta \theta''[t]$  } } ==
  { { (  $\gamma_{12} - \delta y[t] - w \delta \theta[t]$  ) (  $\frac{\gamma}{2} - \delta y[t] + w \delta \theta[t]$  ) (  $-\delta x[t] + h_p \delta \theta[t]$  ) +
     $\kappa (-\mathcal{L} + \gamma_{12} - \delta y[t] - w \delta \theta[t]) (\gamma_{12} - \delta y[t] + w \delta \theta[t]) (-\delta x[t] + h_p \delta \theta[t])$  },
    {  $-\gamma (\gamma_{12} - \delta y[t] - w \delta \theta[t]) (\gamma_{12} - \delta y[t] + w \delta \theta[t]) +$ 
     $\kappa (-\mathcal{L} + \gamma_{12} - \delta y[t] - w \delta \theta[t]) (\gamma_{12} - \delta y[t] + w \delta \theta[t]) (\gamma_{12} - \delta y[t] - w_p \delta \theta[t]) +$ 
     $(\gamma_{12} - \delta y[t] - w \delta \theta[t]) (\frac{\gamma}{2} - \delta y[t] + w \delta \theta[t]) (\gamma_{12} - \delta y[t] + w_p \delta \theta[t])$  },
    {  $-\alpha (\gamma_{12} - \delta y[t] - w \delta \theta[t]) (\frac{\gamma}{2} - \delta y[t] + w \delta \theta[t])$ 
     $(w_p (\gamma_{12} + h_p - \delta y[t] - (-w_p - \delta x[t]) \delta \theta[t]) +$ 
     $h_p (-w_p - \delta x[t] + (\gamma_{12} + h_p - \delta y[t]) \delta \theta[t])) - \alpha \kappa (-\mathcal{L} + \gamma_{12} - \delta y[t] - w \delta \theta[t])$ 
     $(\gamma_{12} - \delta y[t] + w \delta \theta[t]) (w_p (-1 - \frac{\gamma}{2} - h_p + \delta y[t] + (w_p - \delta x[t]) \delta \theta[t]) +$ 
     $h_p (w_p - \delta x[t] + (\gamma_{12} + h_p - \delta y[t]) \delta \theta[t]))$  } }
```

Eliminate

```
In[448]:= EOMLinearized // Expand // TraditionalForm
```

```
Out[448]//TraditionalForm=
```

$$\begin{pmatrix} \frac{1}{4} \delta x''(t) \gamma^2 - \delta y(t) \delta x''(t) \gamma + \delta x''(t) \gamma + \delta y(t)^2 \delta x''(t) - w^2 \delta \theta(t)^2 \delta x''(t) - 2 \delta y(t) \delta x''(t) + \delta x''(t) \\ \frac{1}{4} \delta y''(t) \gamma^2 - \delta y(t) \delta y''(t) \gamma + \delta y''(t) \gamma + \delta y(t)^2 \delta y''(t) - w^2 \delta \theta(t)^2 \delta y''(t) - 2 \delta y(t) \delta y''(t) + \delta y''(t) \\ \frac{1}{4} \delta \theta''(t) \gamma^2 - \delta y(t) \delta \theta''(t) \gamma + \delta \theta''(t) \gamma + \delta y(t)^2 \delta \theta''(t) - w^2 \delta \theta(t)^2 \delta \theta''(t) - 2 \delta y(t) \delta \theta''(t) + \delta \theta''(t) \end{pmatrix} = \begin{pmatrix} -\frac{1}{8} \alpha w_p \gamma^3 + \frac{1}{8} \alpha \kappa w_p \end{pmatrix}$$

```
In[450]:= temp2 = EOMLinearized // Expand
```


In[454]:= **Collect[temp2, $\delta x[t]$ $\delta y[t]$, Simplify]**

