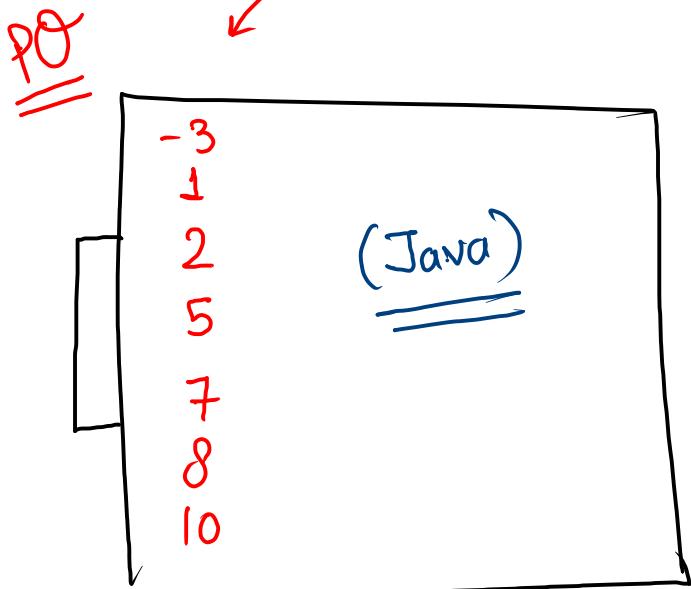


Priority Queue (any element that will be placed in PQ will always be in sorted order)

Heap

2, 7, 1, -3, 10, 5, 8



Note:- { also dynamic nature
no indexing present

Note:- (default)

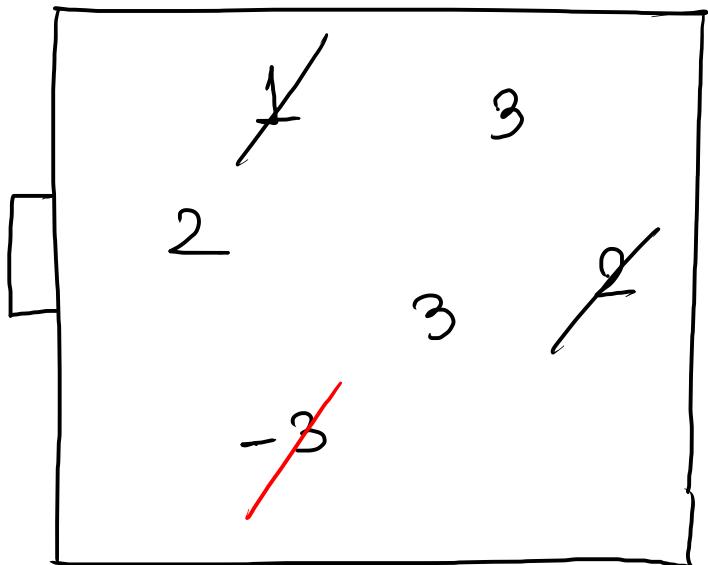
↳ by default, PQ will sort elements in increasing order (Java)

↳ by default, PQ will sort elements in decreasing order (C++)

Note:- we can only access the top element

PO

add $\rightarrow 2, 3, -3, 3, 1, 2$



Note:- In PO, repetition
is allowed

Remove $\rightarrow -3, 1, 2, 2$

Syntax

PriorityQueue<DataType> pq = new PriorityQueue<>();

