

Chapter 8 – Ratio and Proportion

Exercise 8.1 – Ratios

1. Find the ratio in lowest terms:

- (i) ₹75 and 80 $\rightarrow 75:80 = 15:16$
 - (ii) ₹55 and 15.40 \rightarrow convert to paise: $5500:1540 = 25:7$
 - (iii) 120 kg and 150 kg $\rightarrow 120:150 = 4:5$
 - (iv) 150 g and 2 kg $\rightarrow 150:2000 = 3:40$
 - (v) 2 hours 30 minutes and 50 minutes $\rightarrow 150:50 = 3:1$
 - (vi) 20 hours and 1 day $\rightarrow 20:24 = 5:6$
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2. Divide ₹1,080 in ratio 5:7

Total parts = 12 \rightarrow One part = $1080 \div 12 = 90$
 $A = 5 \times 90 = ₹450$, $B = 7 \times 90 = ₹630$

3. Divide 24 chocolates in ratio 5:3

Total parts = 8 \rightarrow One part = $24 \div 8 = 3$
Jaya = $5 \times 3 = 15$, Mansi = $3 \times 3 = 9$

4. Divide 20 bananas in ratio 2:2:1

Total parts = 5 \rightarrow One part = $20 \div 5 = 4$
John = $2 \times 4 = 8$, Rahul = $2 \times 4 = 8$, Jafar = $1 \times 4 = 4$

5. Divide 80 in ratio 5:2:1

Total parts = 8 \rightarrow One part = $80 \div 8 = 10$
Sheela = 50, Sudha = 20, Sharda = 10

6. Income ₹18,200, expenditure ₹11,700, savings = ₹6,500

(i) Expenditure:Savings = $11700:6500 = 9:5$

(ii) Income:Expenditure = $18200:11700 = 14:9$

(iii) Savings:Income = $6500:18200 = 5:14$

7. Boys:Girls = 5:4, Total = 540

Total parts = 9 \rightarrow One part = $540 \div 9 = 60$

Boys = $5 \times 60 = 300$, Girls = $4 \times 60 = 240$

8. Rectangle perimeter = 80 cm, L:B = 5:3

$L + B = 40 \rightarrow$ Let $L=5k$, $B=3k \rightarrow 8k=40 \rightarrow k=5$

Length = 25 cm, Breadth = 15 cm

9. Alloy Copper:Zinc = 2:1, Total = 4.8 kg

Zinc = $\frac{1}{3} \times 4.8 = 1.6$ kg

10. Triangle perimeter = 50 cm, sides ratio 2:3:5

Total parts = 10 \rightarrow One part = $50 \div 10 = 5$

Sides = $2 \times 5 = 10$ cm, $3 \times 5 = 15$ cm, $5 \times 5 = 25$ cm

11. Angles ratio 2:5:2

Total parts = 9 \rightarrow One part = $180 \div 9 = 20^\circ$

Angles = $2 \times 20 = 40^\circ$, $5 \times 20 = 100^\circ$, $2 \times 20 = 40^\circ$

12. Which ratio is greater?

(i) $3:7$ vs $5:11 \rightarrow 5:11$ is greater

(ii) $5:9$ vs $3:7 \rightarrow 5:9$ is greater

(iii) $8:11$ vs $5:6 \rightarrow 5:6$ is greater

(iv) $8:3$ vs $5:2 \rightarrow 8:3$ is greater

Exercise 8.2 – Proportion

1. Are 5, 6, 15, 18 in proportion?

$$5:6::15:18 \rightarrow 5 \times 18 = 6 \times 15 \rightarrow \text{Yes}$$

2. Are 35, 49, 5, 8 in proportion?

$$35 \times 8 \neq 49 \times 5 \rightarrow \text{No}$$

3. Are 16, 18, 24, 18 in proportion?

$$16 \times 18 \neq 18 \times 24 \rightarrow \text{No}$$

4. Find x

(i) $5:7::15:x \rightarrow x = 15 \times 7 \div 5 = 21$

(ii) $8:7::x:21 \rightarrow x = 8 \times 21 \div 7 = 24$

(iii) $7:x::3:6 \rightarrow x = 14$

(iv) $x:9::28:36 \rightarrow x = 7$

5. Rashmi and Sangeeta weight ratio 5:7, Rashmi = 50 kg

$$\text{One part} = 50 \div 5 = 10 \rightarrow \text{Sangeeta} = 7 \times 10 = 70 \text{ kg}$$