$$\begin{aligned} \text{Out[454]} = & \left\{ \left\{ \frac{1}{4} \left((2+\gamma)^2 - 4(2+\gamma)\delta y[t] + 4\delta y[t]^2 - 4w^2\delta\theta[t]^2 \right) \delta x''[t] \right\}, \right. \\ & \left\{ \frac{1}{4} \left((2+\gamma)^2 - 4(2+\gamma)\delta y[t] + 4\delta y[t]^2 - 4w^2\delta\theta[t]^2 \right) \delta y''[t] \right\}, \\ & \left\{ \frac{1}{4} \left((2+\gamma)^2 - 4(2+\gamma)\delta y[t] + 4\delta y[t]^2 - 4w^2\delta\theta[t]^2 \right) \delta\theta''[t] \right\} \} = \\ & \left\{ \left\{ (1+\gamma+2\kappa-\mathcal{L}\kappa+\gamma\kappa) \delta x[t] \delta y[t] + \right. \right. \\ & \quad \frac{1}{4} \left(-\delta x[t] \left((2+\gamma)(\gamma+2\kappa-2\mathcal{L}\kappa+\gamma\kappa) + 4(1+\kappa)\delta y[t]^2 - 4w(-1+\mathcal{L}\kappa)\delta\theta[t] - 4w^2 \right. \right. \\ & \quad \left. \left. (1+\kappa)\delta\theta[t]^2 \right) + h_p \delta\theta[t] \left((2+\gamma)(\gamma+2\kappa-2\mathcal{L}\kappa+\gamma\kappa) - 4(1+\gamma+2\kappa-\mathcal{L}\kappa+\gamma\kappa) \right. \right. \\ & \quad \left. \left. \delta y[t] + 4(1+\kappa)\delta y[t]^2 - 4w(-1+\mathcal{L}\kappa)\delta\theta[t] - 4w^2(1+\kappa)\delta\theta[t]^2 \right) \right\}, \\ & \left\{ \frac{1}{8} \left((2+\gamma)^2(\gamma(-1+\kappa) - 2(-1+\mathcal{L})\kappa) - 8(1+\kappa)\delta y[t]^3 - \right. \right. \\ & \quad 2(2+\gamma)(2w(-1+\mathcal{L}\kappa) + (\gamma(-1+\kappa) - 2(-1+\mathcal{L})\kappa)w_p)\delta\theta[t] + \\ & \quad 4w(w(\gamma-\gamma\kappa-2(1+\kappa)) + 2(1+\mathcal{L}\kappa)w_p)\delta\theta[t]^2 + 8w^2(-1+\kappa)w_p\delta\theta[t]^3 + \\ & \quad 4\delta y[t]^2(4+\gamma+6\kappa-2\mathcal{L}\kappa+3\gamma\kappa-2(-1+\kappa)w_p\delta\theta[t]) - \\ & \quad 2\delta y[t] \left((2+\gamma)(2+(6-4\mathcal{L})\kappa+\gamma(-1+3\kappa)) + \right. \\ & \quad \left. 4(w-w\mathcal{L}\kappa+(1+\gamma+(-2+\mathcal{L})\kappa-\gamma\kappa)w_p)\delta\theta[t] - 4w^2(1+\kappa)\delta\theta[t]^2 \right) \left. \right\}, \\ & \left\{ -\alpha \delta x[t] \delta y[t] \left((1+\gamma+2\kappa-\mathcal{L}\kappa+\gamma\kappa)h_p + (-1+\gamma(-1+\kappa)+2\kappa-\mathcal{L}\kappa)w_p\delta\theta[t] \right) + \right. \\ & \quad \frac{1}{8} \alpha \left(-2w_p^2\delta\theta[t] \left((2+\gamma)(\gamma+2\kappa-2\mathcal{L}\kappa+\gamma\kappa) - 4(1+\gamma+2\kappa-\mathcal{L}\kappa+\gamma\kappa)\delta y[t] + \right. \right. \\ & \quad 4(1+\kappa)\delta y[t]^2 - 4w(-1+\mathcal{L}\kappa)\delta\theta[t] - 4w^2(1+\kappa)\delta\theta[t]^2 \right) + \\ & \quad w_p \left(-8(-1+\kappa)\delta y[t]^3 + 4\delta y[t]^2(-4+3\gamma(-1+\kappa)+6\kappa-2\mathcal{L}\kappa+2(-1+\kappa) \right. \\ & \quad \left. \delta x[t]\delta\theta[t]) + (2+\gamma+2\delta x[t]\delta\theta[t]) \left((2+\gamma)(\gamma(-1+\kappa)-2(-1+\mathcal{L})\kappa) - \right. \right. \\ & \quad 4(w+w\mathcal{L}\kappa)\delta\theta[t] - 4w^2(-1+\kappa)\delta\theta[t]^2 \right) + 2\delta y[t] \left(-(2+\gamma) \right. \\ & \quad \left. (-2+3\gamma(-1+\kappa)+6\kappa-4\mathcal{L}\kappa) + 4(w+w\mathcal{L}\kappa)\delta\theta[t] + 4w^2(-1+\kappa)\delta\theta[t]^2 \right) \left. \right\} + \\ & \quad h_p \left(2\delta x[t] \left((2+\gamma)(\gamma+2\kappa-2\mathcal{L}\kappa+\gamma\kappa) + 4(1+\kappa)\delta y[t]^2 - 4w(-1+\mathcal{L}\kappa)\delta\theta[t] - \right. \right. \\ & \quad \left. 4w^2(1+\kappa)\delta\theta[t]^2 \right) - (2+\gamma+2h_p-2\delta y[t])\delta\theta[t] \\ & \quad \left. \left((2+\gamma)(\gamma+2\kappa-2\mathcal{L}\kappa+\gamma\kappa) - 4(1+\gamma+2\kappa-\mathcal{L}\kappa+\gamma\kappa)\delta y[t] + \right. \right. \\ & \quad \left. \left. 4(1+\kappa)\delta y[t]^2 - 4w(-1+\mathcal{L}\kappa)\delta\theta[t] - 4w^2(1+\kappa)\delta\theta[t]^2 \right) \right\} \right\} \end{aligned}$$

$$\begin{aligned} \text{Out[450]} = & \left\{ \left\{ \delta x''[t] + \gamma \delta x''[t] + \frac{1}{4} \gamma^2 \delta x''[t] - \right. \right. \\ & 2\delta y[t] \delta x''[t] - \gamma \delta y[t] \delta x''[t] + \delta y[t]^2 \delta x''[t] - w^2 \delta\theta[t]^2 \delta x''[t] \left. \right\}, \\ & \left\{ \delta y''[t] + \gamma \delta y''[t] + \frac{1}{4} \gamma^2 \delta y''[t] - 2\delta y[t] \delta y''[t] - \gamma \delta y[t] \delta y''[t] + \right. \\ & \delta y[t]^2 \delta y''[t] - w^2 \delta\theta[t]^2 \delta y''[t] \left. \right\}, \left\{ \delta\theta''[t] + \gamma \delta\theta''[t] + \frac{1}{4} \gamma^2 \delta\theta''[t] - \right. \\ & 2\delta y[t] \delta\theta''[t] - \gamma \delta y[t] \delta\theta''[t] + \delta y[t]^2 \delta\theta''[t] - w^2 \delta\theta[t]^2 \delta\theta''[t] \left. \right\} = \\ & \left\{ \left\{ -\frac{1}{2} \gamma \delta x[t] - \frac{1}{4} \gamma^2 \delta x[t] - \kappa \delta x[t] + \mathcal{L} \kappa \delta x[t] - \gamma \kappa \delta x[t] + \frac{1}{2} \mathcal{L} \gamma \kappa \delta x[t] - \frac{1}{4} \gamma^2 \kappa \delta x[t] + \right. \right. \\ & \delta x[t] \delta y[t] + \gamma \delta x[t] \delta y[t] + 2\kappa \delta x[t] \delta y[t] - \mathcal{L} \kappa \delta x[t] \delta y[t] + \gamma \kappa \delta x[t] \delta y[t] - \\ & \delta x[t] \delta y[t]^2 - \kappa \delta x[t] \delta y[t]^2 + \frac{1}{2} \gamma h_p \delta\theta[t] + \frac{1}{4} \gamma^2 h_p \delta\theta[t] + \kappa h_p \delta\theta[t] - \end{aligned}$$

$$\begin{aligned}
& \mathcal{L} \kappa h_p \delta \theta[t] + \gamma \kappa h_p \delta \theta[t] - \frac{1}{2} \mathcal{L} \gamma \kappa h_p \delta \theta[t] + \frac{1}{4} \gamma^2 \kappa h_p \delta \theta[t] - w \delta x[t] \delta \theta[t] + \\
& w \mathcal{L} \kappa \delta x[t] \delta \theta[t] - h_p \delta y[t] \delta \theta[t] - \gamma h_p \delta y[t] \delta \theta[t] - 2 \kappa h_p \delta y[t] \delta \theta[t] + \\
