From Simpson's 1/3 rule, we have

$$\int_{0}^{1} \frac{\log(1+x^{2})}{1+x^{2}} dx = h/3 \left[(y_{0} + y_{10}) + 4(y_{1} + y_{3} + y_{5} + y_{7} + y_{9}) + 2(y_{2} + y_{4} + y_{6} + y_{8}) \right]$$

$$= \frac{0.1}{3} \left[(0.3278) + 4(0.0098 + 0.0790 + 0.1785 + 0.4868) + 0.3016 + 2(0.0377 + 0.1279 + 0.2260 + 0.2868) + 0.1738 \right]$$

$$= 0.173$$

4.7 WEDDLE'S RULE (n=6)

Substituting n = 6 in the Newton's Cot's formula, we have

$$\int_{x_0}^{x_0+6h} f(x)dx = h \left[6y_0 + 18\Delta y_0 + 27\Delta^2 y_0 + 24\Delta^3 y_0 + \frac{123}{10}\Delta^4 y_0 + \frac{33}{10}\Delta^5 y_0 + \frac{41}{140}\Delta^6 y_0 \right]$$

Then if we write in terms of y_i ,

$$\int_{x_0}^{x_0+6h} f(x)dx = \frac{3h}{10} [y_0 + 5y_1 + y_2 + 6y_3 + y_4 + 5y_5 + y_6]$$

Similarly, for the interval x_6 to x_{12} we have

$$\int_{x_6}^{x_0+12h} f(x)dx = \frac{3h}{10} [y_6 + 5y_7 + y_8 + 6y_9 + y_{10} + 5y_{11} + y_{12}]$$

...

Finally for x_{n-6} to x_n we have

$$\int_{x_{n-6}}^{x_n} f(x) dx = \frac{3h}{10} [y_{n-6} + 5y_{n-5} + y_{n-4} + 6y_{n-3} + y_{n-2} + 5y_{n-1} + y_n]$$