

BDA Final Notebook

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1 BigData Analytics Course Project

1.1 Project Topic: Apply ML Algorithms to Dataset

1.1.1 Aim: To recognize Handwriting using CNN + RNN with Keras and TensorFlow package

Presented by,

* Name: Surya Narayanan S

* Reg No: 121015098

* Year & Dept: 4 IT

- Dataset: <https://www.kaggle.com/landlord/handwriting-recognition>
- Dataset size: 1.3 GB
- No of Images: 3.72 Lakhs
- A CRNN (Convolutional + Recurrent Neural Network) Machine Learning Model is built to recognize and convert Handwritten Images to text using TensorFlow and Keras package in python.
- Accuracy, Support, Confusion matrix, Classification Report, Similarity Histogram are used for evaluation.

1.1.2 Where is it used ?

- To digitalize physical forms (Name, Age etc., details from physical form can be recognized and converted to text)
- Handwriting virtual Keyboard (In mobile phones, we can write in the screen using stylus or hand touch . Which is then converted to text)

```
[1]: #Basic Imports
import os
import cv2
import random
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sn
from IPython.display import display
from PIL import Image
import pylab as pl
```

```
[2]: #Tech Stack
import tensorflow as tf
from tensorflow.keras import backend as K
from tensorflow.keras.models import Model
from tensorflow.keras.layers import Input, Conv2D, MaxPooling2D, Reshape,
    ↳ Bidirectional, LSTM, Dense, Lambda, Activation, BatchNormalization, Dropout
from tensorflow.keras.optimizers import Adam
from sklearn.decomposition import PCA
from sklearn.metrics import classification_report, confusion_matrix,
    ↳ mean_squared_error
from Levenshtein import jaro_winkler
```

```
[3]: os.chdir('C:\\Users\\surya\\Documents\\Lab\\Python\\BigDataProject')

train = pd.read_csv("HandwrittenDataset/written_name_train_v2.csv")
valid = pd.read_csv("HandwrittenDataset/written_name_validation_v2.csv")

display(train.describe(include="all"))
display(train.head())
```

	FILENAME	IDENTITY
count	330961	330396
unique	330961	100539
top	TRAIN_248527.jpg	THOMAS
freq	1	1825

	FILENAME	IDENTITY
0	TRAIN_00001.jpg	BALTHAZAR
1	TRAIN_00002.jpg	SIMON
2	TRAIN_00003.jpg	BENES
3	TRAIN_00004.jpg	LA LOVE
4	TRAIN_00005.jpg	DAPHNE

```
[4]: print("Number of NaNs in train set      : ", train['IDENTITY'].isnull().sum())
print("Number of NaNs in validation set : ", valid['IDENTITY'].isnull().sum())

train.dropna(axis=0, inplace=True)
valid.dropna(axis=0, inplace=True)
```

```
Number of NaNs in train set      : 565
Number of NaNs in validation set : 78
```

```
[5]: #Sample Images
plt.figure(figsize=(15, 10))
print("Sample Images")
for i in range(6):
    ax = plt.subplot(2, 3, i+1)
    img_dir = 'HandwrittenDataset/train_v2/train/'+train.loc[i, 'FILENAME']
```

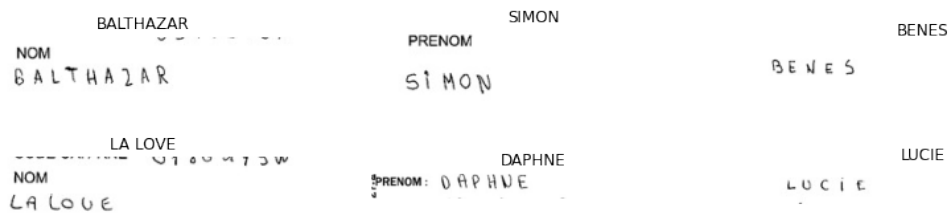
```

image = cv2.imread(img_dir, cv2.IMREAD_GRAYSCALE)
plt.imshow(image, cmap = 'gray')
plt.title(train.loc[i, 'IDENTITY'], fontsize=12)
plt.axis('off')

plt.subplots_adjust(wspace=0.2, hspace=-0.8)

```

Sample Images



```

[6]: #Remove Unreadable
unreadable = train[train['IDENTITY'] == 'UNREADABLE']
unreadable.reset_index(inplace = True, drop=True)
print("No of Unreadable Images " + str(len(unreadable)))
print("Sample Unreadable Images")
plt.figure(figsize=(15, 10))

for i in range(6):
    ax = plt.subplot(2, 3, i+1)
    img_dir = 'HandwrittenDataset/train_v2/train/'+unreadable.loc[i, 'FILENAME']
    image = cv2.imread(img_dir, cv2.IMREAD_GRAYSCALE)
    plt.imshow(image, cmap = 'gray')
    plt.title(unreadable.loc[i, 'IDENTITY'], fontsize=12)
    plt.axis('off')

plt.subplots_adjust(wspace=0.2, hspace=-0.8)
plt.show()

train = train[train['IDENTITY'] != 'UNREADABLE']
valid = valid[valid['IDENTITY'] != 'UNREADABLE']

#Convert all Characters to Upper Case

train['IDENTITY'] = train['IDENTITY'].str.upper()
valid['IDENTITY'] = valid['IDENTITY'].str.upper()

train.reset_index(inplace = True, drop=True)

```

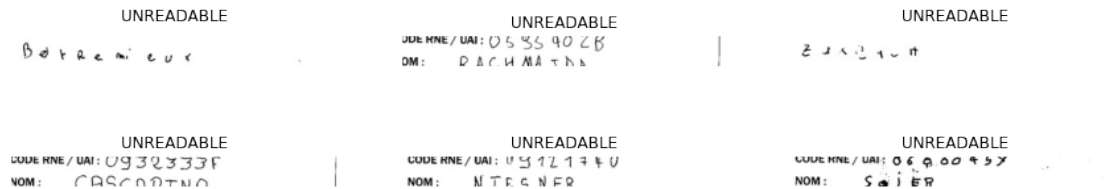
```

valid.reset_index(inplace = True, drop=True)
print("After Cleaning")
print("Length of Train Dataset ", len(train))
print("Length of Validation Dataset ", len(valid))

```

No of Unreadable Images 102

Sample Unreadable Images



After Cleaning

Length of Train Dataset 330294

Length of Validation Dataset 41280

```

[7]: #Image Preprocessing
def preprocess(img):

    #gray = cv2.cvtColor(img, cv2.COLOR_BGR2GRAY)
    ret, img = cv2.threshold(img, 0, 255, cv2.THRESH_OTSU | cv2.
    →THRESH_BINARY_INV)
    #rect_kernel = cv2.getStructuringElement(cv2.MORPH_RECT, (18, 18))
    #dilation = cv2.dilate(thresh1, rect_kernel, iterations = 1)
    #display(Image.fromarray(thresh1))
    (h, w) = img.shape
    final_img = np.ones([64, 256])*0 # blank white image

    # crop
    if w > 256:
        img = img[:, :256]

    if h > 64:
        img = img[:64, :]

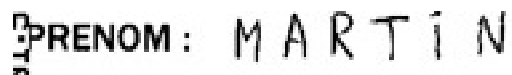
    final_img[:h, :w] = img
    final_img = final_img.astype("uint8")
    #display(Image.fromarray(final_img))
    final_img = cv2.rotate(final_img, cv2.ROTATE_90_CLOCKWISE)
    #display(Image.fromarray(final_img))
    return final_img

```

```
[8]: #Histogram of sample Image before preprocessing
file = "HandwrittenDataset/test_v2/test/TEST_0006.jpg"
#fle = "HandwrittenDataset/Hello.jpg"
#fle = "HandwrittenDataset/Chandra1.jpg"
img = cv2.imread(file, cv2.IMREAD_GRAYSCALE)
print("Image Before Pre-Processing")
display(Image.fromarray(img))
img2 = img.flatten()
plt.hist(img2)
plt.title("Histogram before Pre-Processing")
plt.xlabel("GrayScale Value")
plt.ylabel("Frequency")
plt.show()

processed = preprocess(img)
print("Image after Pre-Processing")
display(Image.fromarray(processed))
img2 = processed.flatten()
plt.hist(img2)
plt.title("Histogram after Pre-Processing")
plt.xlabel("GrayScale Value")
plt.ylabel("Frequency")
plt.show()
```