& \mathcal{L} \kappa h_p \delta y[t] \delta \theta[t] - \gamma \kappa h_p \delta y[t] \delta \theta[t] + h_p \delta y[t]^2 \delta \theta[t] + \kappa h_p \delta y[t]^2 \delta \theta[t] + w h_p \delta \theta[t]^2 - \\
& w \mathcal{L} \kappa h_p \delta \theta[t]^2 + w^2 \delta x[t] \delta \theta[t]^2 + w^2 \kappa \delta x[t] \delta \theta[t]^2 - w^2 h_p \delta \theta[t]^3 - w^2 \kappa h_p \delta \theta[t]^3 \}, \\
& \left\{ -\frac{\gamma}{2} - \frac{\gamma^2}{2} - \frac{\gamma^3}{8} + \kappa - \mathcal{L} \kappa + \frac{3 \gamma \kappa}{2} - \mathcal{L} \gamma \kappa + \frac{3 \gamma^2 \kappa}{4} - \frac{1}{4} \mathcal{L} \gamma^2 \kappa + \frac{\gamma^3 \kappa}{8} - \delta y[t] + \frac{1}{4} \gamma^2 \delta y[t] - \right. \\
& 3 \kappa \delta y[t] + 2 \mathcal{L} \kappa \delta y[t] - 3 \gamma \kappa \delta y[t] + \mathcal{L} \gamma \kappa \delta y[t] - \frac{3}{4} \gamma^2 \kappa \delta y[t] + 2 \delta y[t]^2 + \\
& \frac{1}{2} \gamma \delta y[t]^2 + 3 \kappa \delta y[t]^2 - \mathcal{L} \kappa \delta y[t]^2 + \frac{3}{2} \gamma \kappa \delta y[t]^2 - \delta y[t]^3 - \kappa \delta y[t]^3 + w \delta \theta[t] + \\
& \frac{1}{2} w \gamma \delta \theta[t] - w \mathcal{L} \kappa \delta \theta[t] - \frac{1}{2} w \mathcal{L} \gamma \kappa \delta \theta[t] + \frac{1}{2} \gamma w_p \delta \theta[t] + \frac{1}{4} \gamma^2 w_p \delta \theta[t] - \kappa w_p \delta \theta[t] + \\
& \mathcal{L} \kappa w_p \delta \theta[t] - \gamma \kappa w_p \delta \theta[t] + \frac{1}{2} \mathcal{L} \gamma \kappa w_p \delta \theta[t] - \frac{1}{4} \gamma^2 \kappa w_p \delta \theta[t] - w \delta y[t] \delta \theta[t] + \\
& w \mathcal{L} \kappa \delta y[t] \delta \theta[t] - w_p \delta y[t] \delta \theta[t] - \gamma w_p \delta y[t] \delta \theta[t] + 2 \kappa w_p \delta y[t] \delta \theta[t] - \\
& \mathcal{L} \kappa w_p \delta y[t] \delta \theta[t] + \gamma \kappa w_p \delta y[t] \delta \theta[t] + w_p \delta y[t]^2 \delta \theta[t] - \kappa w_p \delta y[t]^2 \delta \theta[t] - \\
& w^2 \delta \theta[t]^2 + \frac{1}{2} w^2 \gamma \delta \theta[t]^2 - w^2 \kappa \delta \theta[t]^2 - \frac{1}{2} w^2 \gamma \kappa \delta \theta[t]^2 + w w_p \delta \theta[t]^2 + \\
& w \mathcal{L} \kappa w_p \delta \theta[t]^2 + w^2 \delta y[t] \delta \theta[t]^2 + w^2 \kappa \delta y[t] \delta \theta[t]^2 - w^2 w_p \delta \theta[t]^3 + w^2 \kappa w_p \delta \theta[t]^3 \}, \\
& \left\{ -\frac{1}{2} \alpha \gamma w_p - \frac{1}{2} \alpha \gamma^2 w_p - \frac{1}{8} \alpha \gamma^3 w_p + \alpha \kappa w_p - \mathcal{L} \alpha \kappa w_p + \frac{3}{2} \alpha \gamma \kappa w_p - \mathcal{L} \alpha \gamma \kappa w_p + \frac{3}{4} \alpha \gamma^2 \kappa w_p - \right. \\
