

A: matrix([1, 2, 3], [4, 5, 6], [7, 8, 9]);

$$\begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{pmatrix}$$

A[1, 2]; /* Accesses the element in the first row and second column (2) */

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B: matrix([9, 8, 7], [6, 5, 4], [3, 2, 1]);

C: A + B;

D: A - B;

$$\begin{pmatrix} 9 & 8 & 7 \\ 6 & 5 & 4 \\ 3 & 2 & 1 \end{pmatrix}$$

$$\begin{pmatrix} 10 & 10 & 10 \\ 10 & 10 & 10 \\ 10 & 10 & 10 \end{pmatrix}$$

$$\begin{pmatrix} -8 & -6 & -4 \\ -2 & 0 & 2 \\ 4 & 6 & 8 \end{pmatrix}$$

E: A . B;

$$\begin{pmatrix} 30 & 24 & 18 \\ 84 & 69 & 54 \\ 138 & 114 & 90 \end{pmatrix}$$

F: 2 * A; /* Multiplies every element of A by 2 */

$$\begin{pmatrix} 2 & 4 & 6 \\ 8 & 10 & 12 \\ 14 & 16 & 18 \end{pmatrix}$$

G: transpose(A);

$$\begin{pmatrix} 1 & 4 & 7 \\ 2 & 5 & 8 \\ 3 & 6 & 9 \end{pmatrix}$$

;

I: ident(3); /* Creates a 3x3 identity matrix */

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

matrix_size(A); /* Returns [3, 3] for a 3x3 matrix */

[3,3]

row1: row(A, 1); /* Extracts the first row [1, 2, 3] */

$$\begin{pmatrix} 1 & 2 & 3 \end{pmatrix}$$

col1: col(A, 1); /* Extracts the first column [1, 4, 7] */

$$\begin{pmatrix} 1 \\ 4 \\ 7 \end{pmatrix}$$

aug_AB: augment(A, B);

$$\text{augment}\left(\begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{pmatrix}, \begin{pmatrix} 9 & 8 & 7 \\ 6 & 5 & 4 \\ 3 & 2 & 1 \end{pmatrix}\right)$$

app_AB: append(A, B);

$$\begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \\ 9 & 8 & 7 \\ 6 & 5 & 4 \\ 3 & 2 & 1 \end{pmatrix}$$

zero_mat: zeromatrix(3, 3); /* Creates a 3x3 zero matrix */

$$\begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

A_squared: A^^2; /* Computes A * A */

A_cubed: A^^3; /* Computes A * A * A */

$$\begin{pmatrix} 30 & 36 & 42 \\ 66 & 81 & 96 \\ 102 & 126 & 150 \end{pmatrix} \quad \begin{pmatrix} 468 & 576 & 684 \\ 1062 & 1305 & 1548 \\ 1656 & 2034 & 2412 \end{pmatrix}$$

/* Define the coefficient matrix and right-hand side vector */

M: **matrix**([**2**, **1**, **-1**], [**-3**, **-1**, **2**], [**-2**, **1**, **2**]);

B: **matrix**([**8**], [**-11**], [**-3**]);

/* Solve the linear system */

linsolve([**2**·**x** + **y** - **z** = **8**, **-3**·**x** - **y** + **2**·**z** = **-11**, **-2**·**x** + **y** + **2**·**z** = **-3**], [**x**, **y**, **z**]);

$$\begin{pmatrix} 2 & 1 & -1 \\ -3 & -1 & 2 \\ -2 & 1 & 2 \end{pmatrix} \begin{pmatrix} 8 \\ -11 \\ -3 \end{pmatrix} \quad [x=2, y=3, z=-1]$$

/* Define the augmented matrix */

A: **matrix**([**2**, **1**, **-1**, **8**], [**-3**, **-1**, **2**, **-11**], [**-2**, **1**, **2**, **-3**]);

/* Perform elimination */

A_echelon: **echelon**(**A**);

/* Display the matrix in reduced row-echelon form */

A_echelon;

$$\begin{pmatrix} 2 & 1 & -1 & 8 \\ -3 & -1 & 2 & -11 \\ -2 & 1 & 2 & -3 \end{pmatrix} \quad \begin{pmatrix} 1 & \frac{1}{2} & -\left(\frac{1}{2}\right) & 4 \\ 0 & 1 & 1 & 2 \\ 0 & 0 & 1 & -1 \end{pmatrix}$$

$$\begin{pmatrix} 1 & \frac{1}{2} & -\left(\frac{1}{2}\right) & 4 \\ 0 & 1 & 1 & 2 \\ 0 & 0 & 1 & -1 \end{pmatrix}$$

triangularize(**A**);

$$\begin{pmatrix} 2 & 1 & -1 & 8 \\ 0 & 1 & 1 & 2 \\ 0 & 0 & -1 & 1 \end{pmatrix}$$

B2: **matrix**([**1**, **1**, **1**], [**1**, **1**, **1**], [**1**, **1**, **1**])

;

$$\begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix}$$

rank(B2);

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