Image Before Pre-Processing



PRENOM: MARTIN

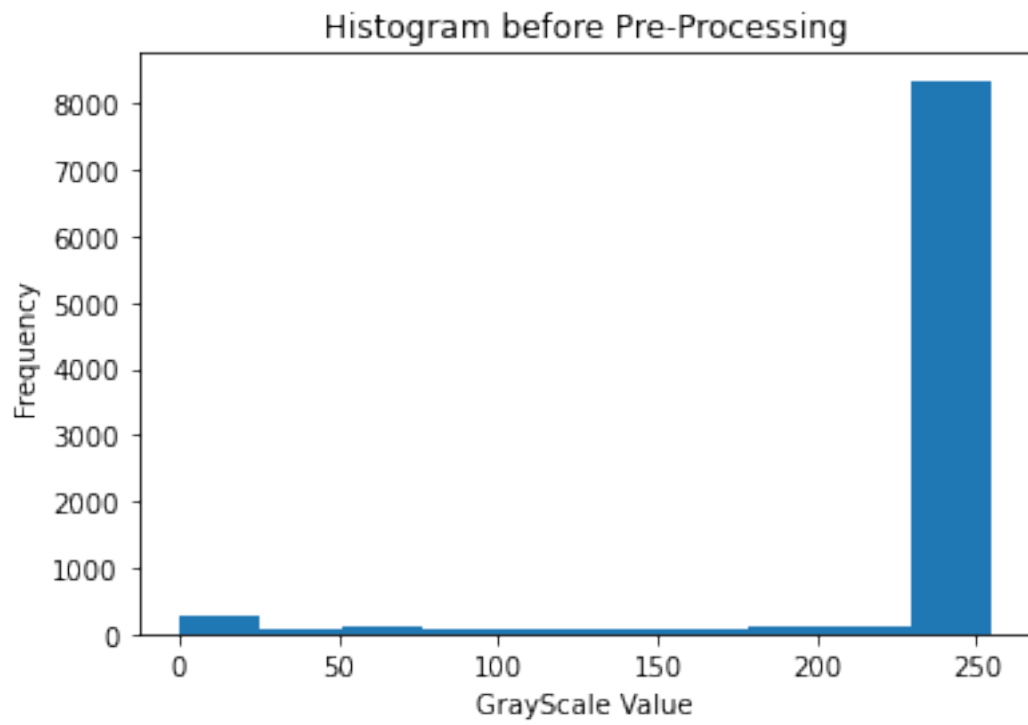
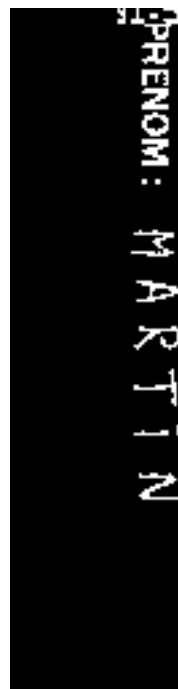
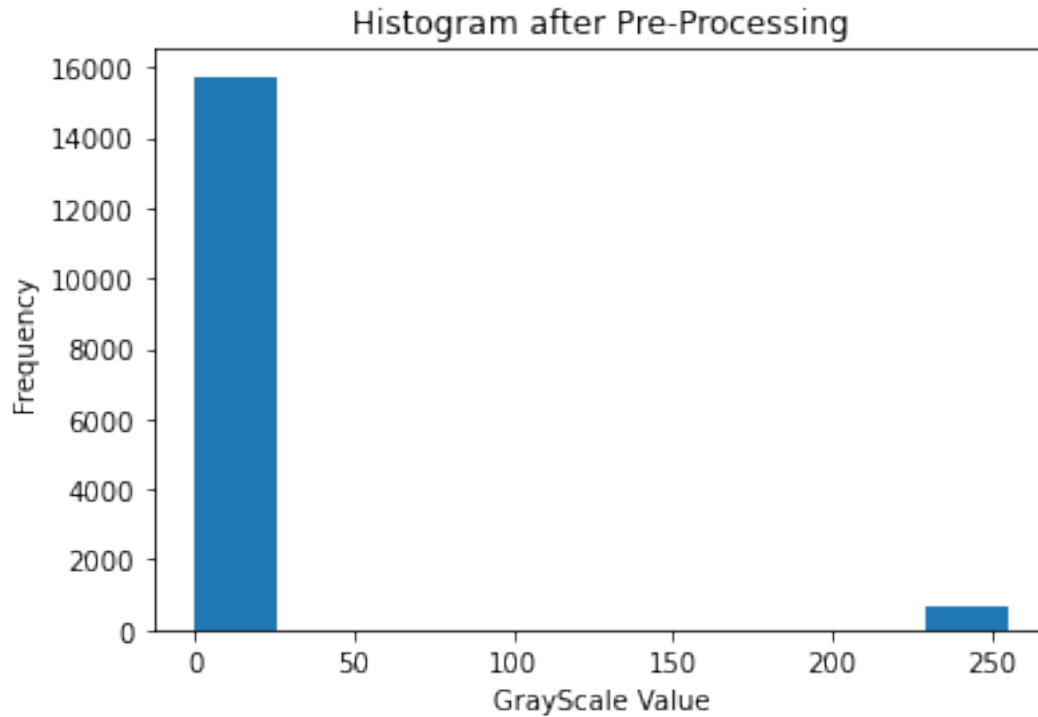


Image after Pre-Processing





```
[9]: #Read Train Images from a folder and preprocess it using OpenCV

train_size = 30000
train_x = []

for i in range(train_size):
    img_dir = 'HandwrittenDataset/train_v2/train/'+train.loc[i, 'FILENAME']
    image = cv2.imread(img_dir, cv2.IMREAD_GRAYSCALE)
    image = preprocess(image)
    image = image/255.
    train_x.append(image)
train_x = np.array(train_x).reshape(-1, 256, 64, 1)
print("Train Images Size ", train_x.shape)
```

Train Images Size (30000, 256, 64, 1)

```
[10]: #Read Validation Images from a folder and preprocess it using OpenCV

valid_x = []
valid_size= 3000
start_ind = 0
for i in range(start_ind,start_ind+valid_size):
    img_dir = 'HandwrittenDataset/validation_v2/validation/'+valid.loc[i, 'FILENAME']
```

```

    image = cv2.imread(img_dir, cv2.IMREAD_GRAYSCALE)
    image = preprocess(image)
    image = image/255.
    valid_x.append(image)
valid_x = np.array(valid_x).reshape(-1, 256, 64, 1)
print("Validation Images Size ",valid_x.shape)

```

Validation Images Size (3000, 256, 64, 1)

```

[11]: # Map characters to a specific number from 0 to 26
alphabets = u"ABCDEFGHJKLMNOPQRSTUVWXYZ-"
max_str_len = 24 # max length of input labels
num_of_characters = len(alphabets) + 1 # +1 for ctc pseudo blank
num_of_timestamps = 64 # max length of predicted labels

#Convert a given label to its corresponding Number
def label_to_num(label):
    label_num = []
    for ch in label:
        label_num.append(alphabets.find(ch))

    return np.array(label_num)

#Convert given number list to its corresponding String
def num_to_label(num):
    ret = ""
    for ch in num:
        if ch == -1: # CTC Blank
            break
        else:
            ret+=alphabets[ch]
    return ret

name = 'JEBASTIN'
num_list = label_to_num(name)
print("Name to Number List")
print(name, ' to ',label_to_num(name))

print("Number List to name")
print(num_list," to ",num_to_label(num_list))

```

```

Name to Number List
JEBASTIN to [ 9  4  1  0 18 19  8 13]
Number List to name
[ 9  4  1  0 18 19  8 13] to JEBASTIN

```


[#https://towardsdatascience.com/](https://towardsdatascience.com/)

[→a-comprehensive-guide-to-convolutional-neural-networks-the-eli5-way-3bd2b1164a53](#)

```
input_data = Input(shape=(256, 64, 1), name='input')

inner = Conv2D(32, (3, 3), padding='same', name='conv1',
    ↪kernel_initializer='he_normal')(input_data)
inner = BatchNormalization()(inner)
inner = Activation('relu')(inner)
inner = MaxPooling2D(pool_size=(2, 2), name='max1')(inner)

inner = Conv2D(64, (3, 3), padding='same', name='conv2',
    ↪kernel_initializer='he_normal')(inner)
inner = BatchNormalization()(inner)
inner = Activation('relu')(inner)
inner = MaxPooling2D(pool_size=(2, 2), name='max2')(inner)
inner = Dropout(0.3)(inner)

inner = Conv2D(128, (3, 3), padding='same', name='conv3',
    ↪kernel_initializer='he_normal')(inner)
inner = BatchNormalization()(inner)
inner = Activation('relu')(inner)
inner = MaxPooling2D(pool_size=(1, 2), name='max3')(inner)
inner = Dropout(0.3)(inner)

# CNN to RNN
inner = Reshape(target_shape=((64, 1024)), name='reshape')(inner)
inner = Dense(64, activation='relu', kernel_initializer='he_normal',
    ↪name='dense1')(inner)

## RNN
#https://colah.github.io/posts/2015-08-Understanding-LSTMs/
inner = Bidirectional(LSTM(256, return_sequences=True), name = 'lstm1')(inner)
inner = Bidirectional(LSTM(256, return_sequences=True), name = 'lstm2')(inner)

## OUTPUT
inner = Dense(num_of_characters,
    ↪kernel_initializer='he_normal',name='dense2')(inner)
y_pred = Activation('softmax', name='softmax')(inner)

model = Model(inputs=input_data, outputs=y_pred)
model.summary()
```

Model: "model"

Layer (type)	Output Shape	Param #
--------------	--------------	---------

```

=====
input (InputLayer)          [(None, 256, 64, 1)]      0
-----
conv1 (Conv2D)              (None, 256, 64, 32)    320
-----
batch_normalization (BatchNo (None, 256, 64, 32)    128
-----
activation (Activation)      (None, 256, 64, 32)    0
-----
max1 (MaxPooling2D)         (None, 128, 32, 32)    0
-----
conv2 (Conv2D)              (None, 128, 32, 64)    18496
-----
batch_normalization_1 (Batch (None, 128, 32, 64)    256
-----
activation_1 (Activation)    (None, 128, 32, 64)    0
-----
max2 (MaxPooling2D)         (None, 64, 16, 64)    0
-----
dropout (Dropout)           (None, 64, 16, 64)    0
-----
conv3 (Conv2D)              (None, 64, 16, 128)    73856
-----
batch_normalization_2 (Batch (None, 64, 16, 128)    512
-----
activation_2 (Activation)    (None, 64, 16, 128)    0
-----
max3 (MaxPooling2D)         (None, 64, 8, 128)    0
-----
dropout_1 (Dropout)         (None, 64, 8, 128)    0
-----
reshape (Reshape)           (None, 64, 1024)       0
-----
dense1 (Dense)              (None, 64, 64)         65600
-----
lstm1 (Bidirectional)       (None, 64, 512)        657408
-----
lstm2 (Bidirectional)       (None, 64, 512)        1574912
-----
dense2 (Dense)              (None, 64, 30)         15390
-----
softmax (Activation)        (None, 64, 30)         0
=====
Total params: 2,406,878
Trainable params: 2,406,430
Non-trainable params: 448
-----

```

```
[15]: # the ctc loss function
#https://towardsdatascience.com/
      ↪intuitively-understanding-connectionist-temporal-classification-3797e43a86c
```

```
def ctc_lambda_func(args):
    y_pred, labels, input_length, label_length = args
    # the 2 is critical here since the first couple outputs of the RNN
    # tend to be garbage
    y_pred = y_pred[:, 2:, :]
    return K.ctc_batch_cost(labels, y_pred, input_length, label_length)
```

```
[16]: #Compile the built model with Adam Optimizer and CTC Loss function
```

```
labels = Input(name='gtruth_labels', shape=[max_str_len], dtype='float32')
input_length = Input(name='input_length', shape=[1], dtype='int64')
label_length = Input(name='label_length', shape=[1], dtype='int64')

ctc_loss = Lambda(ctc_lambda_func, output_shape=(1,), name='ctc')([y_pred,
      ↪labels, input_length, label_length])
model_final = Model(inputs=[input_data, labels, input_length, label_length],
      ↪outputs=ctc_loss)

# the loss calculation occurs elsewhere, so we use a dummy lambda function for
      ↪the loss
model_final.compile(loss={'ctc': lambda y_true, y_pred: y_pred},
      ↪optimizer=Adam(lr = 0.0001))
model_final.summary()
```

