

# ~~Long pressed~~

```
public static boolean longPressed(String str, String tar) {  
    int i = 0;  
    int j = 0;  
    while (j < tar.length()) {  
        if (i < str.length() && str.charAt(i) == tar.charAt(j)) {  
            i++;  
        } else if (j == 0 || tar.charAt(j) != tar.charAt(j - 1)) {  
            return false;  
        }  
        j++;  
    }  
  
    return i == str.length();  
}
```

↓  
int      ↓  
int

traverse  
checking the sequence

i i i i i  
“ a l e x a b c ” i

“ a a l e e x ” x

True / False ✓

$\Rightarrow$  Binary Search      T.C =  $O(\log N)$

↳ it is a searching algorithm.

↳ it can be applied only on sorted series

Note:- if in question, given series is sorted  
and it is expecting better T.C than  $O(N)$   
means we binary search

series (sorted)

len = n

0	1	2	3	4	5	6	7	8	9	10	11	12	13
1	2	3	4	5	6	7	8	9	10	11	12	13	14

target = 10

find idx of target

ans = 10

↑↑  
sir  
↑

$si = 0, mid = n - 1;$

$\text{int } mid = (si + ei) / 2;$

$$mid = (9 + 9) / 2 = 9$$

- a)  $\{ arr[mid] == \text{target}, \text{return mid}$
- b)  $\{ arr[mid] > \text{target}, ei = mid - 1;$
- c)  $\{ arr[mid] < \text{target}, si = mid + 1;$

```

public static void main(String[] args) {
    Scanner scn = new Scanner(System.in);
    int n = scn.nextInt();
    int[] arr = new int[n];
    for (int i = 0; i < n; i++) {
        arr[i] = scn.nextInt();
    }
    int target = scn.nextInt();

    binarySearch(arr, n, target);
}

public static void binarySearch(int[] arr, int n, int target) {
    int si = 0;
    int ei = n - 1;
    while (si <= ei) {
        int mid = (si + ei) / 2; ←
        if (arr[mid] == target) {
            System.out.println(mid); →
            return;
        } else if (arr[mid] > target) {
            ei = mid - 1; ←
        } else {
            si = mid + 1; ←
        }
    }
    System.out.println(-1);
}

```

Note:-

This scenario is  
only for unique  
values  
and not repeated  
ones.

Note:-

with each operation,  
we are discarding  
half of the array  
means we are decreasing  
our range to half

~~Series~~ (sorted)

len = 14

0	1	2	3	4	5	6	7	8	9	10	11	12	13
1	2	3	4	5	6	7	8	9	10	11	12	13	14

↑  
ci  
↑  
si  
↑  
mid

target = 2

ans = 1

$$\text{mid} = (0+13)/2 = 6$$

$$= (0+5)/2 = 2$$

$$= (0+1)/2 = 0$$

$$= (1+1)/2 = 1$$

length = n

$$n + \frac{n}{2} + \frac{n}{4} + \frac{n}{8} + \frac{n}{16} + \dots + 1 = \log(n)$$

(Taylor series)

Proof of T.C = log(N)

replace n with  $n/2$

$$T(n) = 1 + T\left(\frac{n}{2}\right) \quad \left[\frac{n}{2^1}\right]$$

$$T\left(\frac{n}{2}\right) = 1 + T\left(\frac{n}{4}\right) \quad \left[\frac{n}{2^2}\right]$$

$$T\left(\frac{n}{4}\right) = 1 + T\left(\frac{n}{8}\right) \quad \left[\frac{n}{2^3}\right]$$

$$T\left(\frac{n}{2^{k-1}}\right) = 1 + T\left(\frac{n}{2^k}\right) \quad \left[\frac{n}{2^k}\right]$$

$$T(n) = (\underbrace{1+1+1+\dots+1}_{K \text{ times}}) + T\left(\frac{n}{2^k}\right)$$

