

1 # Hyperparameter Optimization with Hyperopt-Intro & Implementation

Hyperparameter Optimization is the process of identifying the best combination of hyperparameters for a machine learning model to satisfy an objective function, which is usually defined as "minimizing" the objective function for consistency.

1. Objective Function: accepts a combination of hyperparameters as input and returns the minimized error/loss.
2. Search Space: Function Arguments
3. Optimization Algorithm: Like random search and Tree of Parzen Estimators(TPE) etc.

In [1]:

```
1 pip install hyperopt
```

Collecting hyperoptNote: you may need to restart the kernel to use updated packages.

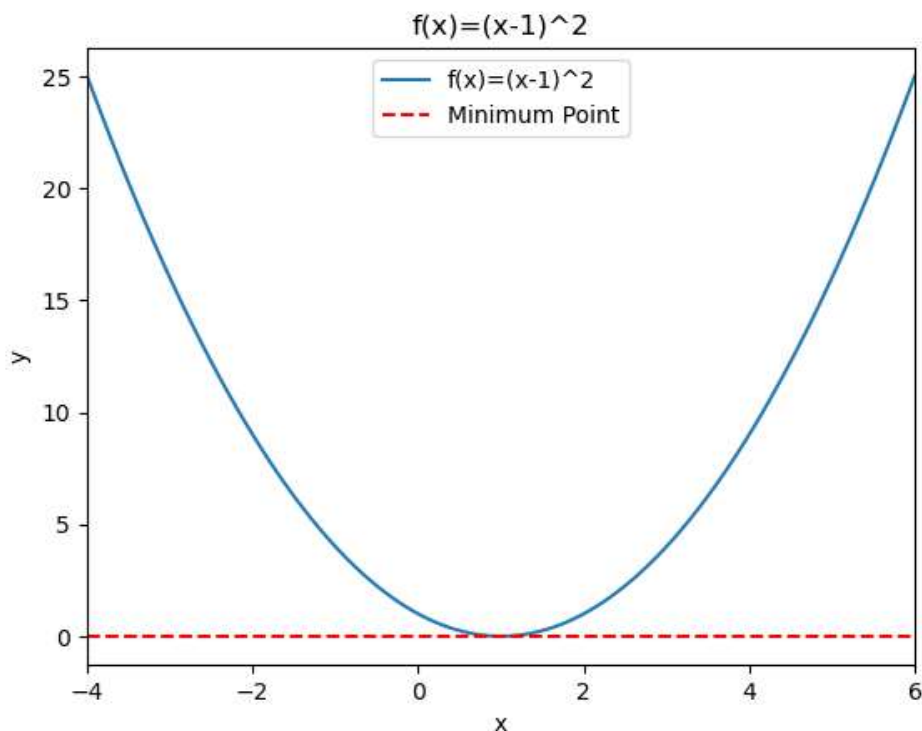
```
Downloading hyperopt-0.2.7-py2.py3-none-any.whl (1.6 MB)
----- 1.6/1.6 MB 301.4 kB/s eta 0:00:00
Requirement already satisfied: numpy in c:\users\kiran\anaconda3\lib\site-packages (from hyperopt) (1.23.5)
Requirement already satisfied: scipy in c:\users\kiran\anaconda3\lib\site-packages (from hyperopt) (1.9.1)
Requirement already satisfied: six in c:\users\kiran\anaconda3\lib\site-packages (from hyperopt) (1.16.0)
Requirement already satisfied: networkx>=2.2 in c:\users\kiran\anaconda3\lib\site-packages (from hyperopt) (2.8.4)
Requirement already satisfied: future in c:\users\kiran\anaconda3\lib\site-packages (from hyperopt) (0.18.2)
Requirement already satisfied: tqdm in c:\users\kiran\anaconda3\lib\site-packages (from hyperopt) (4.64.1)
Requirement already satisfied: cloudpickle in c:\users\kiran\anaconda3\lib\site-packages (from hyperopt) (2.0.0)
Collecting py4j (from hyperopt)
  Downloading py4j-0.10.9.7-py2.py3-none-any.whl (200 kB)
----- 200.5/200.5 kB 406.5 kB/s eta 0:00:00
Requirement already satisfied: colorama in c:\users\kiran\anaconda3\lib\site-packages (from tqdm->hyperopt) (0.4.5)
Installing collected packages: py4j, hyperopt
Successfully installed hyperopt-0.2.7 py4j-0.10.9.7
```

