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# Natural Language to First Order Logic

## NatLog Meeting 9/29/2022

—— NatLog Group Meeting status ——

[The Google slides link to Natural Language to First Order logic-Sep-29-2022](#)

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# Changes to dataset for NL to FOL translation

For each hypothesis, FOLIO has multiple premises (1 to 3 or more)

So I selected all premises and corresponding FOL statements and used that as input for testing Encoder decoder model.

# Results from Stanford Logic API for FOL

## Using First Order Logic parser from StanfordNLP

### Logic

```
In [ ]: prem_fol = "Czech(miroslov) ^ ChoralConductor(miroslov) ^ Specialize(miroslov, renaissance) ^ Specialize(miroslov, baroque)"
pred = read_expr(r'\N F x.(N(\G H.H(G(F)))(\u.x)(\u.u))')

miroslov = read_expr(r'miroslov')
baroque = read_expr(r'baroque')
renaissance = read_expr(r'renaissance')
Czech = read_expr(r'Czech(miroslov)')
ChoralConductor = read_expr(r'ChoralConductor(miroslov)')
Specialize1 = read_expr(r'Specialize(miroslov, renaissance)')
Specialize2 = read_expr(r'Specialize(miroslov, baroque)')
Czech(miroslov).simplify()

Out [ ]: <ApplicationExpression Czech(miroslov,miroslov)>

In [ ]: print((Czech(miroslov) & ChoralConductor(miroslov)).simplify())

(Czech(miroslov,miroslov) & ChoralConductor(miroslov,miroslov))

In [ ]: print((Czech(miroslov) & ChoralConductor(miroslov) & Specialize1(miroslov, renaissance) & Specialize2(miroslov, baroque)).simplify())

(Czech(miroslov,miroslov) & ChoralConductor(miroslov,miroslov) & Specialize(miroslov,renaissance,miroslov,renaissance) & Specialize(miroslov,baroque,miroslov,baroque))
```

# Results from Z3 Solver

## Z3 solver with axioms and functions

### Boolean Logic

First we define BoolSort functions. \ We define an Object of type DeclareSort. \ Then we define constants - which could remain constant in this world. \

#### Proof explanation

Miroslav is from Czech republic and is a ChoralConductor who specializes in renaissance genre and in baroque music. By Classic proof by refutation: We prove that if x is not a ChoralConductor will make this entire logical And operation invalid. \ So each of the Czech(x), ChoralConductor(x), Specialize(x, renaissance), Specialize(x, baroque) will have to be true for the "Czech(miroslav)  $\wedge$  ChoralConductor(miroslav)  $\wedge$  Specialize(miroslav, renaissance)  $\wedge$  Specialize(miroslav, baroque)" to be true.

So z3 proves this by proof by refutation.

```
In [ ]:
prem_fol = "Czech(miroslav)  $\wedge$  ChoralConductor(miroslav)  $\wedge$  Specialize(miroslav, renaissance)  $\wedge$  Specialize(miroslav, baroque)"
Object = DeclareSort('Object')

Czech = Function('Czech', Object, BoolSort())
ChoralConductor = Function('ChoralConductor', Object, BoolSort())
Specialize = Function('Specialize', Object, Object, BoolSort())
miroslav = Const('miroslav', Object)
renaissance = Const('renaissance', Object)
baroque = Const('baroque', Object)
axioms1 = And(Czech(miroslav), ChoralConductor(miroslav))
axioms2 = And(Czech(miroslav), ChoralConductor(miroslav), Specialize(miroslav, renaissance), Specialize(miroslav, baroque))

s = Solver()
s.add(axioms1)
s.add(axioms2)
print(s.check()) # prints sat so axioms are coherent

print(s.model())

print(s.check()) # prints sat so this conjunction is satisfied

sat
[miroslav = Object!val10,
 baroque = Object!val12,
 renaissance = Object!val11,
 ChoralConductor = [else -> True],
 Czech = [else -> True],
 Specialize = [else -> True]]
sat
```

