

$\Rightarrow$  Time Complexity (Time consumed by a program) to execute entirely

↳ Relationship between Input and running time

ex:-

```
main() {  
    Syso("Hello"); // 1  
    Syso("Hi"); // 1  
}
```

Operations = 2

Time Complexity =  $O(2)$   
 $\approx O(1)$  constant

ex:-

```
main() { int n = scn.nextInt();  
    for( int i=0; i<n; i++ ) {  
        Syso("Hi");  
    }  
}
```

Operation =  $n$

Time Complexity  $\approx O(n)$

"n" is the input from user

$O$  = capital  $O$  notation  
worst case scenario

## → Types of operations

- ↳ linear equation
- ↳ quadratic equation
- ↳ cubic equation
- ↳ Logarithmic equation
- ↳ constant equation

| input | output operation |
|-------|------------------|
| $n$   | $n$              |
| $n$   | $n^2$            |
| $n$   | $n^3$            |
| $n$   | $\log(n)$        |
| $n$   | 1                |

Ex 1 :-

```
public static void main() {  
    Scanner scn = new Scanner(System.in);  
    int n = scn.nextInt();  
    for (int i=0 ; i<n ; i++) {  
        System.out.println("Hello");  
    }  
}
```

output operations

input :-       $n = 1 \longrightarrow 1$   
 $n = 10 \longrightarrow 10$   
 $n = 90 \longrightarrow 90$   
 $n = 10000 \longrightarrow 10000$

input  $\propto n$

$\hookrightarrow O(n)$

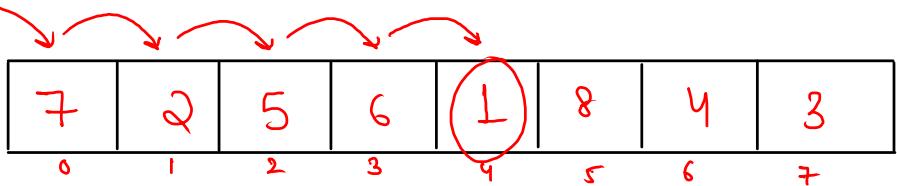
linear  
equation

## $\Rightarrow$ Complexity (Time) :-

- 1) Best case :- when least no. of operations has to be done
- 2) average case :- when average no. of operations has to be done
- 3) worst case :- when most no. of operations has to be done

Ques

You have an array and you have to find '1' in it.



```
int n=8;  
for( int i=0; i<n; i++ ) {  
    if( arr[i] == 1 ) {  
        return;  
    }  
}
```

Time Comp. =  $O(n)$   
where 'n' is size of array

operation = 8 (worst case)

operation = 1 (best case)

operations = 5 (average case)

Ex 1:-

```

public static void main() {
    Scanner scn = new Scanner(System.in);
    int n = scn.nextInt();
    for (int i = 0; i < n; i++) {
        for (int j = 0; j < n; j++) {
            System.out.println("Hi");
        }
    }
}

```

$$n=3 \quad \left. \begin{array}{l} i=0, j=0 \\ j=1 \\ j=2 \end{array} \right\} 3$$

$$\left. \begin{array}{l} i=1, j=0 \\ j=1 \\ j=2 \end{array} \right\} 3$$

$$\left. \begin{array}{l} i=2, j=0 \\ j=1 \\ j=2 \end{array} \right\} 3$$

Input      output ope.

$$\underline{n=5} \rightarrow 25$$

$$n=6 \rightarrow 36$$

$$n=10 \rightarrow 100$$

Input  $\propto n^2$

$\hookrightarrow O(n^2)$

Quadratic equation

Ex 2 :-

```
public static void main() {  
    Scanner scn = new Scanner(System.in);  
    int n = scn.nextInt();  
    int m = scn.nextInt();  
    for (int i = 0; i < n; i++) {  
        for (int j = 0; j < m; j++) {  
            System.out.print("Hi");  
        }  
    }  
}
```

$$\text{Operations} = n * m$$

$$n = 2, m = 3 \rightarrow O/P = 6$$

Input  $\propto n * m$

$O(n * m)$

Ex:-

main() {

Scanner scn = new Scanner();

int n = scn.nextInt();

int m = " " " ;

for (int i=0; i<n; i++) {

System.out.println("Hi1"); //3

}

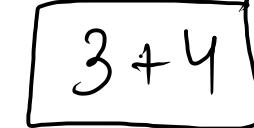
for (int j=0; j<m; j++) {

System.out.println("Hi2"); //4

}

n = 3

m = 4

operation :-  


Time Compl. :-

$\Rightarrow O(n+m)$

e.g.,  $n = 2$

$m = 2000000$

operation = 200002

$\approx O(m)$        $m \ggg n$

$\approx O(n)$        $n \ggg m$

Note:- whenever we have multiple values in addition then we ignore all the smaller values and only the largest one will be considered