Model: "model_1"

Layer (type)	Output Shape	Param #	Connected to
=====			
input (InputLayer)	[(None, 256, 64, 1)]	0	

conv1 (Conv2D)	(None, 256, 64, 32)	320	input[0][0]

batch_normalization (BatchNorma	(None, 256, 64, 32)	128	conv1[0][0]

activation (Activation)	(None, 256, 64, 32)	0	
batch_normalization[0][0]			

max1 (MaxPooling2D)	(None, 128, 32, 32)	0	
activation[0][0]			
conv2 (Conv2D)	(None, 128, 32, 64)	18496	max1[0][0]
batch_normalization_1 (BatchNor	(None, 128, 32, 64)	256	conv2[0][0]
activation_1 (Activation)	(None, 128, 32, 64)	0	
batch_normalization_1[0][0]			
max2 (MaxPooling2D)	(None, 64, 16, 64)	0	
activation_1[0][0]			
dropout (Dropout)	(None, 64, 16, 64)	0	max2[0][0]
conv3 (Conv2D)	(None, 64, 16, 128)	73856	dropout[0][0]
batch_normalization_2 (BatchNor	(None, 64, 16, 128)	512	conv3[0][0]
activation_2 (Activation)	(None, 64, 16, 128)	0	
batch_normalization_2[0][0]			
max3 (MaxPooling2D)	(None, 64, 8, 128)	0	
activation_2[0][0]			
dropout_1 (Dropout)	(None, 64, 8, 128)	0	max3[0][0]
reshape (Reshape)	(None, 64, 1024)	0	dropout_1[0][0]
dense1 (Dense)	(None, 64, 64)	65600	reshape[0][0]
lstm1 (Bidirectional)	(None, 64, 512)	657408	dense1[0][0]

lstm2 (Bidirectional)	(None, 64, 512)	1574912	lstm1[0][0]
dense2 (Dense)	(None, 64, 30)	15390	lstm2[0][0]
softmax (Activation)	(None, 64, 30)	0	dense2[0][0]
gtruth_labels (InputLayer)	[(None, 24)]	0	
input_length (InputLayer)	[(None, 1)]	0	
label_length (InputLayer)	[(None, 1)]	0	
ctc (Lambda)	(None, 1)	0	softmax[0][0]
gtruth_labels[0][0]			
input_length[0][0]			
label_length[0][0]			

Total params: 2,406,878
 Trainable params: 2,406,430
 Non-trainable params: 448

```
[17]: #Fit (Train) the model with Train dataset and validation dataset
history = model_final.fit(x=[train_x, train_y, train_input_len,
    ↪train_label_len], y=train_output, validation_data=([valid_x, valid_y,
    ↪valid_input_len, valid_label_len], valid_output), epochs=60, batch_size=128)
#model.save("tfmodelforhandwriting2")
```

```

Train on 30000 samples, validate on 3000 samples
Epoch 1/60
30000/30000 [=====] - 346s 12ms/sample - loss: 27.4047
- val_loss: 20.6685
Epoch 2/60
30000/30000 [=====] - 324s 11ms/sample - loss: 20.2041
- val_loss: 20.1329
Epoch 3/60
30000/30000 [=====] - 322s 11ms/sample - loss: 19.8590
- val_loss: 19.7312
Epoch 4/60
30000/30000 [=====] - 324s 11ms/sample - loss: 19.3577
```

```

- val_loss: 19.4887
Epoch 5/60
30000/30000 [=====] - 326s 11ms/sample - loss: 18.3595
- val_loss: 17.8821
Epoch 6/60
30000/30000 [=====] - 327s 11ms/sample - loss: 16.4965
- val_loss: 15.6969
Epoch 7/60
30000/30000 [=====] - 331s 11ms/sample - loss: 14.0899
- val_loss: 12.9821
Epoch 8/60
30000/30000 [=====] - 338s 11ms/sample - loss: 11.5439
- val_loss: 10.2836
Epoch 9/60
30000/30000 [=====] - 457s 15ms/sample - loss: 9.1600 -
val_loss: 7.6016
Epoch 10/60
30000/30000 [=====] - 252s 8ms/sample - loss: 7.4566 -
val_loss: 6.3227
Epoch 11/60
30000/30000 [=====] - 250s 8ms/sample - loss: 6.3708 -
val_loss: 5.4702
Epoch 12/60
30000/30000 [=====] - 255s 8ms/sample - loss: 5.6287 -
val_loss: 4.9138
Epoch 13/60
30000/30000 [=====] - 250s 8ms/sample - loss: 5.0709 -
val_loss: 4.4533
Epoch 14/60
30000/30000 [=====] - 248s 8ms/sample - loss: 4.6538 -
val_loss: 4.0078
Epoch 15/60
30000/30000 [=====] - 251s 8ms/sample - loss: 4.3035 -
val_loss: 3.8429
Epoch 16/60
30000/30000 [=====] - 248s 8ms/sample - loss: 4.0188 -
val_loss: 3.5299
Epoch 17/60
30000/30000 [=====] - 246s 8ms/sample - loss: 3.7916 -
val_loss: 3.3993
Epoch 18/60
30000/30000 [=====] - 246s 8ms/sample - loss: 3.5884 -
val_loss: 3.1865
Epoch 19/60
30000/30000 [=====] - 250s 8ms/sample - loss: 3.4148 -
val_loss: 3.1259
Epoch 20/60
30000/30000 [=====] - 249s 8ms/sample - loss: 3.2682 -

```

```

val_loss: 3.0308
Epoch 21/60
30000/30000 [=====] - 249s 8ms/sample - loss: 3.1389 -
val_loss: 2.9397
Epoch 22/60
30000/30000 [=====] - 249s 8ms/sample - loss: 3.0173 -
val_loss: 2.8733
Epoch 23/60
30000/30000 [=====] - 249s 8ms/sample - loss: 2.8983 -
val_loss: 2.7407
Epoch 24/60
30000/30000 [=====] - 254s 8ms/sample - loss: 2.8199 -
val_loss: 2.6947
Epoch 25/60
30000/30000 [=====] - 249s 8ms/sample - loss: 2.7258 -
val_loss: 2.6513
Epoch 26/60
30000/30000 [=====] - 248s 8ms/sample - loss: 2.6494 -
val_loss: 2.5457
Epoch 27/60
30000/30000 [=====] - 250s 8ms/sample - loss: 2.5757 -
val_loss: 2.6148
Epoch 28/60
30000/30000 [=====] - 248s 8ms/sample - loss: 2.5049 -
val_loss: 2.4876
Epoch 29/60
30000/30000 [=====] - 247s 8ms/sample - loss: 2.4419 -
val_loss: 2.4605
Epoch 30/60
30000/30000 [=====] - 247s 8ms/sample - loss: 2.3824 -
val_loss: 2.4245
Epoch 31/60
30000/30000 [=====] - 250s 8ms/sample - loss: 2.3292 -
val_loss: 2.4019
Epoch 32/60
30000/30000 [=====] - 250s 8ms/sample - loss: 2.2588 -
val_loss: 2.3331
Epoch 33/60
30000/30000 [=====] - 249s 8ms/sample - loss: 2.2112 -
val_loss: 2.3519
Epoch 34/60
30000/30000 [=====] - 248s 8ms/sample - loss: 2.1535 -
val_loss: 2.3066
Epoch 35/60
30000/30000 [=====] - 246s 8ms/sample - loss: 2.1200 -
val_loss: 2.2845
Epoch 36/60
30000/30000 [=====] - 248s 8ms/sample - loss: 2.0803 -

```



```

val_loss: 2.2995
Epoch 37/60
30000/30000 [=====] - 248s 8ms/sample - loss: 2.0258 -
val_loss: 2.2557
Epoch 38/60
30000/30000 [=====] - 249s 8ms/sample - loss: 1.9942 -
val_loss: 2.2298
Epoch 39/60
30000/30000 [=====] - 248s 8ms/sample - loss: 1.9443 -
val_loss: 2.2369
Epoch 40/60
30000/30000 [=====] - 248s 8ms/sample - loss: 1.9100 -
val_loss: 2.2292
Epoch 41/60
30000/30000 [=====] - 248s 8ms/sample - loss: 1.8683 -
val_loss: 2.1887
Epoch 42/60
30000/30000 [=====] - 248s 8ms/sample - loss: 1.8402 -
val_loss: 2.1828
Epoch 43/60
30000/30000 [=====] - 249s 8ms/sample - loss: 1.8056 -
val_loss: 2.1601
Epoch 44/60
30000/30000 [=====] - 249s 8ms/sample - loss: 1.7624 -
val_loss: 2.1111
Epoch 45/60
30000/30000 [=====] - 248s 8ms/sample - loss: 1.7366 -
val_loss: 2.1557
Epoch 46/60
30000/30000 [=====] - 247s 8ms/sample - loss: 1.6945 -
val_loss: 2.1256
Epoch 47/60
30000/30000 [=====] - 248s 8ms/sample - loss: 1.6682 -
val_loss: 2.1421
Epoch 48/60
30000/30000 [=====] - 251s 8ms/sample - loss: 1.6340 -
val_loss: 2.0936
Epoch 49/60
30000/30000 [=====] - 248s 8ms/sample - loss: 1.5954 -
val_loss: 2.1428
Epoch 50/60
30000/30000 [=====] - 249s 8ms/sample - loss: 1.5753 -
val_loss: 2.1442
Epoch 51/60
30000/30000 [=====] - 246s 8ms/sample - loss: 1.5479 -
val_loss: 2.1363
Epoch 52/60
30000/30000 [=====] - 249s 8ms/sample - loss: 1.5089 -