Simple Example

Quadratic function of $f(x)=(x-1)^2$

In [3]:

```
1 import numpy as np
2 import matplotlib.pyplot as plt
3
4 #Define the function
5 def f(x):
6     return(x-1)**2
7
8 #Generate x values from -5 to 5
9 x=np.linspace(-4,6,100)
10
11 #Calculate corresponding y values
12 y=f(x)
13
14 #Find the minimum point
15 min_point=np.min(y)
16
17 #Create the plot
18 plt.plot(x,y,label='f(x)=(x-1)^2')
19 plt.xlabel('x')
20 plt.ylabel('y')
21 plt.title('f(x)=(x-1)^2')
22
23 #Set the x-axis limits
24 plt.xlim(-4,6)
25
26 #Add horizontal dashed line at the minimum point
27 plt.axhline(y=min_point,color='red',linestyle='dashed',label='Minimum Point')
28
29 #Add a Legend
30 plt.legend()
31
32 #Display the plot
33 plt.show()
34
```



```
1 # As we can see, the minimum point happens where x=1.
```

```
1 Let`s implement this using Hyperopt and see how it works.
2 In order to do so, we will take the following steps:
3 1. import necessary libraries and packages
4 2. define the objective function and the search space
5 3. run the optimization process
6 4. print the results(i.e the optimized point that we expect to be x=1)
```

In [9]:

```
1 #1. import necessary libraries and packages
2
3 from hyperopt import hp,fmin,tpe,Trials
4
5 #2. define the objective function and the search space
6
7 def objective_function(x):
8     return (x-1)**2
9 search_space=hp.uniform('x',-2,2)
10
11 #3. run the optimization process
12
13 #Trials object to store the results
14
15 trials=Trials()
16
17 #run the optimization
18
19 best=fmin(fn=objective_function,space=search_space,algo=tpe.suggest,trials=trials,max_eval
20
21
22 #4. print the results(i.e the optimized point that we expect to be x=1)
23
24 print(best)
25
```

```
100%|████████████████████████████████████████████████████████████████████████████████| 1
00/100 [00:00<?, ?trial/s, best loss=?]
{'x': 0.9873345471340685}
```

best returns the best combination of hyperparameters that the mode was

able to find and in this case it is almost equal to x=1, as we expected.

Hyperopt implementation

We will implement two separate examples as follows.

1. A classification with Support Vector Machine

2. A regression with Random Forest Regressor

1. Support Vector Machines and Iris Data Set with two parameter that we can optimize as follows: c:
Regularization parameter, which trades off misclassification of

training examples against simplicity of the decision surface.

gamma: Kernel coefficient, which defines how much influence a single training exaple has.

The larger gamma is, the closer other examples must be to be affected.

In [11]:

```
1 from sklearn import datasets
2 from sklearn.svm import SVC
3 from sklearn.model_selection import cross_val_score
4
5 iris=datasets.load_iris()
6 X=iris.data
7 y=iris.target
8
```

Define objective function and search space

Objective function, which will train an SVM and returns the negative of the cross-validation score that is what we want to minimize. Note that we are minimizing the negative of cross-validation score to be consistent with the general goal of minimizing the objective function.

In [12]:

```
1 def objective_function(parameters):
2     clf=SVC(**parameters)
3     score=cross_val_score(clf,X,y,cv=5).mean()
4     return -score
```

Next we will define the search space, which consists of the values that our parameters of c and gamma can take. Note that we will use Hyperopt's `hp.uniform(label,low,high)`, which returns a value uniformly between low and high.