Inbuilt functions

Imp

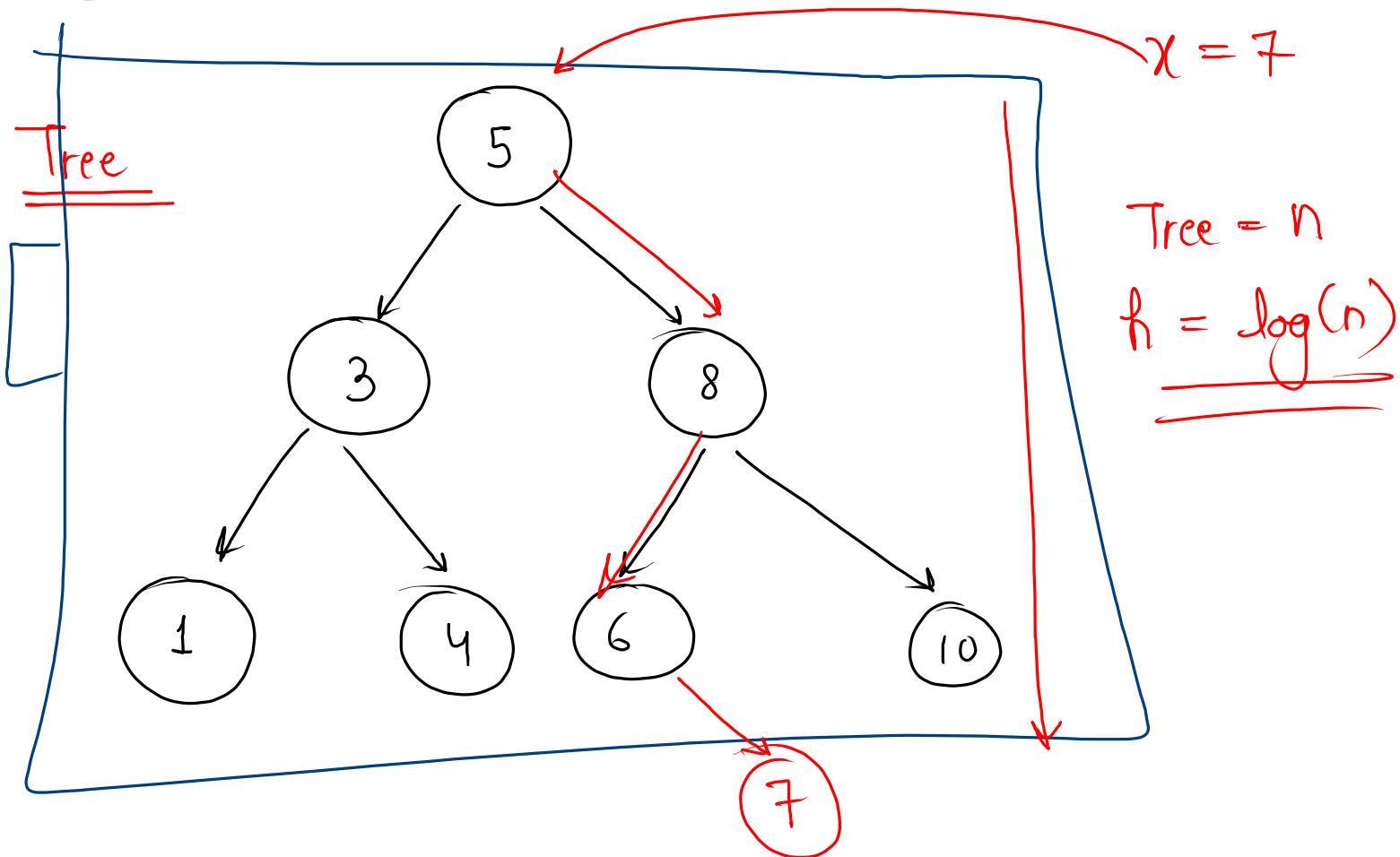
Note :- every inbuilt fn T.C = $\log(n)$

where n is size
of pq

- pq.add(x) // add element in PQ
- pq.remove() }
- pq.pull()
- pq.peek() // return top element of PQ

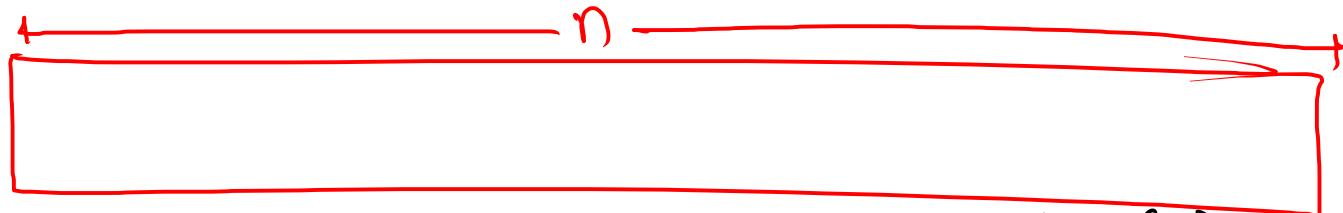
pq.size() / pq.isEmpty() } evergreen

Behind the Scene of PO (Ignore)



