

## Experiment Name: To determine the RC time constant in an RC circuit

### Theory: Charging a capacitor

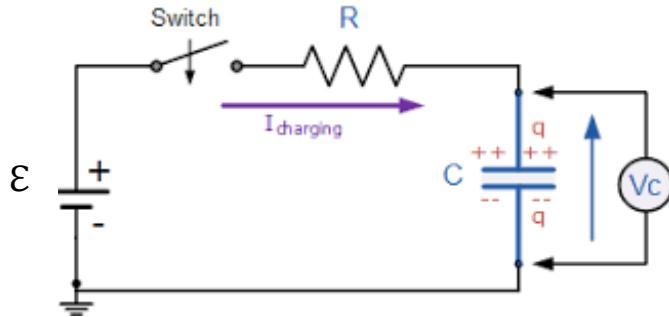


Fig 1 : Charging a capacitor

Kirchhoff's loop theorem:

$$\mathcal{E} - iR - \frac{q}{C} = 0$$

$$\mathcal{E} = iR + \frac{q}{C} \quad [i \text{ & } q = \text{two variables}, i = \frac{dq}{dt}]$$

$$\mathcal{E} = R \frac{dq}{dt} + \frac{q}{C}$$

$$q = C\mathcal{E}(1 - e^{\frac{-t}{RC}})$$

$$CV_c = C\mathcal{E}(1 - e^{\frac{-t}{RC}}) \quad [q = CV_c]$$

$$V_c = \mathcal{E}(1 - e^{\frac{-t}{RC}})$$

$$\frac{V_c}{\mathcal{E}} = 1 - e^{\frac{-t}{RC}}$$

$$e^{\frac{-t}{RC}} = 1 - \frac{V_c}{\mathcal{E}}$$

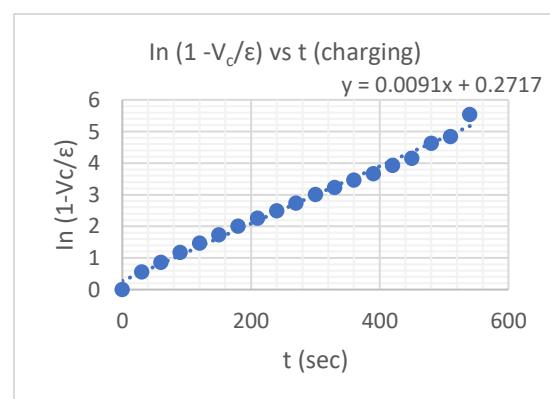
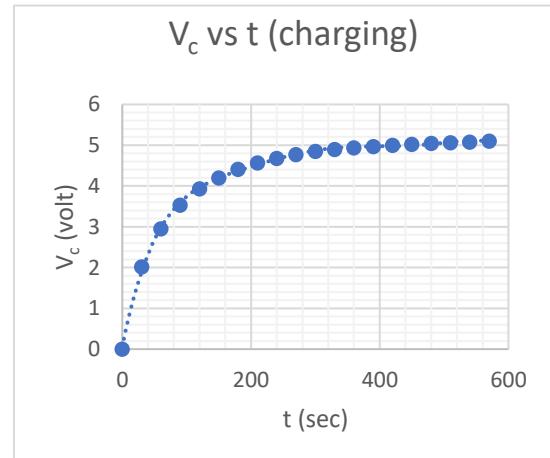
$$\ln(1 - \frac{V_c}{\mathcal{E}}) = \ln(e^{\frac{-t}{RC}})$$

$$\ln(1 - \frac{V_c}{\mathcal{E}}) = -\frac{t}{RC}$$

$$\ln(1 - \frac{V_c}{\mathcal{E}}) = (-\frac{1}{RC})t$$

From the graph,  $y = mx + b$

$$\text{Slope, } m = (-\frac{1}{RC})$$



## Discharging a capacitor:

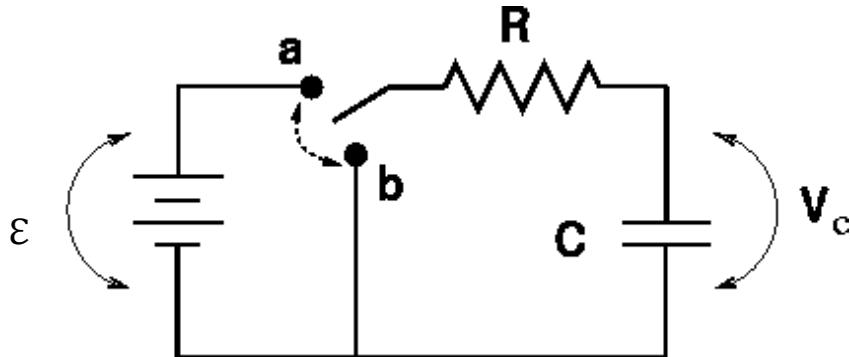


Fig 2: Discharging a capacitor

Kirchhoff's loop theorem:

$$-iR - \frac{q}{c} = 0$$

$$-(iR + \frac{q}{c}) = 0$$

$$R \frac{dq}{dt} + \frac{q}{c} = 0 \quad [ i = \frac{dq}{dt} ]$$

$$q = C\mathcal{E}e^{\frac{-t}{RC}}$$

$$CV_c = C\mathcal{E}e^{\frac{-t}{RC}} \quad [ q = CV_c ]$$

$$V_c = \mathcal{E}e^{\frac{-t}{RC}}$$

$$\frac{V_c}{\mathcal{E}} = e^{\frac{-t}{RC}}$$

$$\ln\left(\frac{V_c}{\mathcal{E}}\right) = \ln(e^{\frac{-t}{RC}})$$

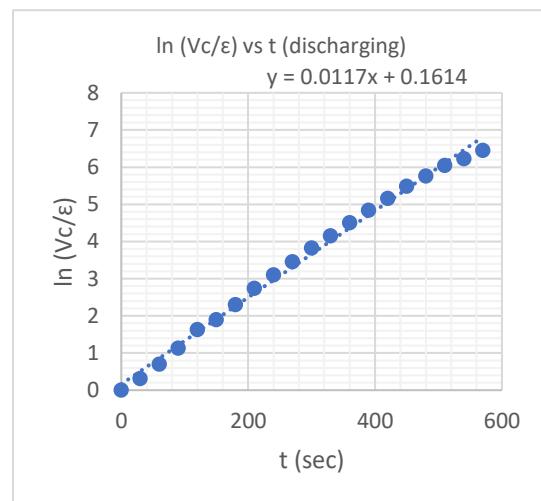
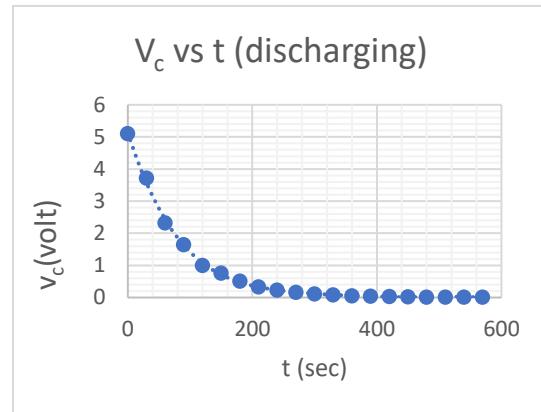
$$\ln\left(\frac{V_c}{\mathcal{E}}\right) = -\frac{t}{RC}$$

$$\ln\left(\frac{V_c}{\mathcal{E}}\right) = \left(-\frac{1}{RC}\right)t$$

From the graph,  $y = mx + b$

$$\text{Slope, } m = \left(-\frac{1}{RC}\right)$$

**Apparatus:** Resistor, capacitor, power supply, voltmeter and stop watch



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Data Table: Charging & Discharging of an RC circuit

Maximum potential difference ( $\mathcal{E}$ ) =

Time (s)	Charging capacitor		Discharging capacitor	
	$V_c$ (volt)	$\ln(1 - \frac{V_c}{\mathcal{E}})$	$V_c$ (volt)	$\ln(\frac{V_c}{\mathcal{E}})$
0				
30				
60				
90				
120				
150				
180				
210				
240				
270				
300				
330				
360				
390				
420				
450				
480				
510				
540				
570				
600				
630				
660				
690				

## **Calculation: Charging a capacitor**

**Theoretically:**

**Time constant,  $\tau = RC =$**

**Experimentally:**

From the graph: Slope,  $m = -\frac{1}{\tau}$

$$\tau = -\frac{1}{m}$$

$$\text{Error of } \tau = \frac{\tau_{th} - \tau_{ex}}{\tau_{th}} \times 100\%$$

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