& \frac{1}{4} \mathcal{L} \alpha \gamma^2 \kappa w_p + \frac{1}{8} \alpha \gamma^3 \kappa w_p + \frac{1}{2} \alpha \gamma h_p \delta x[t] + \frac{1}{4} \alpha \gamma^2 h_p \delta x[t] + \alpha \kappa h_p \delta x[t] - \\
& \mathcal{L} \alpha \kappa h_p \delta x[t] + \alpha \gamma \kappa h_p \delta x[t] - \frac{1}{2} \mathcal{L} \alpha \gamma \kappa h_p \delta x[t] + \frac{1}{4} \alpha \gamma^2 \kappa h_p \delta x[t] + \alpha w_p \delta y[t] + \\
& 2 \alpha \gamma w_p \delta y[t] + \frac{3}{4} \alpha \gamma^2 w_p \delta y[t] - 3 \alpha \kappa w_p \delta y[t] + 2 \mathcal{L} \alpha \kappa w_p \delta y[t] - 3 \alpha \gamma \kappa w_p \delta y[t] + \\
& \mathcal{L} \alpha \gamma \kappa w_p \delta y[t] - \frac{3}{4} \alpha \gamma^2 \kappa w_p \delta y[t] - \alpha h_p \delta x[t] \delta y[t] - \alpha \gamma h_p \delta x[t] \delta y[t] - \\
& 2 \alpha \kappa h_p \delta x[t] \delta y[t] + \mathcal{L} \alpha \kappa h_p \delta x[t] \delta y[t] - \alpha \gamma \kappa h_p \delta x[t] \delta y[t] - 2 \alpha w_p \delta y[t]^2 - \\
& \frac{3}{2} \alpha \gamma w_p \delta y[t]^2 + 3 \alpha \kappa w_p \delta y[t]^2 - \mathcal{L} \alpha \kappa w_p \delta y[t]^2 + \frac{3}{2} \alpha \gamma \kappa w_p \delta y[t]^2 + \alpha h_p \delta x[t] \delta y[t]^2 + \\
& \alpha \kappa h_p \delta x[t] \delta y[t]^2 + \alpha w_p \delta y[t]^3 - \alpha \kappa w_p \delta y[t]^3 - \frac{1}{2} \alpha \gamma h_p \delta \theta[t] - \frac{1}{2} \alpha \gamma^2 h_p \delta \theta[t] - \\
& \frac{1}{8} \alpha \gamma^3 h_p \delta \theta[t] - \alpha \kappa h_p \delta \theta[t] + \mathcal{L} \alpha \kappa h_p \delta \theta[t] - \frac{3}{2} \alpha \gamma \kappa h_p \delta \theta[t] + \mathcal{L} \alpha \gamma \kappa h_p \delta \theta[t] - \\
& \frac{3}{4} \alpha \gamma^2 \kappa h_p \delta \theta[t] + \frac{1}{4} \mathcal{L} \alpha \gamma^2 \kappa h_p \delta \theta[t] - \frac{1}{8} \alpha \gamma^3 \kappa h_p \delta \theta[t] - \frac{1}{2} \alpha \gamma h_p^2 \delta \theta[t] - \\
& \frac{1}{4} \alpha \gamma^2 h_p^2 \delta \theta[t] - \alpha \kappa h_p^2 \delta \theta[t] + \mathcal{L} \alpha \kappa h_p^2 \delta \theta[t] - \alpha \gamma \kappa h_p^2 \delta \theta[t] + \frac{1}{2} \mathcal{L} \alpha \gamma \kappa h_p^2 \delta \theta[t] - \\
& \frac{1}{4} \alpha \gamma^2 \kappa h_p^2 \delta \theta[t] - w \alpha w_p \delta \theta[t] - \frac{1}{2} w \alpha \gamma w_p \delta \theta[t] - w \mathcal{L} \alpha \kappa w_p \delta \theta[t] - \frac{1}{2} w \mathcal{L} \alpha \gamma \kappa w_p \delta \theta[t] - \\
& \frac{1}{2} \alpha \gamma w_p^2 \delta \theta[t] - \frac{1}{4} \alpha \gamma^2 w_p^2 \delta \theta[t] - \alpha \kappa w_p^2 \delta \theta[t] + \mathcal{L} \alpha \kappa w_p^2 \delta \theta[t] - \alpha \gamma \kappa w_p^2 \delta \theta[t] + \\