In [13]:

```
1 search_space={
2     'C':hp.uniform('C',0.1,10),
3     'gamma':hp.uniform('gamma',0.01,1)
4 }
```

Run Optimization

We will use a TPE algorithm and store the results in a trials object

In [14]:

```
1 trials=Trials()
2
3 best=fmin(fn=objective_function,space=search_space,algo=tpe.suggest, trials=trials,max_eva
4
```

100%|██| 100/100 [00:02<00:00, 45.94t
rial/s, best loss: -0.9866666666666667]

In [15]:

```
1 # Visualize Optimization
2
3 print(best)
```

```
{'C': 6.323329285556576, 'gamma': 0.12538458670925196}
```

```
1 Now we have a combination of hyperparameters that minimize the optimization function
  using Hyperopt.
2
```

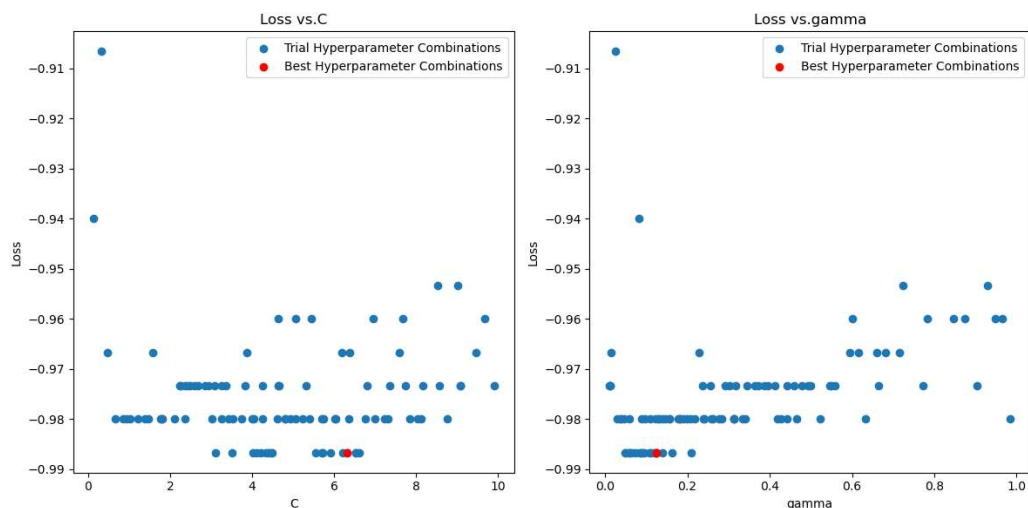
```
1 Let`s visually look at how the objective function values changes as the hyperparameters
  change.
2
3 We will start with defining a function named plot_obj_vs_hp() that accomplishes this
  visualization.
4 Make sure to look for the red dot-- that one indicates the best combination of
  hyperparameters, according to our
5 hyperparameter optimization!
```

In [23]:

```
1 import matplotlib.pyplot as plt
2
3 def plot_obj_vs_hp(trials,search_space,best):
4
5     #Extract the results
6
7     results=trials.trials
8
9     #Create a list of hyperparameters
10
11     hyperparameters=list(search_space.keys())
12
13     #Create a new figure with 2 subplots side by side
14
15     fig,axes= plt.subplots(1,2,figsize=(12, 6))
16
17     #Loop through hyperparameters and generate plots
18
19     for idx, hp in enumerate(hyperparameters):
20
21         #Extract the values of a given hyperparameter
22
23         hp_values=[res['misc']['vals'][f'{hp}'] for res in results]
24
25         #Flatten the list of values
26
27         hp_values=[item for sublist in hp_values for item in sublist]
28
29         #Extract the corresponding objective function values
30
31         objective_values=[res['result']['loss'] for res in results]
32
33         #Create the scatter plot
34
35         axes[idx].scatter(hp_values,objective_values,label='Trial Hyperparameter Combination')
36
37         #Highlight the best hyperparameters
38
39         axes[idx].scatter(best[hp],min(objective_values),color='red',label='Best Hyperparameter')
40         axes[idx].set_xlabel(f'{hp}')
41         axes[idx].set_ylabel('Loss')
42         axes[idx].set_title(f'Loss vs.{hp}')
43         axes[idx].legend(loc='upper right')
44
45     plt.tight_layout()
46     plt.show()
```

In [24]:

```
1 #Plot optimization vs hyperparameters in 2D
2 plot_obj_vs_hp(trials, search_space, best)
```



Note that since c and γ are not really related to each other, we are showing them separately versus changes of the objective function.

