Zeroth-order tableau rule sheet

Peter Susanszky: Learning Logic Backwards

1.
$$X \wedge Y$$

2.
$$X \wedge 1$$

1.
$$X \wedge Y$$

2.
$$Y \wedge 1$$

∧: Conjunction rule

1.
$$\neg (X \lor Y)$$

$$2. \quad \neg X$$

1.
$$\neg (X \lor Y)$$

$$2.$$
 $\neg Y$

 $\neg \lor$: Negated disjunction rule

 $\neg \lor 1$

 $\neg \lor 1$

1.
$$\neg (X \to Y)$$

2.
$$X \longrightarrow X$$

1.
$$\neg(X \to Y)$$

$$2. \qquad \neg Y \qquad \neg \rightarrow$$

 $\neg \rightarrow$: Negated conditional rule

1.
$$X \vee Y$$

$$2. \qquad X \quad Y \qquad \vee 1$$

 \lor : Disjunction rule

1.
$$X \to Y$$

$$2. \qquad \neg X \qquad Y \qquad \rightarrow 1$$

 \rightarrow : Conditional rule

1.
$$\neg (X \land Y)$$

$$2. \quad \neg X \quad \neg Y \quad \neg \land 1$$

 $\neg \wedge$: Negated conjunction rule

1.
$$\neg \neg X$$

$$2. \qquad X \qquad \neg \neg \ 1$$

 $\neg\neg$: Double negation rule