```

```

val_loss: 2.0912
Epoch 53/60
30000/30000 [=====] - 249s 8ms/sample - loss: 1.4991 -
val_loss: 2.1337
Epoch 54/60
30000/30000 [=====] - 247s 8ms/sample - loss: 1.4600 -
val_loss: 2.1432
Epoch 55/60
30000/30000 [=====] - 250s 8ms/sample - loss: 1.4417 -
val_loss: 2.1204
Epoch 56/60
30000/30000 [=====] - 248s 8ms/sample - loss: 1.4026 -
val_loss: 2.1428
Epoch 57/60
30000/30000 [=====] - 246s 8ms/sample - loss: 1.3715 -
val_loss: 2.1028
Epoch 58/60
30000/30000 [=====] - 249s 8ms/sample - loss: 1.3489 -
val_loss: 2.1268
Epoch 59/60
30000/30000 [=====] - 248s 8ms/sample - loss: 1.3279 -
val_loss: 2.1332
Epoch 60/60
30000/30000 [=====] - 250s 8ms/sample - loss: 1.3042 -
val_loss: 2.1523

```

```

[38]: #To Load the saved Model
      model = tf.keras.models.load_model("tfmodelforhandwriting2")

```

```

[76]: #Predict handwritten Images
      preds = model.predict(valid_x)
      decoded = K.get_value(K.ctc_decode(preds, input_length=np.ones(preds.
      ↪shape[0])*preds.shape[1], greedy=True)[0][0])

      prediction = []
      for i in range(valid_size):
          prediction.append(num_to_label(decoded[i]))
      print("No of Predictions: ",len(prediction))

```

No of Predictions: 3000

```

[77]: #To Find Accuracy of Predicted Characters and Predicted Word
      y_true = valid.loc[0:valid_size-1, 'IDENTITY']
      correct_char = 0
      total_char = 0
      correct = 0
      y_true_char = []
      y_pred_char = []

```

```

for i in range(len(y_true)):
    pr = prediction[i]
    tr = y_true[i]

    for j in range(min(len(tr), len(pr))):
        if tr[j] == pr[j]:
            correct_char += 1
        y_true_char.append(tr[j])
        y_pred_char.append(pr[j])

    if pr == tr :
        correct += 1
print("No of Images " + str(len(y_true)))
print("No of Characters over all Images " + str(len(y_true_char)))
print('Correct characters predicted : %.2f%%' %(correct_char*100/
→len(y_true_char)))
print('Correct words predicted      : %.2f%%' %(correct*100/len(y_true)))

```

No of Images 3000

No of Characters over all Images 19410

Correct characters predicted : 92.51%

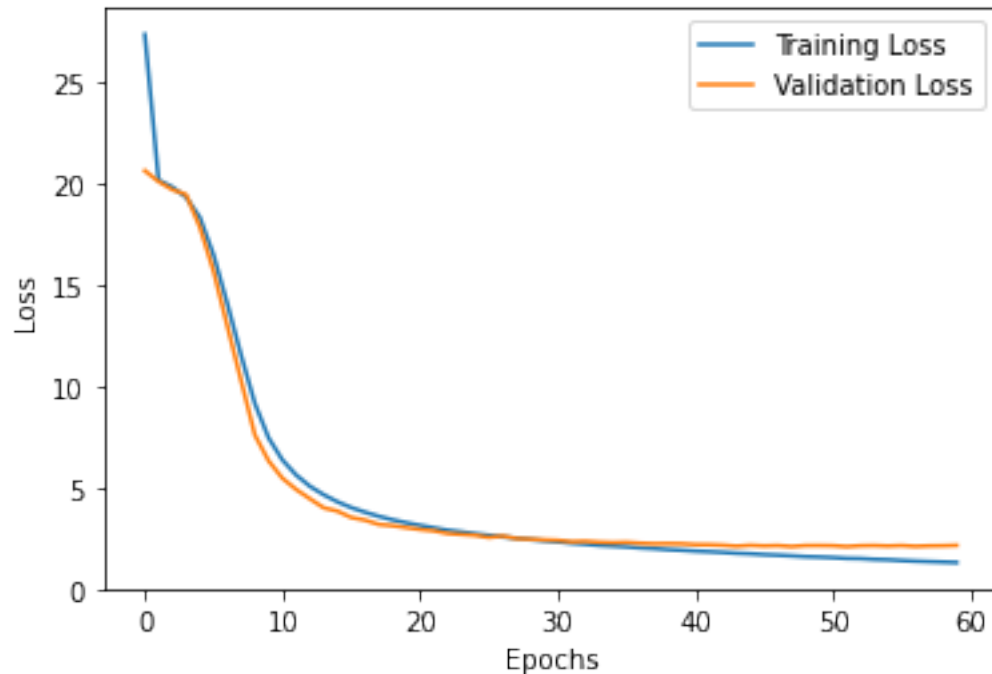
Correct words predicted : 75.17%

```

[33]: #print((history.history))
print("Loss Over training: Model performance")
plt.plot(history.history['loss'])
plt.plot(history.history['val_loss'])
plt.legend(["Training Loss", "Validation Loss"])
plt.xlabel("Epochs")
plt.ylabel("Loss")
plt.show()

```

Loss Over training: Model performance



```
[80]: #Classification Report and Confusion Matrix
print("Classification Report")
print(classification_report(y_true_char,y_pred_char))

cm = (confusion_matrix(y_true_char,y_pred_char,labels =_
    ↳list(u"ABCDEFGHIJKLMNOPQRSTUVWXYZ"),normalize="true"))*100
df_cm = pd.DataFrame(cm,index = list(u"ABCDEFGHIJKLMNOPQRSTUVWXYZ"),columns =_
    ↳list(u"ABCDEFGHIJKLMNOPQRSTUVWXYZ"))
df_cm = df_cm.astype("int32")
sn.set(font_scale=1,rc={'figure.figsize':(10,10)})
sn.heatmap(df_cm,annot=True, annot_kws={"size": 14},cmap='viridis')
plt.title("Confusion Matrix: ")
plt.ylabel("True Characters")
plt.xlabel("Predicted Characters")
plt.show()

mod = "CRNNPredicted"
print("Mean Squared Error: ",mod," ",mean_squared_error([ord(i) for i in_
    ↳y_true_char],[ord(i) for i in y_pred_char]))

clean_result = valid.loc[0:valid_size-1, 'IDENTITY']
```

```

validation_df = pd.Series(prediction,name = mod)
# Create 1 dataframe with both actual and OCR labels
ocr_vs_actual = pd.
    ↳merge(validation_df,clean_result,right_index=True,left_index=True)

# Remove labels which do not exist
ocr_vs_actual = ocr_vs_actual.loc[ocr_vs_actual[mod].notnull(),:]

# Remove spaces in OCR output
ocr_vs_actual['IDENTITY'] = ocr_vs_actual['IDENTITY'].str.replace('\\s', '',
    ↳regex=True)
#ocr_vs_actual.head(10)

# Create jaro-winkler similarity score
vectorized_jaro_winkler = np.vectorize(jaro_winkler)

ocr_vs_actual['SIMILARITY_SCORE'] = vectorized_jaro_winkler(ocr_vs_actual[mod].
    ↳str.upper(), np.where(ocr_vs_actual['IDENTITY'].isnull(), '',
    ↳ocr_vs_actual['IDENTITY'].str.upper()))
print("Similarity Score between True Label and Predicted Label: " + mod)
display(ocr_vs_actual.head(10))

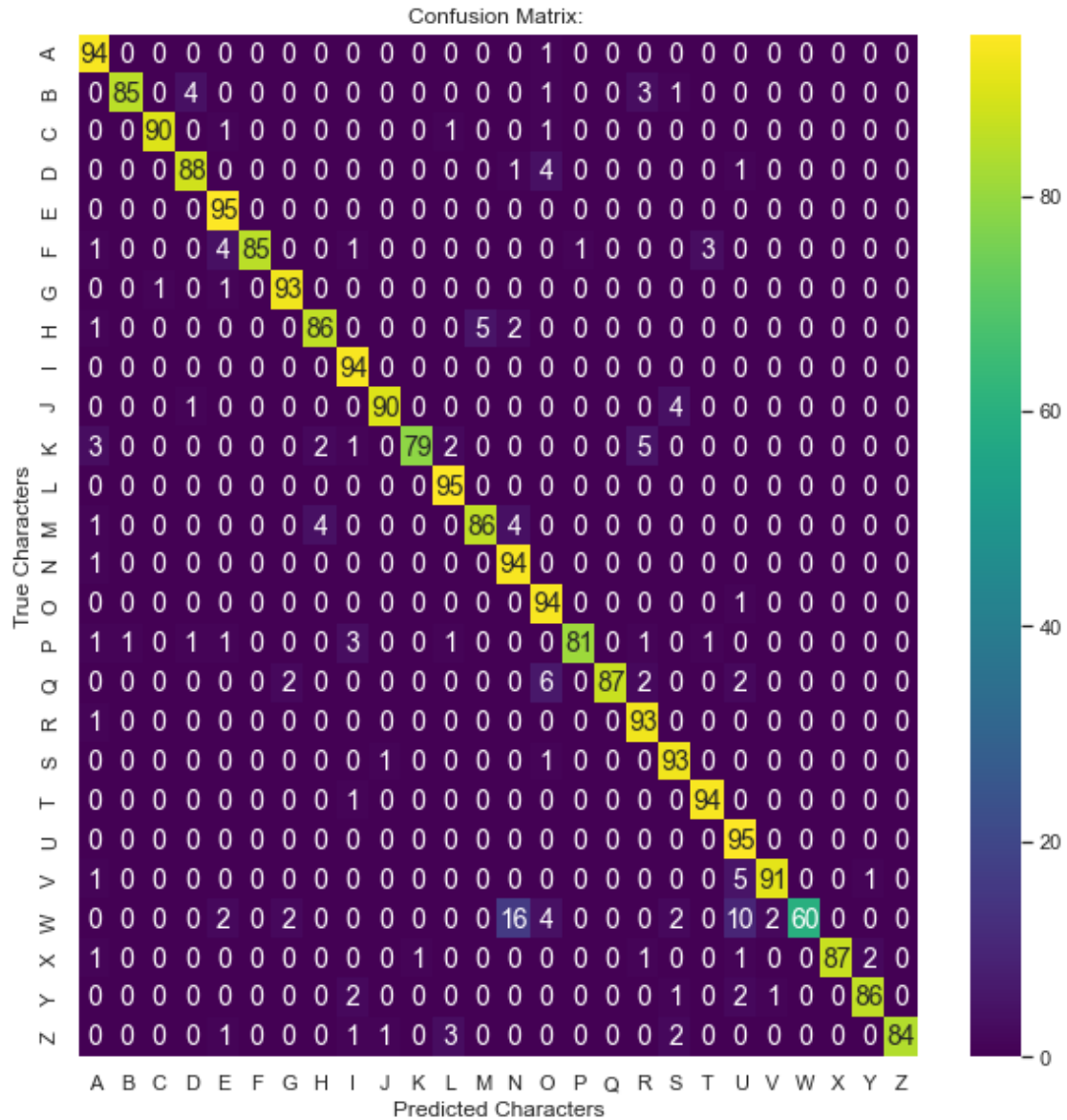
# Plot histogram of similarity scores to see how well we did
print("Histogram of Similarity: " + mod)
plt.style.use('seaborn-white')
plt.figure(figsize=(8,3), dpi=120)
plt.hist(ocr_vs_actual['SIMILARITY_SCORE'], bins=50, alpha=0.5,
    ↳color='steelblue', edgecolor='none')
plt.title('Histogram of Jaro-Winkler similarity score between label and
    ↳OCR-results: ' + mod)
plt.xlabel("Similarity")
plt.ylabel("No of Images")
plt.xticks(np.arange(0, 1.1,0.1))
plt.yticks(np.arange(0,len(ocr_vs_actual)+1,len(ocr_vs_actual)/6))
plt.show()

