

⑧ $\mathbb{R}^2 \not\stackrel{omeo}{=} \mathbb{R} \times [0, \infty)$

assurdo: $\mathbb{R}^2 \stackrel{omeo}{=} \mathbb{R} \times [0, \infty) \Rightarrow \mathbb{R}^2 \setminus \{0\} \cong (\mathbb{R} \times [0, \infty)) \setminus \{(0,0)\}$ omeomorfi

$\Rightarrow \mathbb{R}^2 \setminus \{0\} \simeq (\mathbb{R} \times [0, \infty)) \setminus \{(0,0)\}$ omotopi

$\Rightarrow \pi_1(\mathbb{R}^2 \setminus \{0\}) \cong \pi_1((\mathbb{R} \times [0, \infty)) \setminus \{(0,0)\})$ isomorfi

na $\begin{cases} \pi_1(\mathbb{R}^2 \setminus \{0\}) \cong \mathbb{Z} \\ \pi_1((\mathbb{R} \times [0, \infty)) \setminus \{(0,0)\}) \cong \{e\} \end{cases} \xRightarrow{\text{assurdo}} \Rightarrow \mathbb{R}^2 \not\stackrel{omeo}{=} \mathbb{R} \times [0, \infty)$