6. Girls:Boys = 7:8, Boys = 368 \rightarrow Girls = $7 \times (368 \div 8) = 322$

7. Park L:B = 7:4, L = 56 m \rightarrow B = 32 m

8. Metals A:B = 5:8, A = 91 g \rightarrow B = $8 \times (91 \div 5) = 145.6$ g

9. 8 books = 96 \rightarrow 15 books = $15 \times (96 \div 8) = 180$

10. 25 kg wheat = 200 \rightarrow 35 kg = $35 \times (200 \div 25) = 280$

11. 4 washing machines = 34160 \rightarrow 9 machines = $9 \times (34160 \div 4) = 76860$

12. Man walks 90 km in 5 days \rightarrow 11 days = $11 \times (90 \div 5) = 198$ km

13. Car consumes 5 L \rightarrow 85 km \rightarrow 17 L = $17 \times (85 \div 5) = 289$ km

14. 15 men \rightarrow 12 days \rightarrow 20 men \rightarrow $12 \times 15 / 20 = 9$ days

15. 18 men \rightarrow 25 days \rightarrow 10 days \rightarrow $18 \times 25 / 10 = 45$ men

16. 32 men \rightarrow 24 days \rightarrow 16 days $\rightarrow 32 \times 24 / 16 = 48$ men

17. 160 men \rightarrow 27 days \rightarrow 180 men $\rightarrow 4320 / 180 = 24$ days

Exercise 8.3 – Speed, Price, and Work Problems

1. MCQs

(i) 10 shirts \times 500 = 5000 \rightarrow (b) 5000

(ii) 5 persons \times 2 days \rightarrow 10 persons \rightarrow 1 day

(iii) 3 kg rice \rightarrow 20 persons \rightarrow 50 persons $\rightarrow 3 \times 50 \div 20 = 7.5$ kg

2. Train 360 km in 3 h 20 min \rightarrow speed = 108 km/h \rightarrow 90 km $\rightarrow 90 \div 108 = 0.833$ h = 50 min

3. Oranges 24 for ₹40 \rightarrow ₹50 $\rightarrow 24 \times 50 / 40 = 30$ oranges

4. 1 dozen pens = ₹60 \rightarrow 60 pens = $60 \div 12 \times 60 = 300$

5. 15 oranges = ₹40 \rightarrow 36 oranges = $36 \times 40 / 15 = 96$

6. 38 kg rice = 275.50 \rightarrow per kg = $275.50 / 38 = 7.25$ \rightarrow 20 kg = 145

7. 12 kg wheat = 108 \rightarrow per kg = 9 \rightarrow ₹144 \rightarrow 16 kg

8. 10 persons \times 20 hours = 200 man-hours \rightarrow 5 hours $\rightarrow 200 / 5 = 40$ persons

9. Rakesh 10 pens = 55 \rightarrow 5.5 per pen, Raju 2 pens = 13 \rightarrow 6.5 \rightarrow Raju paid more

10. First bus 36 km/0.5 h = 72 km/h, Second 120/2 = 60 km/h \rightarrow First is faster

Exercise 8.4 – Speed, Distance, Time

1. Karan runs 200 m in 20 s \rightarrow speed = $200/20 = 10$ m/s \rightarrow 36 km/h
 2. Bus 428.5 km in 8 h $\rightarrow 428.5/8 = 53.56$ km/h
 3. Car 26 km/h \rightarrow 5 h \rightarrow distance = $26 \times 5 = 130$ km
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Miscellaneous Exercise

1. Ratios

- (i) 50:11.50 \rightarrow 1:23
- (ii) 40.500 kg:20.400 kg \rightarrow 135:68
- (iii) 45 cm:2 m \rightarrow 9:40
- (iv) 15 L:500 ml \rightarrow 30:1