#### Proof explanation

For All x if x is ChoralConductor then this implies x is musician. By Classic proof by refutation: We prove that if x is not a ChoralConductor then x is not a musician. \ The else (the negation) should have to be false. \ So we know true case valid.

```
In [ ]:
premise_fol = "Vx (ChoralConductor(x)  $\Rightarrow$  Musician(x))"
Object = DeclareSort('Object')

ChoralConductor = Function('ChoralConductor', Object, BoolSort())
Musician = Function('Musician', Object, BoolSort())
x = Const('x', Object)

axioms1 = ForAll(x, Implies(ChoralConductor(x), Musician(x)))

s = Solver()
s.add(axioms1)
print(s.check()) # prints sat so axioms are coherent

print(s.model())

print(s.check()) # prints sat so this conjunction is satisfied

sat
[ChoralConductor = [else -> False],
 Musician = [else -> False]]
sat
```

## Using Encoder Decoder T5 model without Fine tuning

Test BLEU score : 0.00064

# of Test samples: 513

```
...                                     ...
```

1021	BornIn(ailtonsilva, y1995) ∧ CommonlyKnownAs(a...	<pad> Natürliche Sprache bis zu First Order Lo...
1022	FootballPlayer(ailton) ∧ LoanedTo(ailton, braga)	<pad> Natürliche Sprache zu der Logik der Erst...
1023	Brazilian(aitonsilva) ∧ Footballplayer(ailton...	<pad> Natürliche Sprache zu der Logik der erst...
1024	FootballClub(nautico) ∧ FootballClub(braga)	<pad> Natürliche Sprache zu First Order Logik...
1025	FootballClub(fluminense)	<pad> Natürliche Sprache zu erster Ordnung Log...

1026 rows x 2 columns

```
[ ] df = results.to_pandas()
df.loc[0,'prediction']

'<pad> Natürliche Sprache zu erster Ordnung Logik: Wenn Menschen häufig in schulischen Tale
<pad><pad><pad><pad><pad><pad><pad><pad><pad><pad><pad><pad><pad><pad><pad><pad><pad><pad>'

[ ] test.column_names

['nl', 'fol']
```

Now evaluate the quality of translations using the BLEU metric:

```
from datasets import load_metric

metric = load_metric('sacrebleu')

for r in results:
    prediction = r['prediction']
    reference = [r['reference']]
    metric.add(prediction=prediction, reference=reference)

metric.compute()
```

```
{'score': 0.0006430186886559712,
'counts': [297, 0, 0, 0],
'totals': [229797, 228771, 227745, 226719],
'precisions': [0.1292445071084479,
0.00021855917052423601,
0.00010977189400425915,
5.513432927985745e-05],
'bp': 1.0,
'sys_len': 229797,
'ref_len': 12947}
```

# Baseline : Finetuned Encoder Decoder T5 model

Evaluation BLEU score : 46.69

# of Evaluation samples: 513

Test BLEU score: 0.011

```
1 metrics = train_result.metrics
  metrics['train_samples'] = len(train_dataset)

  trainer.log_metrics('train', metrics)
  trainer.save_metrics('train', metrics)
  trainer.save_state()

  ***** train metrics *****
  epoch                =      3.0
  total_flos           = 117836GF
  train_loss           =      0.124
  train_runtime        = 0:04:52.00
  train_samples        =     5227
  train_samples_per_second = 53.702
  train_steps_per_second  = 13.428

Now evaluate:

[ ] # https://discuss.huggingface.co/t/evaluation-results-metric-during-training-is-different-from-the-evaluation-results-at-the-end/15401

  metrics = trainer.evaluate(
    max_length=max_target_length,
    num_beams=num_beams,
    metric_key_prefix='eval',
  )

  metrics['eval_samples'] = len(eval_dataset)

  trainer.log_metrics('eval', metrics)
  trainer.save_metrics('eval', metrics)

  ***** Running Evaluation *****
  Num examples = 513
  Batch size = 4
  [ 67/129 00:19 < 00:18, 3.32 it/s]
  [129/129 00:35]

  ***** eval metrics *****
  epoch                =      3.0
  eval_bleu            = 46.6949
  eval_loss            =      0.2484
  eval_runtime         = 0:00:35.96
  eval_samples         =     513
  eval_samples_per_second = 14.264
  eval_steps_per_second  =      3.587
```

