

$$W = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 4 & 6 \\ 3 & 6 & 9 \end{bmatrix}$$

[3.1]: Only one independent column (C_1).

\therefore Only one independent direction of information.

[3.2]: $\text{Rank}(W) = 1$ [1 linearly independent row/column]

[3.3]: $A = C \cdot R \quad \hookrightarrow \quad A \rightarrow m \times n, \text{ rank} \rightarrow r$

$$\left. \begin{array}{l} C \rightarrow m \times r \rightarrow 3 \times 1 \\ R \rightarrow r \times n \rightarrow 1 \times 3 \end{array} \right\} \quad \therefore$$

Here, $m = n = 3$

$r = 1$