```

Classification Report

	precision	recall	f1-score	support
	0.76	0.67	0.71	84
'	0.00	0.00	0.00	2
-	0.66	0.75	0.70	51
A	0.94	0.94	0.94	2433
B	0.94	0.85	0.90	446
C	0.92	0.91	0.91	623

D	0.92	0.88	0.90	588
E	0.95	0.95	0.95	2399
F	0.94	0.86	0.90	166
G	0.90	0.94	0.92	362
H	0.88	0.86	0.87	513
I	0.94	0.95	0.94	1587
J	0.86	0.90	0.88	140
K	0.85	0.80	0.82	119
L	0.95	0.95	0.95	1439
M	0.90	0.86	0.88	740
N	0.93	0.94	0.93	1506
O	0.90	0.94	0.92	1240
P	0.88	0.82	0.85	251
Q	0.88	0.88	0.88	48
R	0.93	0.94	0.93	1314
S	0.94	0.93	0.93	805
T	0.94	0.94	0.94	914
U	0.89	0.95	0.92	869
V	0.93	0.91	0.92	225
W	0.76	0.60	0.67	48
X	0.96	0.87	0.92	118
Y	0.88	0.87	0.87	267
Z	0.90	0.85	0.87	113
accuracy			0.93	19410
macro avg	0.86	0.84	0.85	19410
weighted avg	0.93	0.93	0.92	19410



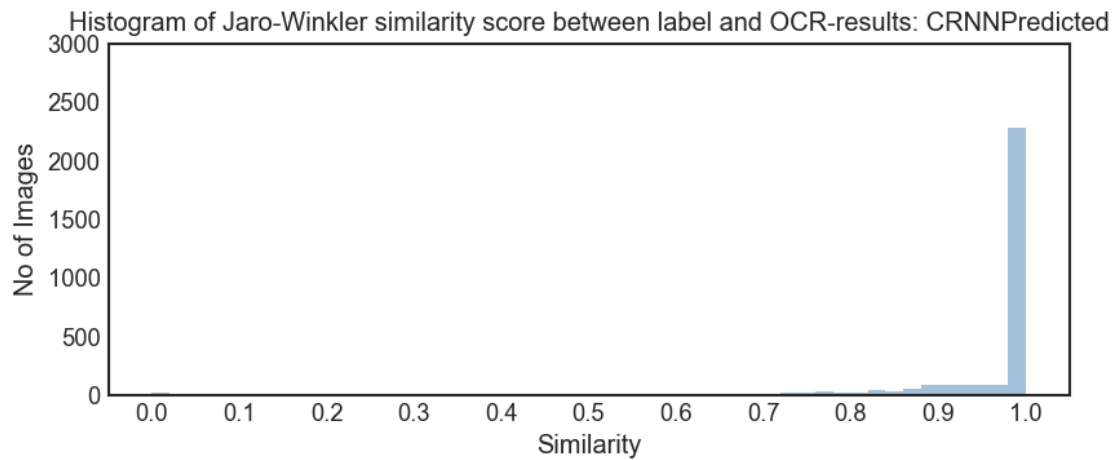
Mean Squared Error: CRNNPredicted 11.183153013910356

Similarity Score between True Label and Predicted Label: CRNNPredicted

	CRNNPredicted	IDENTITY	SIMILARITY_SCORE
0	BILEL	BILEL	1.000000
1	LAUMONIER	LAUMIONIER	0.946667
2	LEA	LEA	1.000000
3	JEAN-ROCH	JEAN-ROCH	1.000000
4	RUPP	RUPP	1.000000
5	PICHON	PICHON	1.000000
6	DANIEL	DANIEL	1.000000
7	JEREMY	JEREMY	1.000000

8	JEAN-MICHEL	JEAN-MICHEL	1.000000
9	JULIEN	JULIEN	1.000000

Histogram of Similarity: CRNNPredicted



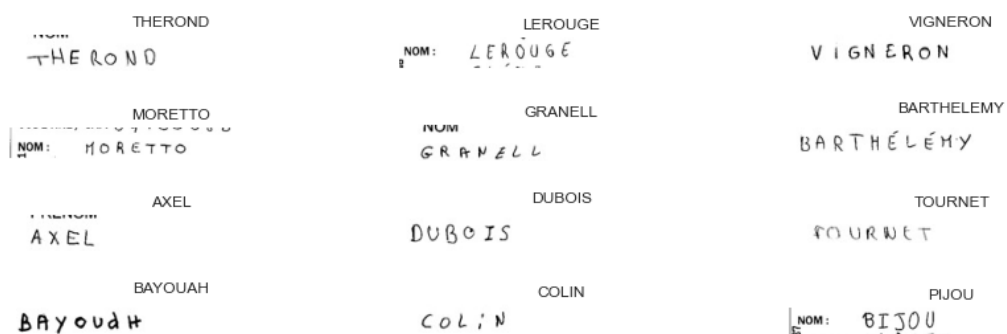
```
[81]: #To test sample Images. To view Sample Images along with predicted Label
#test = pd.read_csv("HandwrittenDataset/written_name_train_v2.csv")
test = pd.read_csv('HandwrittenDataset/written_name_test_v2.csv')

plt.figure(figsize=(15, 10))
start_img_ind = 3000
for i in range(start_img_ind, start_img_ind+12):
    ax = plt.subplot(4, 3, i+1-start_img_ind)
    img_dir = 'HandwrittenDataset/test_v2/test/'+test.loc[i, 'FILENAME']
    #img_dir = 'HandwrittenDataset/train_v2/train/'+test.loc[i, 'FILENAME']
    image = cv2.imread(img_dir, cv2.IMREAD_GRAYSCALE)
    plt.imshow(image, cmap='gray')

    image = preprocess(image)
    image = image/255.
    pred = model.predict(image.reshape(1, 256, 64, 1))
    decoded = K.get_value(K.ctc_decode(pred, input_length=np.ones(pred.
→shape[0])*pred.shape[1], greedy=True)[0][0])
    plt.title(num_to_label(decoded[0]), fontsize=12)

    plt.axis('off')

plt.subplots_adjust(wspace=0.2, hspace=-0.8)
```

```
[7]: #To Load the saved Model
CNNmodel = tf.keras.models.load_model("CNNModel")
print("CNN Model")
print(CNNmodel.summary())
RNNmodel = tf.keras.models.load_model("RNNModel4")
print("RNN Model")
print(RNNmodel.summary())
```

CNN Model

Model: "model_1"

Layer (type)	Output Shape	Param #
input (InputLayer)	[(None, 256, 64, 1)]	0
conv1 (Conv2D)	(None, 256, 64, 32)	320
batch_normalization_3 (Batch Normalization)	(None, 256, 64, 32)	128
activation_3 (Activation)	(None, 256, 64, 32)	0
max1 (MaxPooling2D)	(None, 128, 32, 32)	0
conv2 (Conv2D)	(None, 128, 32, 64)	18496
batch_normalization_4 (Batch Normalization)	(None, 128, 32, 64)	256
activation_4 (Activation)	(None, 128, 32, 64)	0
max2 (MaxPooling2D)	(None, 64, 16, 64)	0
dropout_2 (Dropout)	(None, 64, 16, 64)	0
conv3 (Conv2D)	(None, 64, 16, 128)	73856

```

batch_normalization_5 (Batch Normalization) (None, 64, 16, 128) 512
-----
activation_5 (Activation) (None, 64, 16, 128) 0
-----
max3 (MaxPooling2D) (None, 64, 8, 128) 0
-----
dropout_3 (Dropout) (None, 64, 8, 128) 0
-----
reshape (Reshape) (None, 64, 1024) 0
-----
dense2 (Dense) (None, 64, 30) 30750
-----
softmax (Activation) (None, 64, 30) 0
=====
Total params: 124,318
Trainable params: 123,870
Non-trainable params: 448
-----
None
RNN Model
Model: "model_4"
-----
Layer (type) Output Shape Param #
=====
input_4 (InputLayer) [(None, 16384)] 0
-----
reshape_2 (Reshape) (None, 64, 256) 0
-----
dense_3 (Dense) (None, 64, 64) 16448
-----
lstm_4 (LSTM) (None, 64, 256) 328704
-----
lstm_5 (LSTM) (None, 64, 256) 525312
-----
dense_4 (Dense) (None, 64, 30) 7710
-----
activation_2 (Activation) (None, 64, 30) 0
=====
Total params: 878,174
Trainable params: 878,174
Non-trainable params: 0
-----
None

```

```

[82]: valid = pd.read_csv("TrainTable.csv")
      #display(valid.describe(include="all"))
      valid.fillna('', inplace=True)

```

```
display(valid.head())
display(valid.tail())
print("No of Images Tested with ", len(valid))
```