& \frac{1}{2} \mathcal{L} \alpha \gamma \kappa w_p^2 \delta \theta[t] - \frac{1}{4} \alpha \gamma^2 \kappa w_p^2 \delta \theta[t] + w \alpha h_p \delta x[t] \delta \theta[t] - w \mathcal{L} \alpha \kappa h_p \delta x[t] \delta \theta[t] - \\
& \frac{1}{2} \alpha \gamma w_p \delta x[t] \delta \theta[t] - \frac{1}{4} \alpha \gamma^2 w_p \delta x[t] \delta \theta[t] + \alpha \kappa w_p \delta x[t] \delta \theta[t] - \mathcal{L} \alpha \kappa w_p \delta x[t] \delta \theta[t] +
\end{aligned}$$

$$\begin{aligned}
& \alpha \gamma \kappa w_p \delta x[t] \delta \theta[t] - \frac{1}{2} \mathcal{L} \alpha \gamma \kappa w_p \delta x[t] \delta \theta[t] + \frac{1}{4} \alpha \gamma^2 \kappa w_p \delta x[t] \delta \theta[t] + \\
& \alpha h_p \delta y[t] \delta \theta[t] + 2 \alpha \gamma h_p \delta y[t] \delta \theta[t] + \frac{3}{4} \alpha \gamma^2 h_p \delta y[t] \delta \theta[t] + 3 \alpha \kappa h_p \delta y[t] \delta \theta[t] - \\
& 2 \mathcal{L} \alpha \kappa h_p \delta y[t] \delta \theta[t] + 3 \alpha \gamma \kappa h_p \delta y[t] \delta \theta[t] - \mathcal{L} \alpha \gamma \kappa h_p \delta y[t] \delta \theta[t] + \\
& \frac{3}{4} \alpha \gamma^2 \kappa h_p \delta y[t] \delta \theta[t] + \alpha h_p^2 \delta y[t] \delta \theta[t] + \alpha \gamma h_p^2 \delta y[t] \delta \theta[t] + 2 \alpha \kappa h_p^2 \delta y[t] \delta \theta[t] - \\
& \mathcal{L} \alpha \kappa h_p^2 \delta y[t] \delta \theta[t] + \alpha \gamma \kappa h_p^2 \delta y[t] \delta \theta[t] + w \alpha w_p \delta y[t] \delta \theta[t] + w \mathcal{L} \alpha \kappa w_p \delta y[t] \delta \theta[t] + \\
& \alpha w_p^2 \delta y[t] \delta \theta[t] + \alpha \gamma w_p^2 \delta y[t] \delta \theta[t] + 2 \alpha \kappa w_p^2 \delta y[t] \delta \theta[t] - \mathcal{L} \alpha \kappa w_p^2 \delta y[t] \delta \theta[t] + \\
& \alpha \gamma \kappa w_p^2 \delta y[t] \delta \theta[t] + \alpha w_p \delta x[t] \delta y[t] \delta \theta[t] + \alpha \gamma w_p \delta x[t] \delta y[t] \delta \theta[t] - \\
& 2 \alpha \kappa w_p \delta x[t] \delta y[t] \delta \theta[t] + \mathcal{L} \alpha \kappa w_p \delta x[t] \delta y[t] \delta \theta[t] - \alpha \gamma \kappa w_p \delta x[t] \delta y[t] \delta \theta[t] - \\
& 2 \alpha h_p \delta y[t]^2 \delta \theta[t] - \frac{3}{2} \alpha \gamma h_p \delta y[t]^2 \delta \theta[t] - 3 \alpha \kappa h_p \delta y[t]^2 \delta \theta[t] + \mathcal{L} \alpha \kappa h_p \delta y[t]^2 \delta \theta[t] - \\
& \frac{3}{2} \alpha \gamma \kappa h_p \delta y[t]^2 \delta \theta[t] - \alpha h_p^2 \delta y[t]^2 \delta \theta[t] - \alpha \kappa h_p^2 \delta y[t]^2 \delta \theta[t] - \alpha w_p^2 \delta y[t]^2 \delta \theta[t] - \\
