

1. [25 pts] Implement the following four functions (at the same time) using only three half adders. Complements of the variables and logic levels 0 and 1 are NOT available.

$$A = X \oplus Y \oplus Z$$

$$B = X'YZ + XY'Z$$

$$C = X'Z + XYZ' + Y'Z$$

$$D = XYZ$$

2. [25 pts] Design a circuit that takes 2's complement of any four-bit number by using only 3 *XOR* and minimum number of *OR* gates.

3. [25 pts] Design an even parity check circuit with 3 binary inputs, which counts the number of 1's in its input. If the number of 1's are even, then the output of the circuit is 1. If the number of 1s are odd, then the output is 0.
- [12 pts] Implement in minimal Sum-of-Product form.
 - [13 pts] Implement in minimal Product-of-Sum form.