	Index	FILENAME	IDENTITY	CRNNPredicted	CNNPredicted	RNNPredicted
0	0	TRAIN_00001.jpg	BALTHAZAR	BALTHAZAR	BALTHAZAR	BLALTHAIAR
1	1	TRAIN_00002.jpg	SIMON	SIMON	SIMON	BLIMON
2	2	TRAIN_00003.jpg	BENES	BENES	BENES	BVENES
3	3	TRAIN_00004.jpg	LA LOVE	LALOUE	LALOUE	BLALOUE
4	4	TRAIN_00005.jpg	DAPHNE	DAPHNE	DAPHNE	CMAHNE

	Index	FILENAME	IDENTITY	CRNNPredicted	CNNPredicted	RNNPredicted \
330287	330287	TRAIN_330957.jpg	LENNY	LENNY	LENNY	LENNY
330288	330288	TRAIN_330958.jpg	TIFFANY	TIFFANY	TIFFANY	TIEEANY
330289	330289	TRAIN_330959.jpg	COUTINHO DESA	COUTINHO DESA	COUTINHO DESA	COUTINHODESA
330290	330290	TRAIN_330960.jpg	MOURAD	MOURAD	MOURAD	AOURAD
330291	330291	TRAIN_330961.jpg	HELOISE	HELOISE	HELOISE	HELOISE

	RNNPredicted
330287	BLENNY
330288	BLIEFANY
330289	BCOUTINO DEA
330290	BAOURAD
330291	BLELOISE

No of Images Tested with 330292

```
[84]: col_names = ["CRNNPredicted", "CNNPredicted", "RNNPredicted"]
hsh_class = {}
for mod in col_names:
    print("Prediction Result for ", mod)
    prediction = valid[mod]
    y_true = valid['IDENTITY']
    correct_char = 0
    total_char = 0
    correct = 0
    y_true_char = []
    y_pred_char = []
    for i in range(len(y_true)):
        pr = (prediction[i])
        tr = y_true[i]
        total_char += min(len(tr), len(pr))
        #print(tr, pr)
        for j in range(min(len(tr), len(pr))):
            if mod == "RNNPredicted":
                if tr[-j] == pr[-j]:
                    correct_char += 1
            y_true_char.append(tr[-j])
```

```

        y_pred_char.append(pr[-j])
    else:
        if tr[j] == pr[j]:
            correct_char += 1
        y_true_char.append(tr[j])
        y_pred_char.append(pr[j])

    if pr == tr :
        correct += 1

print("No of Images " + str(len(y_true)))
print("No of Characters over all Images " + str(len(y_true_char)))
print('Correct characters predicted : %.2f%%' %(correct_char*100/
→len(y_true_char)))
print('Correct words predicted      : %.2f%%' %(correct*100/len(y_true)))
print("Classification Report: " + mod)
print(classification_report(y_true_char,y_pred_char,zero_division=0))
hsh_class[mod] =_
→classification_report(y_true_char,y_pred_char,zero_division=0,output_dict =_
→True)
print("Confusion Matrix: " + mod)
cm = (confusion_matrix(y_true_char,y_pred_char,labels =_
→list(u"ABCDEFGHJKLMNOPQRSTUVWXYZ"),normalize="true"))*100
df_cm = pd.DataFrame(cm,index = list(u"ABCDEFGHJKLMNOPQRSTUVWXYZ"),columns_
→= list(u"ABCDEFGHJKLMNOPQRSTUVWXYZ"))
df_cm = df_cm.astype("int32")
sn.set(font_scale=1,rc={'figure.figsize':(10,10)})
sn.heatmap(df_cm,annot=True, annot_kws={"size": 14},cmap='viridis')
plt.title("Confusion Matrix: " + mod)
plt.ylabel("True Characters")
plt.xlabel("Predicted Characters")
plt.show()

print("Mean Squared Error: ",mod," ",mean_squared_error([ord(i) for i in_
→y_true_char],[ord(i) for i in y_pred_char]))

clean_result = valid["IDENTITY"]
validation_df = pd.Series(prediction,name = mod)
# Create 1 dataframe with both actual and OCR labels
ocr_vs_actual = pd.
→merge(validation_df,clean_result,right_index=True,left_index=True)

# Remove labels which do not exist
ocr_vs_actual = ocr_vs_actual.loc[ocr_vs_actual[mod].notnull(),:]

```

```

# Remove spaces in OCR output
ocr_vs_actual['IDENTITY'] = ocr_vs_actual['IDENTITY'].str.replace('\s',
↳ '', regex=True)
#ocr_vs_actual.head(10)

# Create jaro-winkler similarity score
vectorized_jaro_winkler = np.vectorize(jaro_winkler)

ocr_vs_actual['SIMILARITY_SCORE'] =
↳ vectorized_jaro_winkler(ocr_vs_actual[mod].str.upper(), np.
↳ where(ocr_vs_actual['IDENTITY'].isnull(), '', ocr_vs_actual['IDENTITY'].str.
↳ upper()))
print("Similarity Score between True Label and Predicted Label: " + mod)
display(ocr_vs_actual.head(10))

# Plot histogram of similarity scores to see how well we did
print("Histogram of Similarity: " + mod)
plt.style.use('seaborn-white')
plt.figure(figsize=(8,3), dpi=120)
plt.hist(ocr_vs_actual['SIMILARITY_SCORE'], bins=50, alpha=0.5,
↳ color='steelblue', edgecolor='none')
plt.title('Histogram of Jaro-Winkler similarity score: '+ mod)
plt.xlabel("Similarity")
plt.ylabel("No of Images")
plt.xticks(np.arange(0, 1.1,0.1))
#plt.yticks(np.arange(0, len(ocr_vs_actual)+1, len(ocr_vs_actual)/6))
plt.show()

```

Prediction Result for CRNNPredicted

No of Images 330292

No of Characters over all Images 2134747

Correct characters predicted : 92.98%

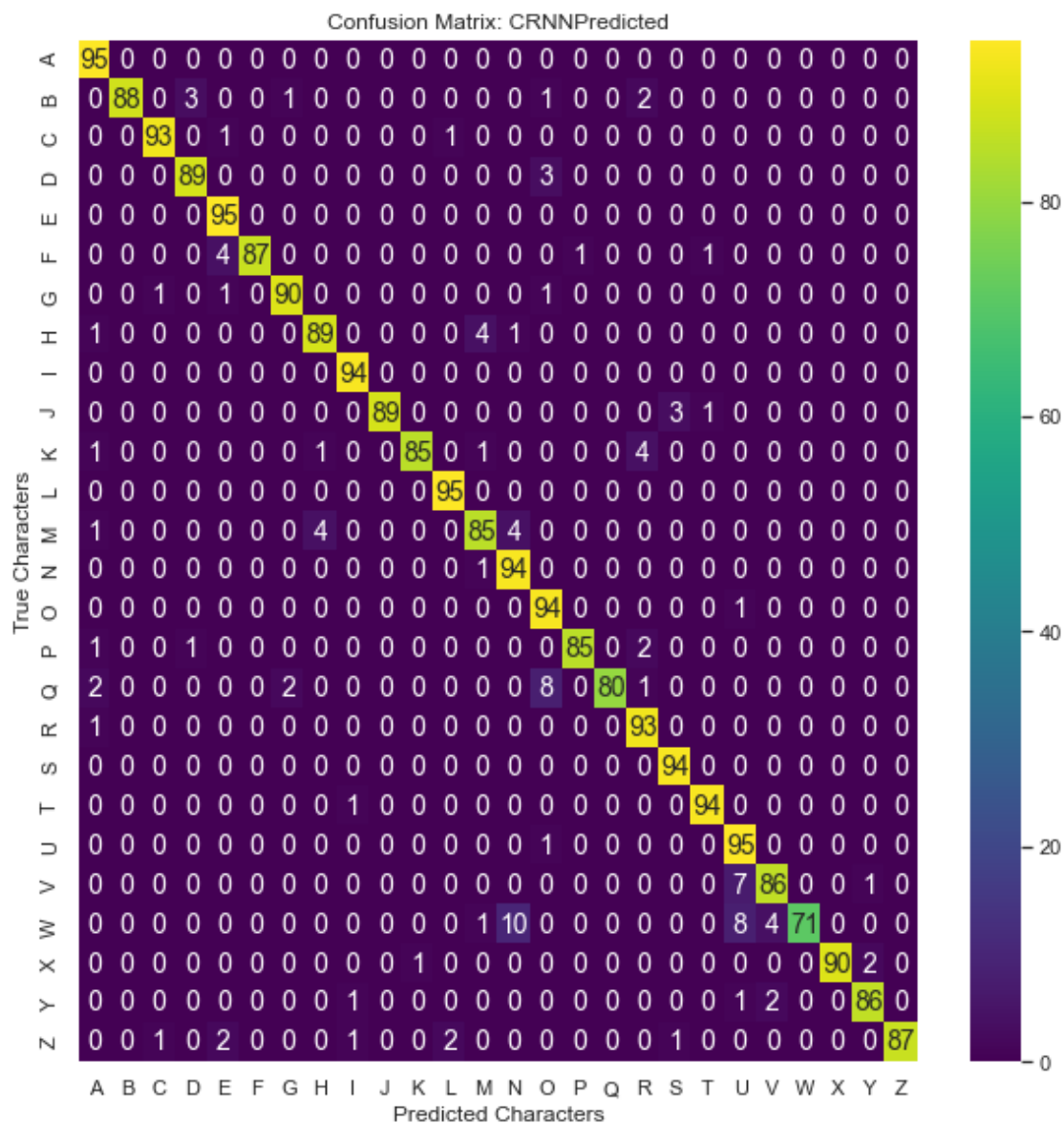
Correct words predicted : 75.56%

Classification Report: CRNNPredicted

	precision	recall	f1-score	support
	0.76	0.63	0.69	10100
#	0.00	0.00	0.00	1
'	0.61	0.22	0.32	230
-	0.66	0.72	0.69	6493
?	0.00	0.00	0.00	0
A	0.95	0.95	0.95	266965
B	0.93	0.88	0.91	45634
C	0.91	0.93	0.92	67580
D	0.91	0.89	0.90	59587

