

1.9.1

EE25BTECH11012-BEERAM MADHURI

Question:

The distance between the points $(m, -n)$ and $(-m, n)$ is _____.

Solution: let **A** and **B** be the vectors such that:

Variable	value
A	$\begin{pmatrix} m \\ -n \end{pmatrix}$
B	$\begin{pmatrix} -m \\ n \end{pmatrix}$

TABLE 0: Variables used

Distance between **A** and **B** or Norm of **A - B** is:

$$\begin{aligned}
 \|\mathbf{A} - \mathbf{B}\| &= \sqrt{\|\mathbf{A}\|^2 + \|\mathbf{B}\|^2 - 2\mathbf{A}^\top \mathbf{B}} \\
 &= \sqrt{(m^2 + n^2) - 2(-m^2 - n^2) + m^2 + n^2} \\
 &= \sqrt{4(m^2 + n^2)} \\
 &= 2\sqrt{m^2 + n^2}
 \end{aligned}$$

Hence Distance between **A** and **B** is $2\sqrt{m^2 + n^2}$.

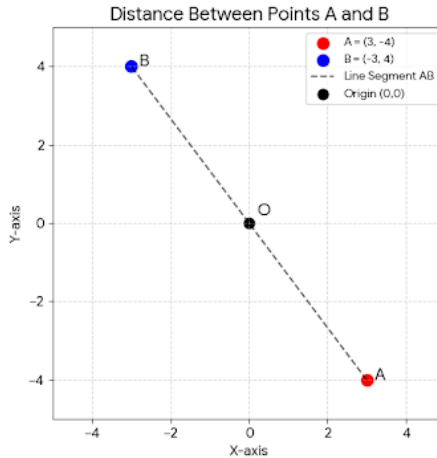


Fig. 0.1: Plot