Since we want the objective function to be minimized, then we're looking for the furthest bottom side of the plots above and based on the results of the hyperparameter optimization, we know that what we are looking for is where $\{ 'C': 6.323329285556576, 'gamma': 0.12538458670925196 \}$, which results in an objective function loss of around -0.986 and is indicated by a red dot.

I was also curious to look at these plots in a three-dimensional manner so I created the function below to accomplish that.

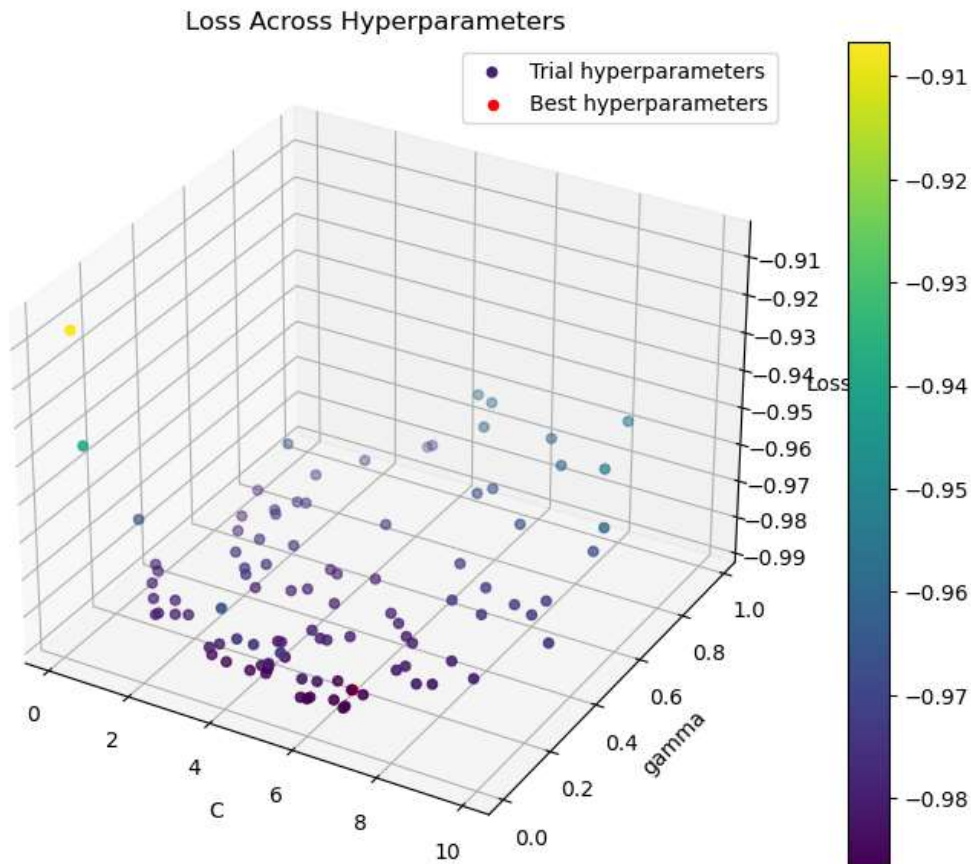
Let's look at the plot

In [32]:

```
1 from mpl_toolkits.mplot3d import Axes3D
2 import matplotlib.pyplot as plt
3
4 # define 3D plot function
5
6 def plot_obj_vs_hp_3d(trials,search_space,best):
7
8     #Extract the results
9
10    results=trials.trials
11
12    #Create a list of hyperparameters
13
14    hyperparameters=list(search_space.keys())
15
16    #Extract the values of hyperparameters
17
18    hp_values_0=[res['misc']['vals'][f'{hyperparameters[0]}'] for res in results]
19    hp_values_1=[res['misc']['vals'][f'{hyperparameters[1]}'] for res in results]
20
21    #Flatten the Lists of values
22
23    hp_values_0=[item for sublist in hp_values_0 for item in sublist]
24    hp_values_1=[item for sublist in hp_values_1 for item in sublist]
25
26    #Extract the corresponding objective function values
27
28    objective_values=[res['result']['loss'] for res in results]
29
30    #Create a new figure
31
32    fig=plt.figure(figsize=(10,7))
33
34    #Add a 3D subPlot
35
36    ax=fig.add_subplot(111,projection='3d')
37
38    #Create the scatter plot
39
40    scatter=ax.scatter(hp_values_0,hp_values_1,objective_values,c=objective_values,cmap='v
41
42    #Highlight the best hyperparameters
43
44    ax.scatter(best[hyperparameters[0]],best[hyperparameters[1]],min(objective_values),col
45
46    #Add labels using hyperparameters from search_space
47    ax.set_xlabel(hyperparameters[0])
48    ax.set_ylabel(hyperparameters[1])
49    ax.set_zlabel('Loss')
50    ax.set_title('Loss Across Hyperparameters')