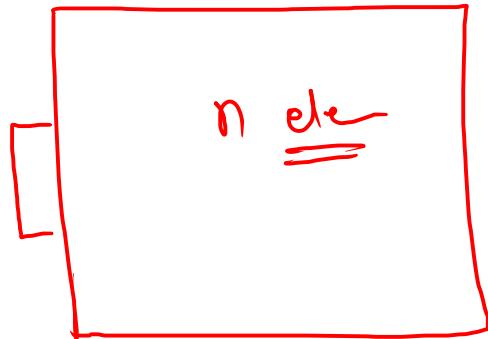
Note:- every question that can be solved using PO, can also be solved using sorting & vice versa

arr :-



Sort :- $n \log(n)$

PO



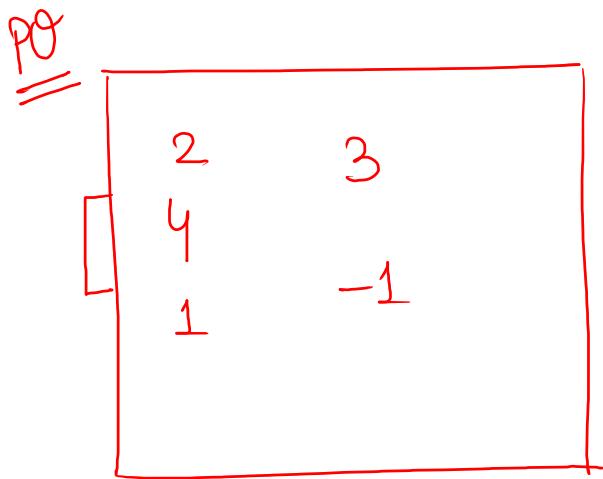
$$\begin{aligned} T.C &= n \log(n) + n \log(n) \\ &= 2n \log(n) \\ &\approx \underline{\underline{n \log(n)}} \end{aligned}$$

Jmp :- Lambda Function

```
Arrays.sort (arr, (a, b) → {  
    return a - b;  
});
```

```
PriorityQueue<Integer> pq = new PriorityQueue<>((a, b) → {  
    return a - b; // first  
});  
                                b - a; // first
```

priority queue basics



$t = 5$

4 → 4
2 → 2
1 → 1
3 → 1
-1 → -1

A vertical list of five pairs, each consisting of a number and an arrow pointing to its right. The numbers are 4, 2, 1, 3, and -1. The first four pairs (4, 2, 1, 3) have arrows pointing to the number 1, indicating they are mapped to the same value. The last pair (-1) has an arrow pointing to itself, indicating it is mapped to itself.

Code

$$T.C = O(n \log(n))$$
$$S.C = O(n)$$

```
public static void main(String[] args) {
    Scanner scn = new Scanner(System.in);
    int t = scn.nextInt();
    int[] arr = new int[t];
    for (int i = 0; i < t; i++) {
        arr[i] = scn.nextInt();
    }
    solve(arr, t);
}

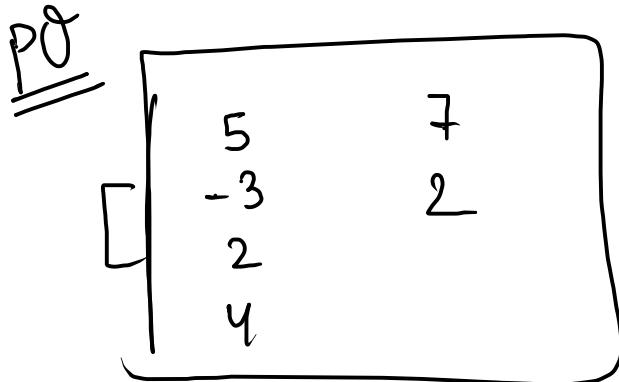
public static void solve(int[] arr, int n) {
    PriorityQueue<Integer> pq = new PriorityQueue<>();
    for (int i : arr) {
        pq.add( i );
        System.out.println( pq.peek() );
    }
}
```

