

Regression  $\Rightarrow y = mx + c$

$$\bar{x} = \frac{1}{n} \sum x_i, \quad \bar{y} = \frac{1}{n} \sum y_i$$

$$\text{var}(x) = \frac{1}{n-1} \sum (x_i - \bar{x})^2$$

$$\text{Cov}(x, y) = \frac{1}{n-1} \sum [(x_i - \bar{x}) \cdot (y_i - \bar{y})]$$

$$m = \frac{\text{Cov}(x, y)}{\text{var}(x)}, \quad c = \bar{y} - m\bar{x}$$

Q  $\Rightarrow$

| x  | y  |
|----|----|
| 43 | 99 |
| 21 | 65 |
| 25 | 79 |
| 42 | 75 |
| 57 | 87 |
| 59 | 81 |

$$\bar{x} = \frac{1}{n} \sum x_i, \quad \bar{y} = \frac{1}{n} \sum y_i$$

$$\bar{x} = 41.16, \quad \bar{y} = 81$$

$$\text{var}(x) = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2$$

$$= 248.16$$

$$\text{Cov}(x, y) = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})$$

$$= 6.62 + 64.51 + 6.46 - 1.008$$

$$+ 19.008 + 0$$

$$= 95.6 \text{ J}.$$

$$m = \frac{\text{Cov}(x, y)}{\text{Var}(x)} = \frac{95.6}{248.16} = 0.385$$

$$c = \bar{y} - m\bar{x} = 81 - 0.385 * 41.16$$

$$= 65.15$$

$$y = 0.385x + 65.15$$