

# Recursion Concepts & Qns ...

Motivation (भाषण) ...



“

Whenever you feel  
like quitting, remember

- why you started ←
- what will success feel like ←
- Mom, Dad, your happiness

”

#codestorywithMIK



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Instagram } → code story with MIK

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Qualcomm

Company :- Google amazon

and many more companies ✓✓



## 51. N-Queens

Hard

Topics

Companies

The **n-queens** puzzle is the problem of placing  $n$  queens on an  $n \times n$  chessboard such that no two queens attack each other.

Given an integer  $n$ , return all distinct solutions to the **n-queens** puzzle. You may return the answer in any order.

Each solution contains a distinct board configuration of the n-queens' placement, where 'Q' and '.' both indicate a queen and an empty space, respectively.

Example :-  $n = 4$

	0	1	2	3
0	.	Q	.	.
1	.	.	.	Q
2	Q	.	.	.
3	.	.	Q	.

{  
 ". Q . .",  
 ". . . Q",  
 "Q . . .",  
 ". . Q ."  
 }

# Thought Process

$n=4$

4Q

	0	1	2	3
0	.	.	Q	.
1	Q	.	.	.
2	.	.	.	Q
3	.	Q	.	.

row

row+1

row+2

row+3

"...Q...",  
 "...Q...",  
 "Q...",  
 "...Q...",  
 "...Q...",  
 "...Q...",  
 "...Q...",  
 "...Q..."

Story Points :-

$n=3$

(.) Board  $\rightarrow$

$$f \left( \begin{array}{ccc} " & & " \\ . & . & . \\ " & & " \\ . & . & . \\ " & & " \end{array} \right) = f \left( \begin{array}{c} \text{wavy line} \\ " \dots " \\ \text{---} \\ \text{X} \end{array} , \begin{array}{c} \text{wavy line} \\ " \dots " \\ \text{---} \\ \text{X} \end{array} , \begin{array}{c} \text{wavy line} \\ " \dots " \\ \text{---} \\ \text{X} \end{array} \right)$$

```
vector<string> board(n, string(n, '.'));
```

↑                      ↑  
string                  each thing

c) `Solve(Board, 0)` ; // row = 0

(.) Place Queen in column & explore.  
"Recursion Magic"

```
Solve (Board, row) {
    if (row >= n) {
        result.push-back (Board); return;
    }
    for (col = 0; col < n; col++) {
        if (isValid(Board, row, col)) {
```

Do

Explore

undo

$\Rightarrow$  Solve (Board, row+1); // Trust

$\Rightarrow$  Board[row][col] = '.' ;

isValid (Board, row, col)

(2, 0)  
(3, 1)

	0	1	2	3	4
0	Q	.	.	.	• •
1	.	.	Q	•	.
2	•	.	•	.	Q
3	□	Q	.	.	.
4	.	.	.	.	.

Colso

← row

row = 3, col = 0

r → [3] [1]<sup>c</sup>

(3, 1)  
(2, 2)  
(1, 3)  
(0, 4)

↙ upward

[row-1][c]  
(row-2)[c]  
⋮  
[0][c]

↙ upwardDiag Right

↙ upwardDiag left

Time Complexity :- ....

void solve(vector<string>& board, int row) {  
 if (row >= N) {  
 // ...  
 }  
}

✓	Q	X	X	X	✓	
X	X	X	X		X	
X			X			
			X	X		
			X		X	

$N-3$   
 $\times$   
 $N-5$   
 $\times$

```

result.push_back(board);
return;
}

for(int col = 0; col < N; col++) {
    if(isValid(board, row, col)) {
        board[row][col] = 'Q';
        solve(board, row+1);
        board[row][col] = '.';
    }
}

```

$\leftarrow n$   
 $\leftarrow n$   
 $\leftarrow T(n-1)$

$$T(n) = n * (n + T(n-1))$$

$$T(n) = n * T(n-1) + n^2$$

$$= n * \left[ (n-1) * T(n-2) + (n-1)^2 \right] + n^2$$

$$= n * (n-1) * T(n-2) + n * (n-1)^2 + n^2$$

$$= n * (n-1) * (n-2) * \dots + \dots$$

$$T.C \approx O(N!)$$

Space Complexity:

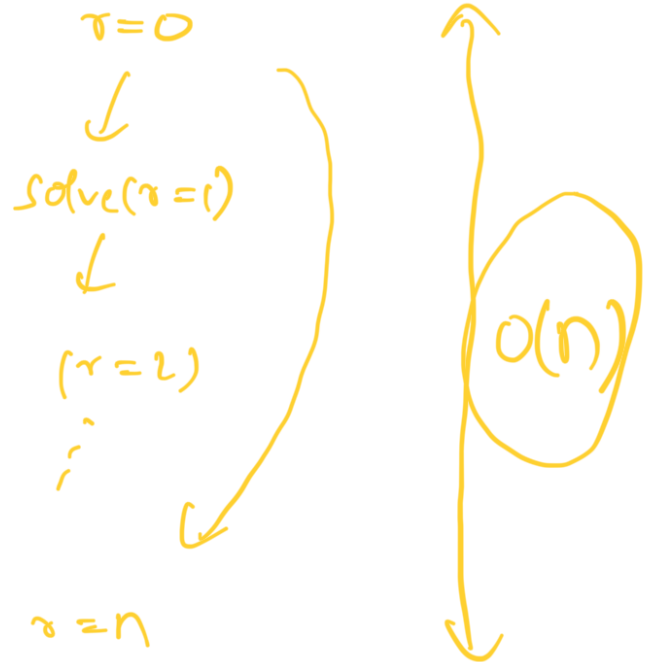
# Space Complexity :-

Extra auxiliary space. =  $O(1)$

System Stack =  $O(n)$ .

```
void solve(vector<string>& board, int row) {  
    if (row >= N) {  
        result.push_back(board);  
        return;  
    }  
  
    for(int col = 0; col < N; col++) {  
        if(isValid(board, row, col)) {  
            board[row][col] = 'Q';  
            solve(board, row+1);  
            board[row][col] = '.';  
        }  
    }  
}
```

row = n



## Approach - 2

what was the problem in 1<sup>st</sup> Approach:-



```

void solve(vector<string>& board, int row) {
    if(row >= N) {
        result.push_back(board);
        return;
    }

    for(int col = 0; col < N; col++) {
        if(isValid(board, row, col)) {
            board[row][col] = 'Q';
            solve(board, row+1);
            board[row][col] = '.';
        }
    }
}

```

$(i, j)$

	0	1	2	3	5
0			Q		
1					Q
2					
3					
4					

Columns → { 2, 5 }

Diagonals → { 2, }

Anti-di → { }

SP:  $O(n)$

$$2-1=1$$

$$(2,1) = 2+1=3$$

$$(1,2) = 1+2=3$$

$$(0,3) = 0+3=3$$

$$(2,1) = 2-1=1$$

$$(1,0) = 1-0=1$$

$(i-j)$  Constant → Anti-diag.

$(i+j)$  Const → Diagon.

Columns.insert(col);

diag.insert(row+col); // [row][col]

anti.insert(row-col);

Solve (board, row+1);

col. en (col).