E	0.95	0.96	0.95	266361
F	0.93	0.88	0.90	18135
G	0.90	0.90	0.90	38807
H	0.90	0.89	0.89	61232
I	0.95	0.95	0.95	171683
J	0.90	0.89	0.90	15745
K	0.91	0.86	0.88	13880
L	0.95	0.95	0.95	159677
M	0.90	0.86	0.88	83273
N	0.93	0.94	0.94	164645
O	0.92	0.94	0.93	134912
P	0.90	0.86	0.88	29106
Q	0.88	0.80	0.84	5131
R	0.94	0.93	0.94	146178
S	0.95	0.95	0.95	89762
T	0.93	0.94	0.94	99376
U	0.90	0.95	0.93	95253
V	0.91	0.87	0.89	24865
W	0.85	0.71	0.78	5464
X	0.94	0.90	0.92	11116
Y	0.88	0.86	0.87	29630
Z	0.92	0.88	0.90	13925
`	0.00	0.00	0.00	1
accuracy			0.93	2134747
macro avg	0.81	0.78	0.79	2134747
weighted avg	0.93	0.93	0.93	2134747

Confusion Matrix: CRNNPredicted



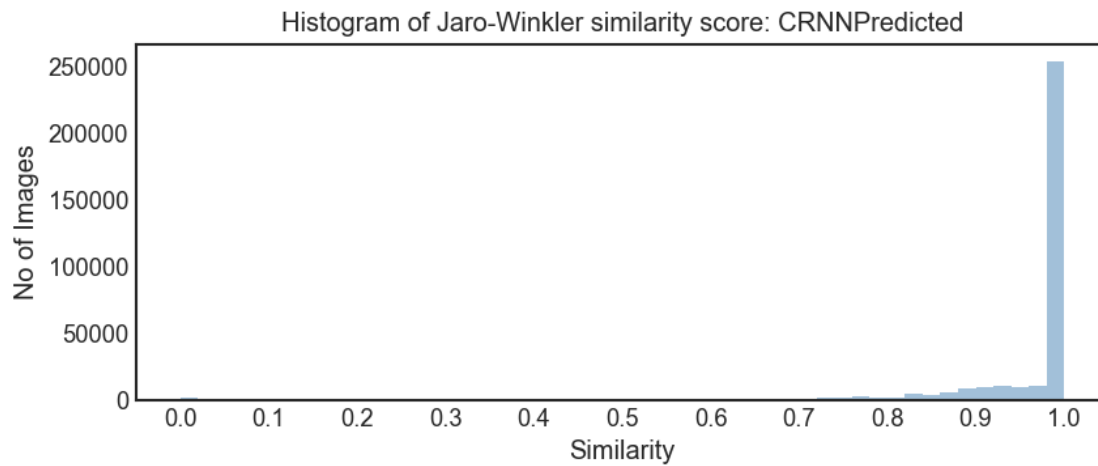
Mean Squared Error: CRNNPredicted 10.623822869876383

Similarity Score between True Label and Predicted Label: CRNNPredicted

	CRNNPredicted	IDENTITY	SIMILARITY_SCORE
0	BALTHAZAR	BALTHAZAR	1.000000
1	SIMON	SIMON	1.000000
2	BENES	BENES	1.000000
3	LALOUÉ	LALOVE	0.933333
4	DAPHNE	DAPHNE	1.000000
5	LUCIE	LUCIE	1.000000
6	NASSIM	NASSIM	1.000000
7	ASSRAOUI	ASSRAOUI	1.000000

8	VLAVIAN	LAVIAN	0.869048
9	MAEVA	MAEVA	1.000000

Histogram of Similarity: CRNNPredicted



Prediction Result for CRNNPredicted

No of Images 330292

No of Characters over all Images 2090486

Correct characters predicted : 84.25%

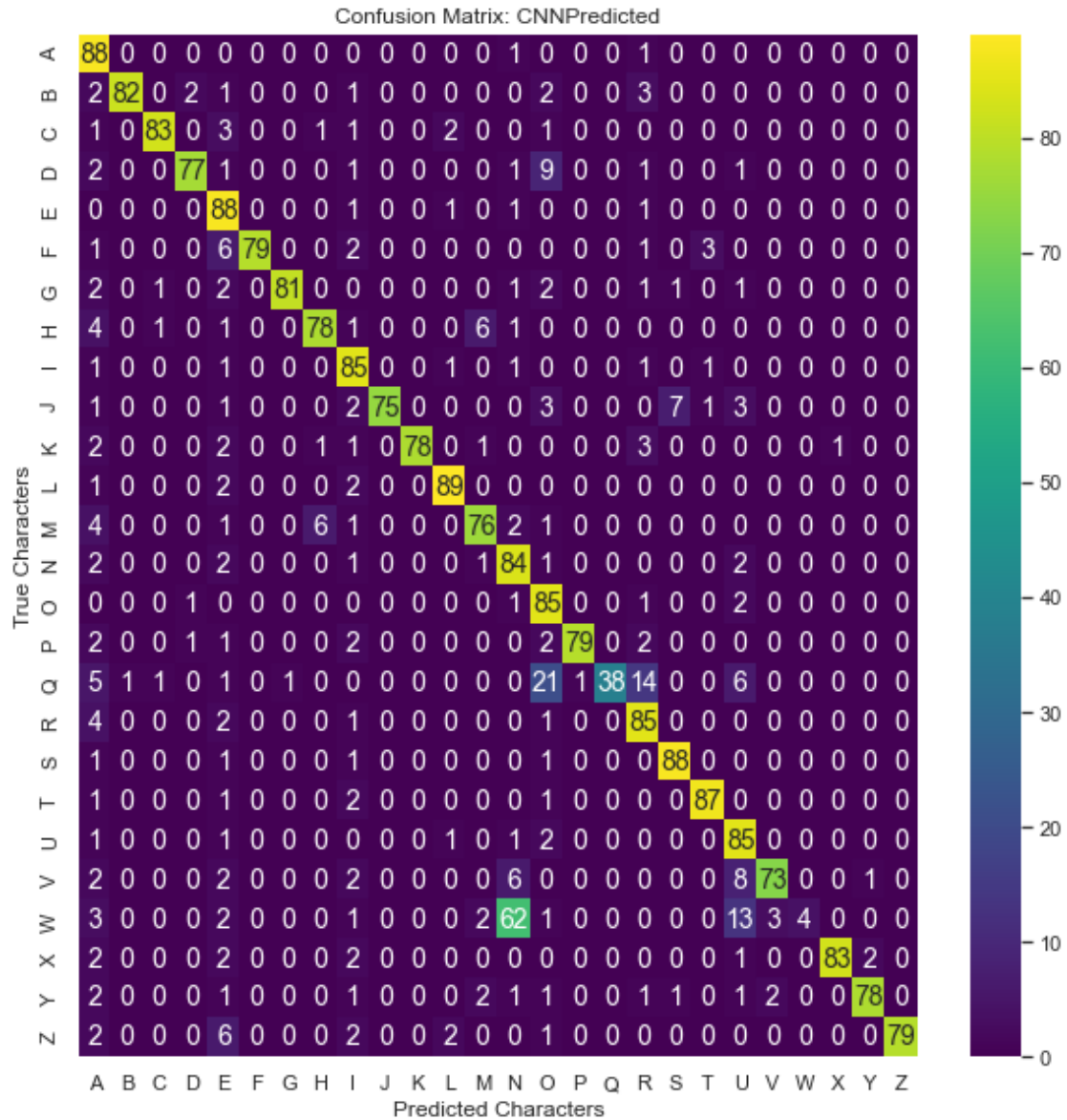
Correct words predicted : 59.54%

Classification Report: CRNNPredicted

	precision	recall	f1-score	support
	0.01	0.00	0.00	9874
#	0.00	0.00	0.00	1
'	0.00	0.00	0.00	217
-	0.58	0.51	0.55	6406
A	0.86	0.88	0.87	262418
B	0.85	0.82	0.83	45311
C	0.83	0.84	0.84	66669
D	0.83	0.77	0.80	58235
E	0.87	0.88	0.88	258264
F	0.82	0.79	0.81	17890
G	0.85	0.81	0.83	38457
H	0.77	0.79	0.78	60455
I	0.84	0.86	0.85	168646
J	0.86	0.75	0.80	15684
K	0.84	0.78	0.81	13612
L	0.89	0.89	0.89	157627
M	0.80	0.77	0.78	81691
N	0.84	0.85	0.84	159273
O	0.80	0.86	0.83	132511

P	0.84	0.80	0.82	28657
Q	0.77	0.39	0.51	5065
R	0.84	0.85	0.85	143343
S	0.87	0.88	0.87	86890
T	0.88	0.88	0.88	96796
U	0.79	0.86	0.82	93805
V	0.79	0.73	0.76	24637
W	0.57	0.04	0.08	5405
X	0.84	0.83	0.84	10624
Y	0.84	0.78	0.81	28490
Z	0.85	0.79	0.82	13532
`	0.00	0.00	0.00	1
accuracy			0.84	2090486
macro avg	0.71	0.67	0.68	2090486
weighted avg	0.84	0.84	0.84	2090486

Confusion Matrix: CNNPredicted



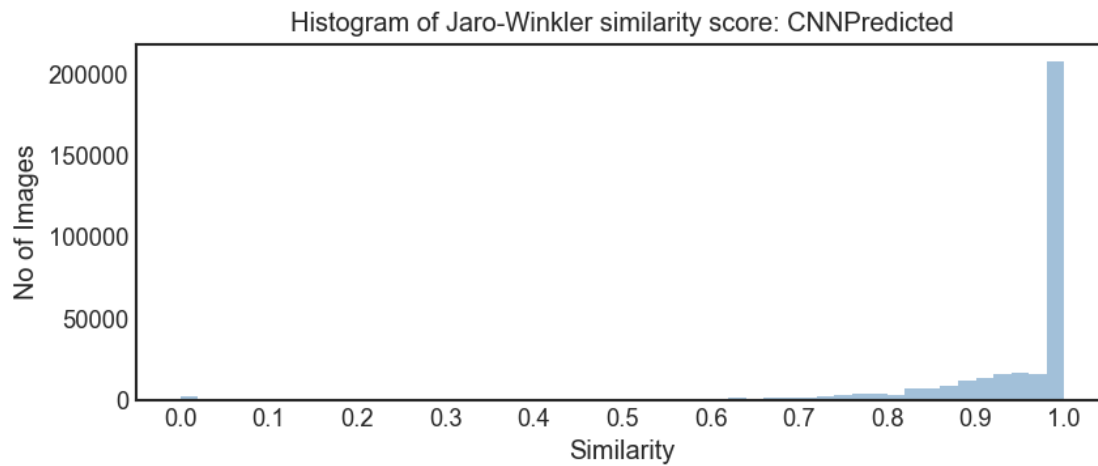
Mean Squared Error: CNNPredicted 25.33519956603393

