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import numpy as np
import matplotlib.pyplot as plt

# Function and derivative definitions
def function(x):
    # Defines the equation:  $f(x) = e^x - (4 - x^2)$ 
    return np.exp(x) - (4 - x**2)

def derivative(x):
    # Defines the derivative of  $f(x)$ :  $f'(x) = e^x + 2x$ 
    return np.exp(x) + 2*x

# Initial guess and tolerance for Newton's method
initial_guess = -1 # Starting point for Newton's method
tolerance = 1e-6 # Stopping criterion for iteration
max_iterations = 100 # Maximum allowed iterations

# Newton's Method implementation
x_current = initial_guess # Initialize current approximation
for iteration in range(max_iterations):
    # Compute the next approximation using Newton's formula
    x_new = x_current - function(x_current) / derivative(x_current)
    # Check if the difference between consecutive approximations is within tolerance
    if abs(x_new - x_current) < tolerance:
        break
    # Update the current approximation
    x_current = x_new

# Generate data for the plot
x_range = np.linspace(-3, 3, 400) # Create a range of x values for plotting
y_exp = np.exp(x_range) # Calculate y-values for the exponential function
y_parabola = 4 - x_range**2 # Calculate y-values for the parabola function

# Plotting the functions and the approximated root
plt.figure(figsize=(8, 6)) # Set the figure size
plt.plot(x_range, y_exp, label=r'$e^x$', color='blue') # Plot the exponential function
plt.plot(x_range, y_parabola, label=r'$4 - x^2$', color='orange') # Plot the parabola
plt.scatter(x_current, np.exp(x_current), color='red', label='Root Approximation', zorder=5) # Mark the approximated root

# Adding labels and details
plt.axhline(0, color='black', linewidth=0.5, linestyle='--') # Add a horizontal line at y=0
plt.axvline(x=x_current, color='green', linestyle='--', label='Root Location') # Add a vertical line at the approximated root
plt.title('Finding the Negative Root:  $e^x = 4 - x^2$ ', fontsize=14) # Title of the plot
plt.xlabel('x', fontsize=12) # Label for x-axis
plt.ylabel('y', fontsize=12) # Label for y-axis
plt.grid(True, linestyle='--', alpha=0.7) # Add a grid with dashed lines
plt.legend(fontsize=10) # Add a legend with specified font size

# Display the plot
plt.show() # Render the plot

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