Time complexity :-  $O(n+m+a+b)$

Case :-

$$a = 7$$

$$b = 2$$

$$n = 6$$

$$m = 10$$

$$\cong O(m)$$

Compare

$$\frac{\underline{\underline{O(n)}}}{\underline{\underline{O(n^2)}}} < \frac{\underline{\underline{O(n^2)}}}{\underline{\underline{O(n^3)}}}$$

$$n = 1$$

$$1$$

$$1$$

$$1$$

$$n = 2$$

$$2$$

$$4$$

$$8$$

$$n = 3$$

$$3$$

$$9$$

$$27$$

:

:

:

$$n = 10^5$$

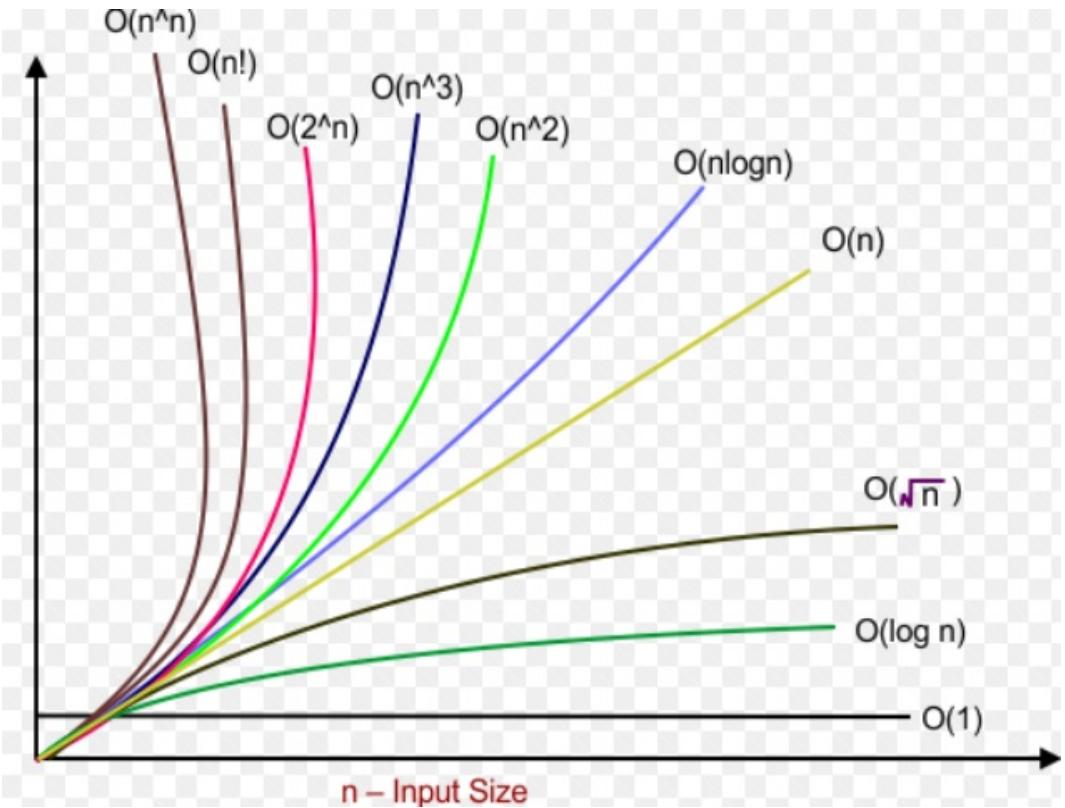
$$10^5$$

1 sec

$$10^{10}$$

$$10^{15}$$

10 min



↙  $O(1)$  *10msec* constant fastest

↙  $O(\log(n))$  logarithmic

↙  $O(\sqrt{n})$

↙  $O(n)$  linear

↙  $O(n \log(n))$

↙  $O(n^2)$  quadratic

↙  $O(n^3)$  cubic

↙  $O(2^n)$

↙  $O(n!)$

↙  $O(n^n)$  *1 year* slowest ↓

Ex:- for( int i=0 ; i<n ; i+=2 ) {  
    y  
    System.out.println(y);  
}

$$\text{operations} = n/2$$

$$\begin{aligned} \text{T.C.} &= O(n/2) \\ &\approx O(n) \end{aligned}$$

Ex:-

$$\left. \begin{aligned} n*2 &= O(n) \\ n^2+2 &= O(n^2) \\ n-2 &= O(n) \\ n/2 &= O(n) \end{aligned} \right\}$$

for ( int i=0 ; i<n ; i+=2 ) {  
    y = n/2  
    System.out.println(y);  
}

$$y = 5n^2 + 2n$$

$$O(n^2)$$

$$\text{Op: } 2*n + 5 = O(n)$$

$$\text{Op: } 7*n^2 + n/2 + 27 = O(n^2)$$