$$\Rightarrow \frac{n}{2^k} = 1$$

$$\Rightarrow n = 2^k$$

$$\Rightarrow \text{take } \log_2 \text{ both side}$$

$$\Rightarrow \log_2(n) = \log_2(2^k)$$

$$\log_2(n) = K \log_2(2)$$

$$\log(n) = K * 1 = K$$

binary search complexity is  $O(k)$

$\Rightarrow O(\log N)$

# Find Square Root

$$\underline{n = 25}, \quad \underline{\text{ans} = 5}$$

$$\underline{n = 37}, \quad \underline{\text{ans} = 6}$$

example

$$\underline{\underline{n = 12}},$$

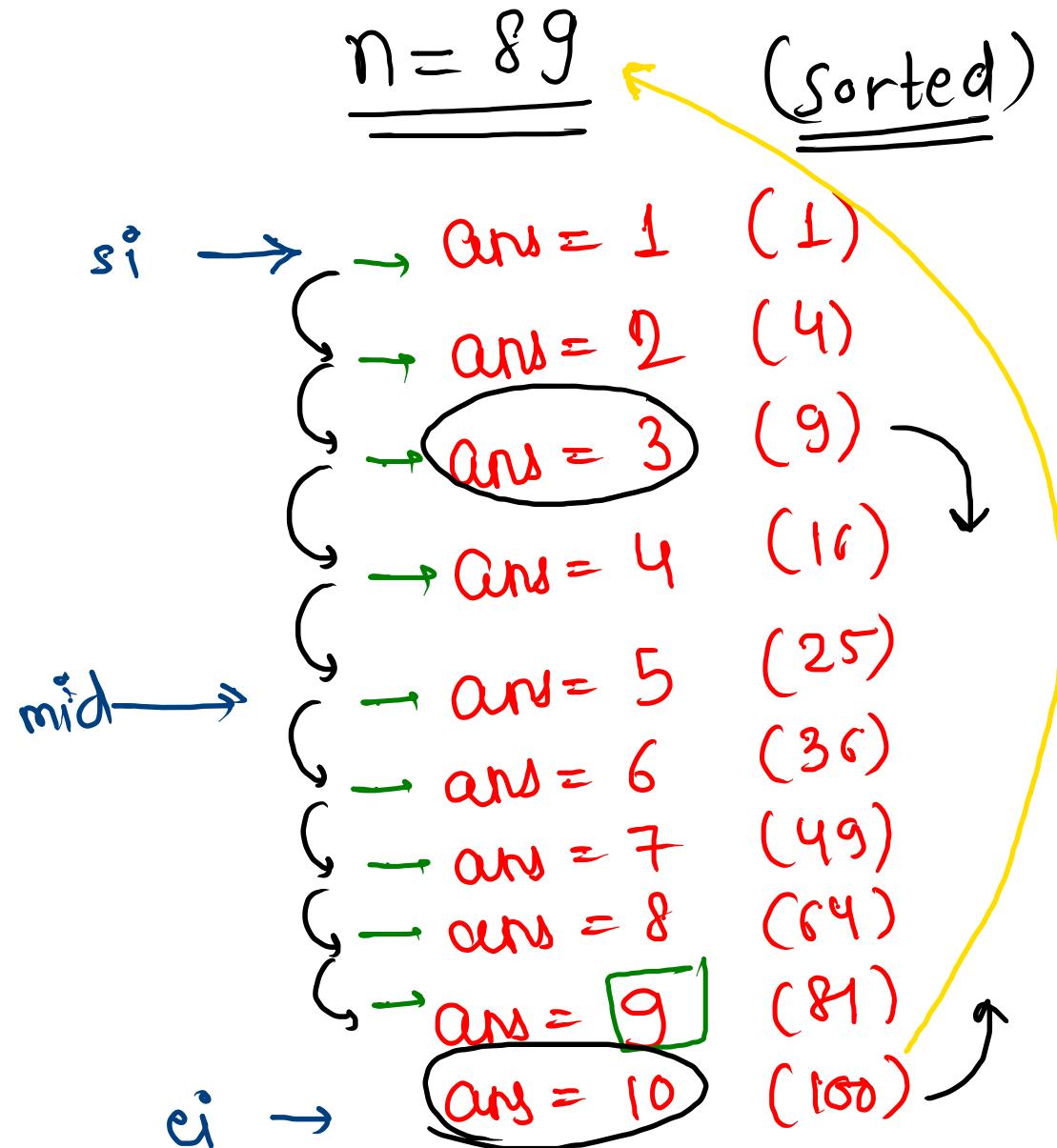
Square

$$\text{ans} = 1, \quad 1 \times 1 = 1$$

$$= 2, \quad 2 \times 2 = 4$$

$$= 3, \quad 3 \times 3 = 9$$

$$= 4, \quad 4 \times 4 = 16$$



assuming

$$\underline{n = 89}$$

(magic of B.S is you can traverse in  
imaginary range as well)

$$\underline{s_i = 1}, \underline{e_i = n}$$

int mid = (s<sup>i</sup> + e<sup>i</sup>) / 2 ;

if (mid \* mid > n) {

    e<sup>i</sup> = mid - 1;

} else {

    s<sup>i</sup> = mid + 1;

}

val = arr[mid] X

val = mid ✓

{  
S.C = O(1)  
T.C = O(logN)

Code

```
public static void main(String[] args) {  
    Scanner scn = new Scanner(System.in);  
    int n = scn.nextInt();  
  
    binarySearch(n);  
}  
  
public static void binarySearch(int n) {  
    int si = 1;  
    int ei = n;  
    while ( si <= ei ) {  
        int mid = (si + ei) / 2;  
        if ( mid * mid <= n ) {  
            a [ si = mid + 1; ]  
        } else {  
            b [ ei = mid - 1; ]  
        }  
    }  
    System.out.println(ei);  
}
```

$n = 225$

$si = 1, ei = 225, mid = 113$

$si = 1, ei = 112, mid = 56$

$si = 1, ei = 55, mid = 28$

$si = 1, ei = 27, mid = 14$

$si = 15, ei = 27, mid = 21$

$si = 15, ei = 20, mid = 17$

$si = 15, ei = 16, mid = 15$

$si = 16, ei = 16, mid = 16$

$si = 16, \underline{ei = 15}, mid = 15$