Similarity Score between True Label and Predicted Label: CNNPredicted

	CNNPredicted	IDENTITY	SIMILARITY_SCORE
0	BALTHAZAR	BALTHAZAR	1.000000
1	SIMON	SIMON	1.000000
2	BENES	BENES	1.000000
3	LALOUÉ	LALOVE	0.933333
4	DAPHNE	DAPHNE	1.000000
5	LUCIE	LUCIE	1.000000
6	NASSIM	NASSIM	1.000000
7	ASSRAOUI	ASSRAOUI	1.000000

8	MLAVIAN	LAVIAN	0.952381
9	MAEVA	MAEVA	1.000000

Histogram of Similarity: CNNPredicted



Prediction Result for RNNPredicted

No of Images 330292

No of Characters over all Images 2144334

Correct characters predicted : 69.81%

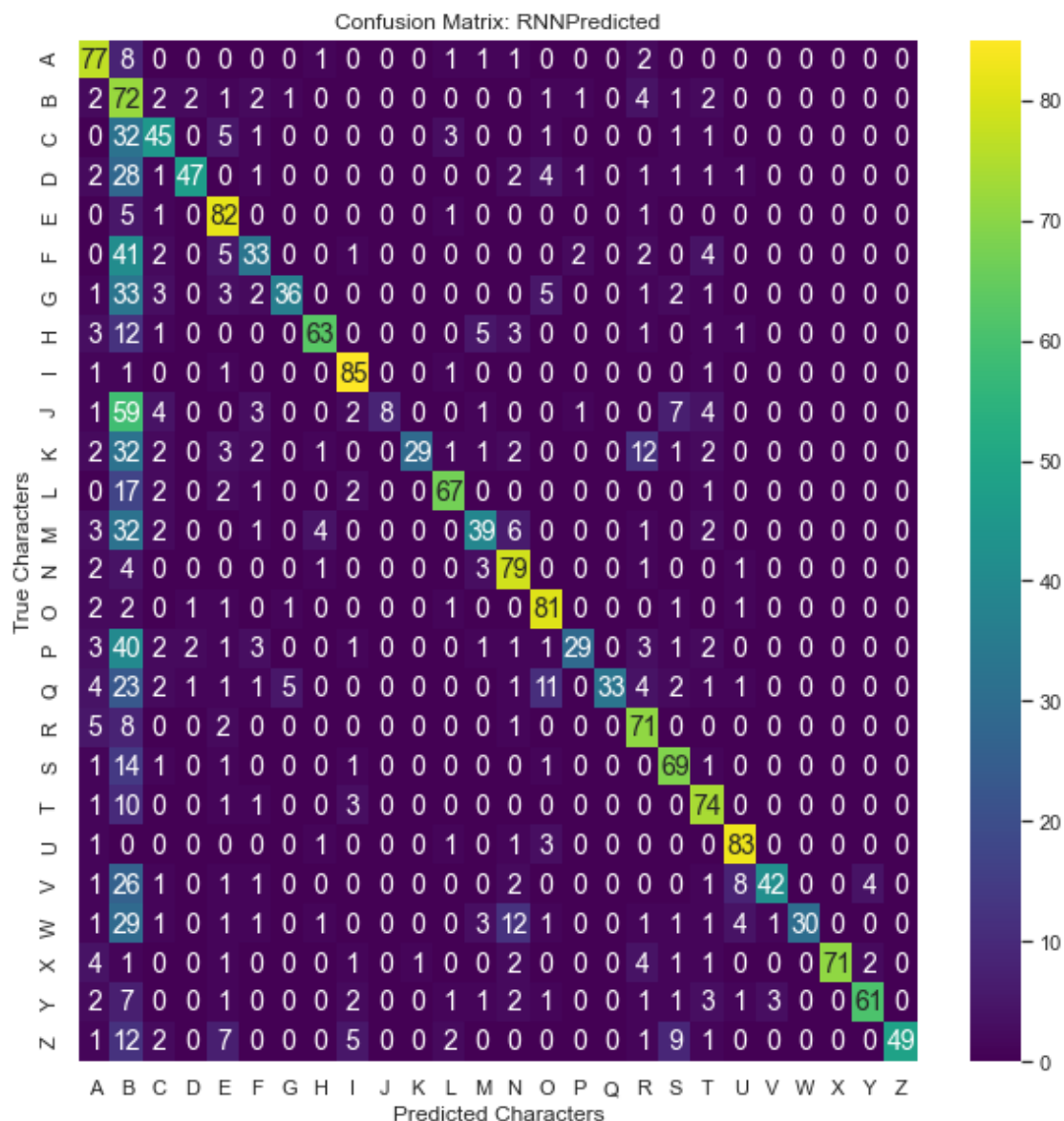
Correct words predicted : 0.26%

Classification Report: RNNPredicted

	precision	recall	f1-score	support
	0.56	0.42	0.48	9877
#	0.00	0.00	0.00	1
'	0.45	0.10	0.16	216
-	0.40	0.44	0.42	6474
?	0.00	0.00	0.00	1
A	0.84	0.77	0.81	266860
B	0.12	0.72	0.20	45613
C	0.52	0.45	0.48	67799
D	0.73	0.48	0.58	60078
E	0.87	0.82	0.85	268372
F	0.24	0.33	0.28	18198
G	0.64	0.37	0.47	38919
H	0.73	0.63	0.67	61191
I	0.87	0.85	0.86	172547
J	0.27	0.08	0.13	15759
K	0.59	0.30	0.39	14022
L	0.83	0.68	0.74	160140
M	0.60	0.39	0.47	82771
N	0.84	0.79	0.81	166194

O	0.83	0.81	0.82	134731
P	0.47	0.29	0.36	29025
Q	0.56	0.33	0.41	5134
R	0.79	0.72	0.75	146995
S	0.78	0.69	0.73	90876
T	0.75	0.74	0.74	100754
U	0.83	0.83	0.83	95309
V	0.56	0.42	0.48	24921
W	0.57	0.31	0.40	5481
X	0.82	0.71	0.76	11300
Y	0.78	0.61	0.69	30703
Z	0.69	0.50	0.58	14072
`	0.00	0.00	0.00	1
accuracy			0.70	2144334
macro avg	0.58	0.49	0.51	2144334
weighted avg	0.76	0.70	0.72	2144334

Confusion Matrix: RNNPredicted



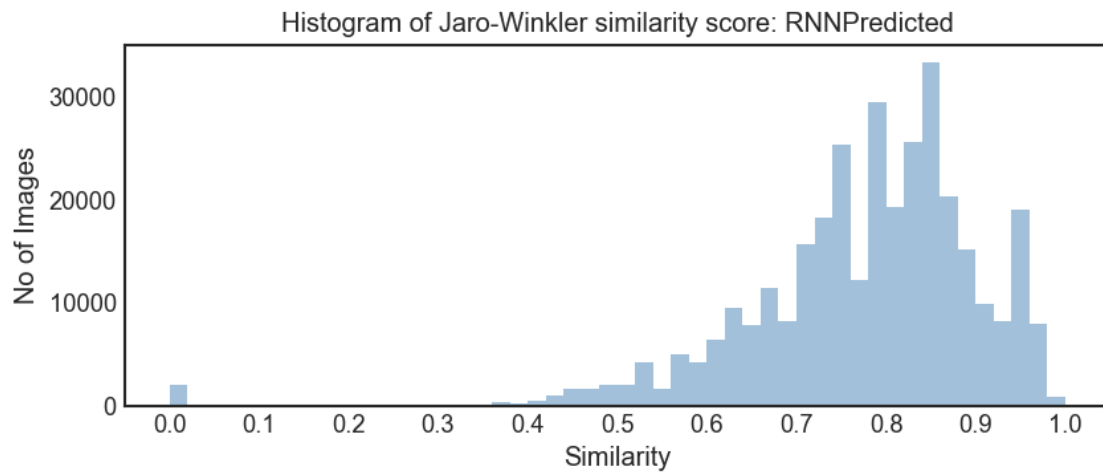
Mean Squared Error: RNNPredicted 41.535935166816365

Similarity Score between True Label and Predicted Label: RNNPredicted

	RNNPredicted	IDENTITY	SIMILARITY_SCORE
0	BLALTHAIAR	BALTHAZAR	0.869167
1	BLIMON	SIMON	0.822222
2	BVENES	BENES	0.950000
3	BLALOUE	LALOVE	0.849206
4	CMAHPNE	DAPHNE	0.849206
5	BLUCIE	LUCIE	0.944444
6	BCMASSIM	NASSIM	0.652778
7	TFBSSRAOUI	ASSRAOUI	0.858333

8	BALAVRAN	LAVIAN	0.686111
9	BLAEVA	MAEVA	0.822222

Histogram of Similarity: RNNPredicted



```
[68]: fig,ax = plt.subplots()

ax.
    ↳plot(list(u"ABCDEFGHIJKLMNOPQRSTUVWXYZ"),[hsh_class["CRNNPredicted"][i]["f1-score"]_
    ↳for i in "ABCDEFGHIJKLMNOPQRSTUVWXYZ"])

ax.
    ↳plot(list(u"ABCDEFGHIJKLMNOPQRSTUVWXYZ"),[hsh_class["CNNPredicted"][i]["f1-score"]_
    ↳for i in "ABCDEFGHIJKLMNOPQRSTUVWXYZ"])

ax.
    ↳plot(list(u"ABCDEFGHIJKLMNOPQRSTUVWXYZ"),[hsh_class["RNNPredicted"][i]["f1-score"]_
    ↳for i in "ABCDEFGHIJKLMNOPQRSTUVWXYZ"])
ax.set_title('f1-score vs Classes')
ax.legend(['CRNN','CNN','RNN'])
ax.xaxis.set_label_text('Characters')
ax.yaxis.set_label_text('f1-score')
plt.yticks(np.arange(0,1.1, 0.1))
plt.show()
```