Maximum Product of Two Elements in an Array

$$\text{arr} = [5, -3, 2, 4, 7, -2]$$

$$\text{val} = \underbrace{(arr[i] - 1) * (arr[j] - 1)}_{\text{max}} \quad \}$$

$$\text{Val} = (7 - 1) * (5 - 1) = 24$$



Note :-

PO with ascending order :- min heap
nature

PO with descending order :- max heap
nature

Code

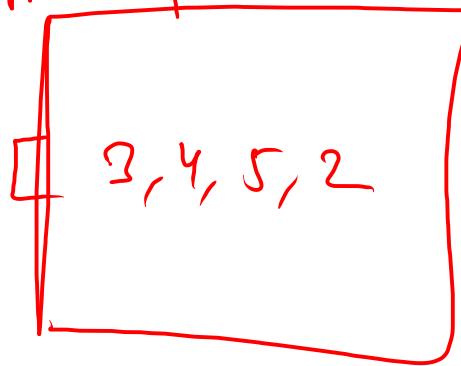
```
public static void main(String[] args) {
    Scanner scn = new Scanner(System.in);
    int t = scn.nextInt();
    int[] arr = new int[t];
    for (int i = 0; i < t; i++) {
        arr[i] = scn.nextInt();
    }
    System.out.println(solve(arr, t));
}

public static int solve(int[] arr, int n) {
    // max heap
    PriorityQueue<Integer> pq = new PriorityQueue<>((a, b) -> {
        return b - a;
    });
    for (int i : arr) {
        pq.add(i);
    }

    int num1 = pq.poll();
    int num2 = pq.poll();
    return (num1 - 1) * (num2 - 1);
}
```

3, 4, 5, 2

max heap



$$\begin{aligned} T.C &= O(n \log n + 2 \log n) \\ &= O((n+2) \log(n)) \\ &= \underline{\underline{O(n \log(n))}} \end{aligned}$$

Lambda fn never effects the T.C

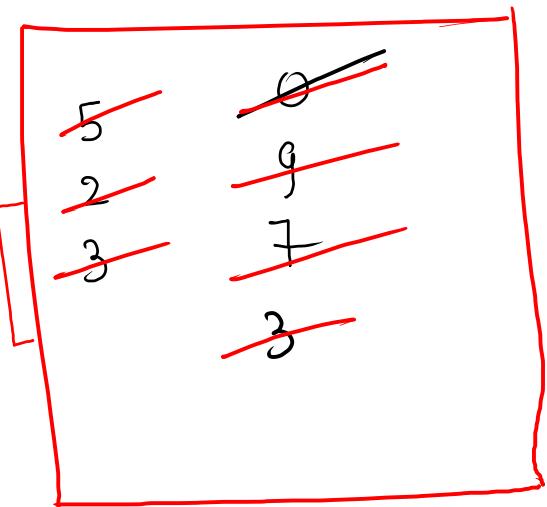
minimum digits

arr = [~~5~~, ~~2~~, ~~3~~, ~~0~~, ~~9~~, ~~7~~, 3]

num1 = 037

num2 = 259

~~min
heap~~



num1 = num1 * 10 + peek

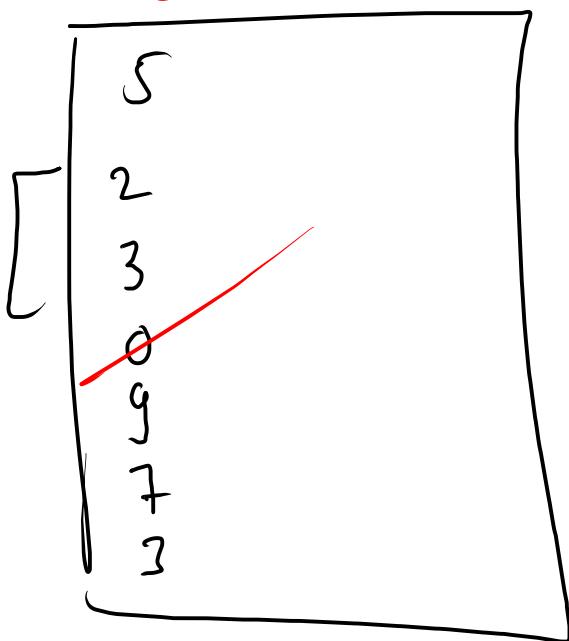
num2 = num2 * 10 + peek

num1 = 0359

num2 = 237

$\text{arr} = [\underset{0}{5}, \underset{1}{2}, \underset{2}{3}, \underset{3}{0}, \underset{4}{9}, \underset{5}{7}, \underset{6}{3}]$

Size=7



$\text{pq.size} = \text{odd}$

$\text{num1} =$

$\text{num2} =$

$\curvearrowright \text{pq.size} = \text{even}$

Code

T.C = O(n log(n)), S.C = O(n)

```
public static long minimumSum(int[] arr, int n) {  
    PriorityQueue<Integer> pq = new PriorityQueue<>();  
    for (int i : arr) {  
        pq.add(i);  
    }  
  
    long num1 = 0;  
    long num2 = 0;  
    while ( pq.size() > 0 ) {  
        int rem = pq.poll();  
        if ( pq.size() % 2 == 0 ) {  
            num1 = num1 * 10 + rem;  
        } else {  
            num2 = num2 * 10 + rem;  
        }  
    }  
  
    return num1 + num2;  
}
```