

$$= nh \left[ y_0 + \frac{n}{2} \Delta y_0 + \frac{n(2n-3)}{12} \Delta^3 y_0 \dots \right] \dots \dots \dots (4.1)$$

This is general formula is known as Newton-cote's Formula.

#### 4.5.2 Trapezoidal Formula (composite)( $n = 1$ )

Putting  $n = 1$  in formula (4.1) and taking the curve through  $(x_0, y_0)$  and  $(x_1, y_1)$  as a polynomial of degree 1 so that differences of order higher than one vanish, we get,

$$\begin{aligned} \int_{x_0}^{x_0+h} f(x) dx &= h \left[ y_0 + \frac{1}{2} \Delta y_0 \right] \\ &= \frac{h}{2} [2y_0 + (y_1 - y_0)] \\ &= \frac{h}{2} [y_0 + y_1] \end{aligned}$$

Similarly, for the next interval  $(x_0-h, x_0+2h)$ , we get,

$$\int_{x_0+h}^{x_0+2h} f(x) dx = \frac{h}{2} [y_1 + y_2]$$

... ..

$$\int_{x_0+(n-1)h}^{x_0+nh} f(x) dx = \frac{h}{2} (y_{n-1} + y_n)$$

Adding the above integrals, we get;

$$\int_{x_0}^{x_0+nh} f(x) dx = \frac{h}{2} [(y_0 + y_n) + 2(y_1 + y_2 + \dots + y_{n-1})]$$

$$= \frac{h}{2} [( \text{Sum of first and last terms} ) + 2 \times ( \text{Sum of all intermediate ordinate} )]$$

which is known as composite trapezoidal rule.

#### 4.5.3 Geometrical Interpretation of Trapezoidal Formula

The area of shaded region bounded by the curve  $y = f(x)$ ,  $x$ -axis, and the lines  $x = a$  and  $x = b$  represents the trapezoidal formula for the integral given by  $\int_a^b f(x) dx = \frac{h}{2} [y_0 + y_1]$  formula. This formula replaces the area of the shaded region by the area of the trapezoid.