2. Divide 980 in ratio 3:11 \rightarrow Charan = 210, Pawan = 770

3. 25 chocolates in ratio 3:2 \rightarrow Ratan = 15, Aadil = 10

4. 35 pencils in ratio 2:1:4 \rightarrow Raja=10, Mahesh=5, Naresh=20

5. Angles ratio 2:3:4 \rightarrow 40° , 60° , 80°

6. Perimeter 24 cm, sides ratio 2:3:1 \rightarrow 8 cm, 12 cm, 4 cm

7. Which ratio is greater?

- (i) 5:4 vs 7:6 \rightarrow 5:4 greater
- (ii) 3:5 vs 5:6 \rightarrow 5:6 greater

8. Find x

- (i) Missing info
- (ii) $x:78 = 8:4 \rightarrow x = 156$

9. Girls:Boys = 3:4, Boys = 560 \rightarrow Girls = 420

10. 8 inkpots = 96 \rightarrow 27 inkpots = 324

11. Are 3,2,21,14 in proportion? \rightarrow Yes
12. Incomes $A:B = 5:7$, $A = 4200 \rightarrow B = 5880$
13. 8 men \rightarrow 9 days \rightarrow 12 days \rightarrow 6 men
14. 15 men \rightarrow 50 days \rightarrow 10 days \rightarrow 75 men
15. Car 548 km in 9 h \rightarrow 60.89 km/h
16. Coding: PROPORTION = 6850586954
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Chapter Test – Step-by-Step Solutions

1. Ratios:

- (i) $50.40:40.80 \rightarrow 5040:4080 \rightarrow 6:5$
- (ii) $50 \text{ kg}:45 \text{ kg} \rightarrow 50:45 \rightarrow 10:9$

2. Divide 720 in ratio $4:3:2 \rightarrow$ total parts=9 \rightarrow one part=80 \rightarrow
 $A=320, B=240, C=160$

3. Angles ratio $5:3:1 \rightarrow$ sum=9 \rightarrow one part= $180/9=20 \rightarrow$
angles= $100^\circ, 60^\circ, 20^\circ$

4. Smaller ratio:

- (i) $5:7$ vs $3:4 \rightarrow 5/7=0.714, 3/4=0.75 \rightarrow 5:7$ smaller
- (ii) $3:8$ vs $7:20 \rightarrow 3/8=0.375, 7/20=0.35 \rightarrow 7:20$ smaller

5. Income ₹8250, Savings ₹2250 \rightarrow Expenditure=6000

- (i) Savings:Expenditure= $2250:6000=3:8$
- (ii) Savings:Income= $2250:8250=3:11$
- (iii) Income:Expenditure= $8250:6000=11:8$

6. Copper:Gold= $3:4$, Total=10.5 \rightarrow Gold= $4/7 \times 10.5=6 \text{ kg}$

7. Cyclist A= $72/9=8 \text{ km/h}$, B= $165/15=11 \text{ km/h} \rightarrow$ ratio=8:11

8. $5:3::20:x \rightarrow x=12$

9. Male:Female= $7:9$, Male=28 \rightarrow Female= $28 \times 9/7=36$

10. Rama:Shama=5:9, Rama=4500 \rightarrow Shama= $4500 \times 9/5=8100$

11. Rod 7 m \rightarrow 63 kg \rightarrow 11 m $\rightarrow 63 \times 11/7=99$ kg

12. 11 fans=10373 \rightarrow 8 fans= $10373 \times 8/11=7544.73$

13. Car 270 km/15 L \rightarrow 9 L $\rightarrow 270 \times 9/15=162$ km

14. 32 men \rightarrow 18 days \rightarrow 24 days $\rightarrow 32 \times 18/24=24$ men

15. Train 60 km/h \rightarrow 9 h \rightarrow distance=540 km \rightarrow 45 km/h \rightarrow time= $540/45=12$ h

16. 1 dozen pens=50 \rightarrow 72 pens $\rightarrow 72/12 \times 50=300$

17. Train 738 km/9 h \rightarrow speed= $738/9=82$ km/h