51    fig.colorbar(scatter)
52    ax.legend(loc='upper right')
53
54    plt.show()
55
```


In [33]:

```
1 #plot optimization vs. hyperparameters in 3D
2
3 plot_obj_vs_hp_3d(trials,search_space,best)
```



Admittedly, this is not very easy to read but let's give it a shot. We are looking for the lowest loss, which is the darkest dots on the plot (and the red dot is almost hidden by one of the dark dots). Visually it aligns with the two-dimensional plots that we had generated before.

Random Forest and Diabetes Data Set

This example focuses on a regression model that attempts at measuring the progression of the disease, one year after baseline.

We will use a Random Forest Regressor model for this example and will optimize the objective function for two hyperparameters as follows:

1. `n_estimators`: Number of trees in the random forest
2. `max_depth`: Maximum depth of trees in the random forest

In [35]:

```
1 from sklearn import datasets
2 from sklearn.ensemble import RandomForestRegressor
3 from hyperopt import fmin,tpe,hp, Trials
4 import matplotlib.pyplot as plt
5 from mpl_toolkits.mplot3d import Axes3D
6
7 #Load Diabetes dataset
8 diabetes=datasets.load_diabetes()
9
10 X=diabetes.data
11 y=diabetes.target
12
```

In [42]:

```

1  #Define objective function
2
3  def objective_function(parameters):
4
5      #Initiate RandomForestRegressor
6
7      regressor=RandomForestRegressor(**parameters)
8
9      #Calculate the mean cross-validation score using 5 folds
10
11     score=cross_val_score(regressor,X,y,cv=5).mean()
12
13     return -score
14
15 #Define search Space
16
17 search_space={
18     'n_estimators':hp.choice('n_estimators',range(10,300)),
19     'max_depth':hp.choice('max_depth',range(1,30)),
20 }

```

Run Optimization

In [43]:

```
1 #Trials object to store the results
2
3 trials=Trials()
4
5 #Run Optimization
6
7 best=fmin(fn=objective_function,space=search_space,algo=tpe.suggest,
8           trials=trials,max_eval
```

```
100%|███████████| 100/100 [11:59<00:00, 7.19  
s/trial, best loss: -0.4395051293022144]
```