# Observations

Removes first letter of the function in FOL statement:

**NL statement:** *People either perform in school talent shows often or are inactive and disinterested members of their community.*

**Original FOL statements:**

$\forall x (\text{Combine}(\text{Talent}, \text{Shows})(x) \rightarrow \text{Not}(\text{disinterested}(x)))$  "Engaged"

$\forall x (\text{TalentShows}(x) \vee \text{Inactive}(x))$

**Predicted FOL statement:**

$\forall x (\text{AlentShows}(x) \rightarrow \text{ingrijireInactive}(x))$

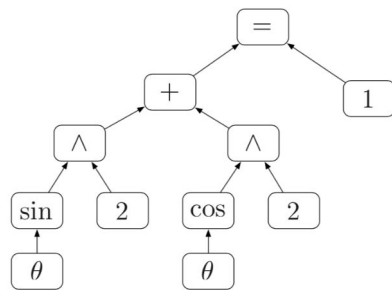
$\forall x (\text{AlentShows}(x) \rightarrow \text{ingrijireInactive}(x))$

**Next steps to explore**

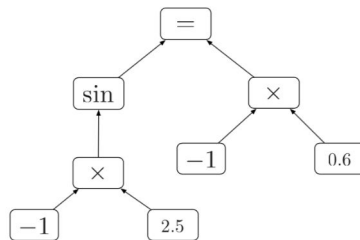


# Neural Math

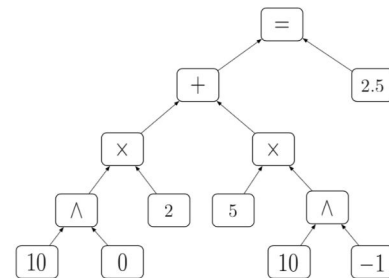
1. Weighted tree LSTMs for Math equations and evaluation for formal evaluation  
<https://openreview.net/forum?id=Hksj2WWAW&notId=Hksj2WWAW>
2. Terminal symbols use one-hot encoding
3. Each equation LHS (Left Hand Side) and RHS (Right Hand Side) is represented as an LSTM. And weighted LSTM training and evaluation for values.



$$\sin^2(\theta) + \cos^2(\theta) = 1$$



$$\sin(-2.5) = -0.6$$



decimal tree for 2.5

# Dependency Parsing

Dependency parsing for FOL and NL using Hierarchical Tree LSTMs:

<https://aclanthology.org/Q16-1032/>

# Exploring Neural Models for Parsing Natural Language into First-Order Logic

1. <https://arxiv.org/pdf/2002.06544.pdf>
2. *"...Encoder decoder model by introducing a variable alignment mechanism that enables it to align variables across predicates in the predicted FOL. We further show the effectiveness of predicting the category of FOL entity - Unary, Binary, Variables and Scoped Entities, at each decoder step as an auxiliary task on improving the consistency of generated FOL. We perform rigorous evaluations and extensive ablations."*
3. Lambda Dependency-based Compositional Semantics
4. They used sequence to sequence transduction:  
[https://www.cs.toronto.edu/~graves/seq\\_trans\\_slides.pdf](https://www.cs.toronto.edu/~graves/seq_trans_slides.pdf)
- 5.

# Siamese Recurrent networks

Siamese recurrent networks (using LSTM + GRUs) :

<https://arxiv.org/abs/1906.00180>

# Approach to explore similar to converting NL to SQL statements or SPARQL

Alignment between NL and FOL - approach to explore (similar to converting NL to SQL statements or SPARQL which have different symbols/commands)