& \alpha \kappa w_p^2 \delta y[t]^2 \delta \theta[t] - \alpha w_p \delta x[t] \delta y[t]^2 \delta \theta[t] + \alpha \kappa w_p \delta x[t] \delta y[t]^2 \delta \theta[t] + \\
& \alpha h_p \delta y[t]^3 \delta \theta[t] + \alpha \kappa h_p \delta y[t]^3 \delta \theta[t] - w \alpha h_p \delta \theta[t]^2 - \frac{1}{2} w \alpha \gamma h_p \delta \theta[t]^2 + \\
& w \mathcal{L} \alpha \kappa h_p \delta \theta[t]^2 + \frac{1}{2} w \mathcal{L} \alpha \gamma \kappa h_p \delta \theta[t]^2 - w \alpha h_p^2 \delta \theta[t]^2 + w \mathcal{L} \alpha \kappa h_p^2 \delta \theta[t]^2 + w^2 \alpha w_p \delta \theta[t]^2 + \\
& \frac{1}{2} w^2 \alpha \gamma w_p \delta \theta[t]^2 - w^2 \alpha \kappa w_p \delta \theta[t]^2 - \frac{1}{2} w^2 \alpha \gamma \kappa w_p \delta \theta[t]^2 - w \alpha w_p^2 \delta \theta[t]^2 + w \mathcal{L} \alpha \kappa w_p^2 \delta \theta[t]^2 - \\
& w^2 \alpha h_p \delta x[t] \delta \theta[t]^2 - w^2 \alpha \kappa h_p \delta x[t] \delta \theta[t]^2 - w \alpha w_p \delta x[t] \delta \theta[t]^2 - w \mathcal{L} \alpha \kappa w_p \delta x[t] \delta \theta[t]^2 + \\
& w \alpha h_p \delta y[t] \delta \theta[t]^2 - w \mathcal{L} \alpha \kappa h_p \delta y[t] \delta \theta[t]^2 - w^2 \alpha w_p \delta y[t] \delta \theta[t]^2 + w^2 \alpha \kappa w_p \delta y[t] \delta \theta[t]^2 + \\
& w^2 \alpha h_p \delta \theta[t]^3 + \frac{1}{2} w^2 \alpha \gamma h_p \delta \theta[t]^3 + w^2 \alpha \kappa h_p \delta \theta[t]^3 + \frac{1}{2} w^2 \alpha \gamma \kappa h_p \delta \theta[t]^3 + \\
& w^2 \alpha h_p^2 \delta \theta[t]^3 + w^2 \alpha \kappa h_p^2 \delta \theta[t]^3 + w^2 \alpha w_p^2 \delta \theta[t]^3 + w^2 \alpha \kappa w_p^2 \delta \theta[t]^3 + w^2 \alpha w_p \delta x[t] \delta \theta[t]^3 - \\
& w^2 \alpha \kappa w_p \delta x[t] \delta \theta[t]^3 - w^2 \alpha h_p \delta y[t] \delta \theta[t]^3 - w^2 \alpha \kappa h_p \delta y[t] \delta \theta[t]^3 \}
\end{aligned}$$

(*EOMLinearized[[2]]-EOM[[2]]//Simplify//TraditionalForm*)

(*EOMrephrase[[2]]-EOM[[2]]//Simplify//TraditionalForm*)

Out[403]//TraditionalForm=

$$\left(-\sqrt{(\sin(\theta_p(t)) h_p + \cos(\theta_p(t)) l_p + x_1(t) - x_p(t))^2 + (\cos(\theta_p(t)) h_p - \sin(\theta_p(t)) l_p - y_1(t) + y_p(t))^2} \right.$$

$$\left. \alpha \left((l_p (\cos(\theta_p(t)) (y_1(t) - y_p(t)) - \sin(\theta_p(t)) (x_1(t) - x_p(t))) + h_p (\cos(\theta_p(t)) (x_1(t) - x_p(t)) + \sin(\theta_p(t)) (y_1(t) - y_p(t)))) \left(1 - \frac{1}{\sqrt{(\sin(\theta_p(t)) h_p + \cos(\theta_p(t)) l_p + x_1(t) - x_p(t))^2 + (\cos(\theta_p(t)) h_p - \sin(\theta_p(t)) l_p - y_1(t) + y_p(t))^2}} \right) \right) \right)$$