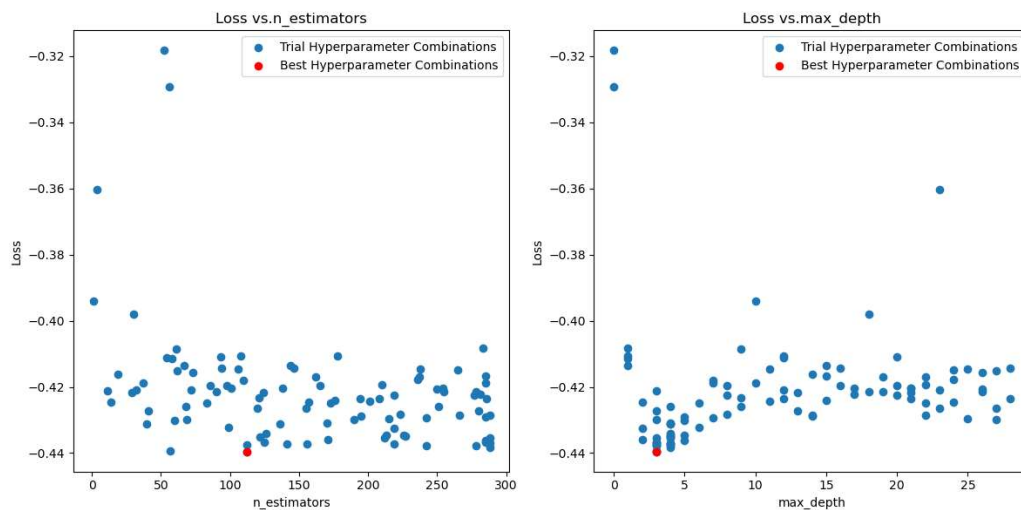
In [44]:

```
1 print(best)
```

```
{'max_depth': 3, 'n_estimators': 112}
```

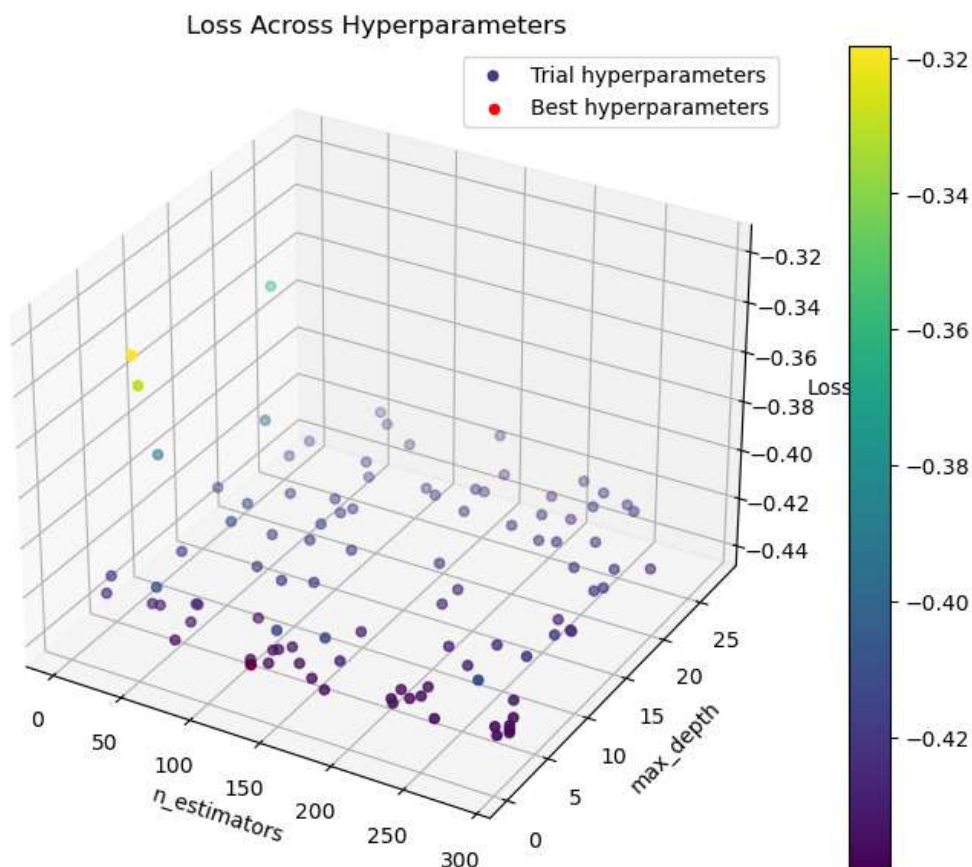
In [45]:

```
1 #plot optimization vs.hyperparameters in 2D
2
3 plot_obj_vs_hp(trials,search_space,best)
```



In [47]:

```
1 #plot optimization vs.hyperparameters in 3D
2 plot_obj_vs_hp_3d(trials,search_space,best)
```



In []:

1	
---	--