

$$W = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 4 & 6 \\ 3 & 6 & 9 \end{bmatrix}$$

3.1: Only one independent column ( $C_1$ ).

$\therefore$  Only one independent direction of information.

3.2:  $\text{Rank}(W) = 1$  [1 linearly independent row/column]

3.3:  $A = C \cdot R$   $\hookrightarrow A \rightarrow m \times n$ , rank  $\rightarrow r$

$$\left. \begin{array}{l} C \rightarrow m \times r \rightarrow 3 \times 1 \\ R \rightarrow r \times n \rightarrow 1 \times 3 \end{array} \right\} \therefore$$

Here,  $m = n = 3$   $\rightarrow r = 1$