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Chapter 29 Check Point Questions

Section 29.2

▼ 29.2.1

For the code `WeightedEdge edge = new WeightedEdge(1, 2, 3.5)`, what is `edge.u`, `edge.v`, and `edge.weight`?

`edge.u` is 1, `edge.v` is 2, and `edge.weight` is 3.5

Hide Answer

▼ 29.2.2

What is the output of the following code?

```
List<WeightedEdge> list = new ArrayList<>();  
list.add(new WeightedEdge(1, 2, 3.5));  
list.add(new WeightedEdge(2, 3, 4.5));  
WeightedEdge e = java.util.Collections.max(list);  
System.out.println(e.u);  
System.out.println(e.v);  
System.out.println(e.weight);
```

The output is

2
3
4.5

Hide Answer

Section 29.3

▼ 29.3.1

If a priority queue is used to store weighted edges, what is the output of the following code?

```
PriorityQueue<WeightedEdge> q = new PriorityQueue<>();  
q.offer(new WeightedEdge(1, 2, 3.5));  
q.offer(new WeightedEdge(1, 6, 6.5));  
q.offer(new WeightedEdge(1, 7, 1.5));  
System.out.println(q.poll().weight);  
System.out.println(q.poll().weight);  
System.out.println(q.poll().weight);
```

The output is

1.5
3.5
6.5

Hide Answer

▼ 29.3.2

If a priority queue is used to store weighted edges, what is wrong in the following code? Fix it and show the output.

```
List<PriorityQueue<WeightedEdge>> queues = new ArrayList<>();
queues.get(0).offer(new WeightedEdge(0, 2, 3.5));
queues.get(0).offer(new WeightedEdge(0, 6, 6.5));
queues.get(0).offer(new WeightedEdge(0, 7, 1.5));
queues.get(1).offer(new WeightedEdge(1, 0, 3.5));
queues.get(1).offer(new WeightedEdge(1, 5, 8.5));
queues.get(1).offer(new WeightedEdge(1, 8, 19.5));
System.out.println(queues.get(0).peek()
    .compareTo(queues.get(1).peek()));
```

The code is wrong because there is no `queues.get(0)`. You need to first create and add a queue into `queues` using the following statements:

```
queues.add(new PriorityQueue<WeightedEdge>());
queues.add(new PriorityQueue<WeightedEdge>());
```

After the fix, the output is -1.

Hide Answer

▼ 29.3.3

Show the output of the following code.

```
public class Test {
    public static void main(String[] args) throws Exception {
        WeightedGraph<Character> graph = new WeightedGraph<>();
        graph.addVertex('U');
        graph.addVertex('V');
        int indexForU = graph.getIndex('U');
        int indexForV = graph.getIndex('V');
        System.out.println("indexForU is " + indexForU);
        System.out.println("indexForV is " + indexForV);
        graph.addEdge(indexForU, indexForV, 2.5);
        System.out.println("Degree of U is " +
            graph.getDegree(indexForU));
        System.out.println("Degree of V is " +
            graph.getDegree(indexForV));
        System.out.println("Weight of UV is " +
            graph.getWeight(indexForU, indexForV));
    }
}
```

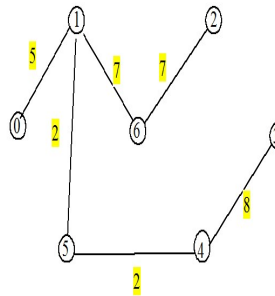
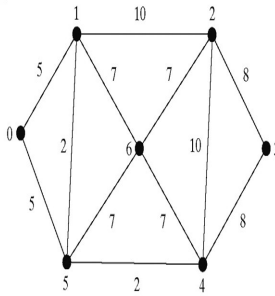
indexForU is 0
 indexForV is 1
 Degree of U is 1
 Degree of V is 0
 Weight of UV is 2.5

Hide Answer

Section 29.4

▼ 29.4.1

Find a minimum spanning tree for the following graph.



Hide Answer

▼ 29.4.2

Is a minimum spanning tree unique if all edges have different weights?

Yes.

Hide Answer

▼ 29.4.3

If you use an adjacency matrix to represent weighted edges, what will be the time complexity for Prim's algorithm?

$O(n^2 \log n)$, n is the number of vertices.

Hide Answer

▼ 29.4.4

What happens to the `getMinimumSpanningTree()` method in `WeightedGraph` if the graph is not connected? Verify your answer by writing a test program that creates an unconnected graph and invokes the `getMinimumSpanningTree()` method.

Line 95 in `WeightedGraph.java`, the loop

```
while (T.size() < numberOfVertices) {
```

continues if `T.size() < numberOfVertices`. If the graph is not connected, the `v` will be set to -1 in line 98, if no edges are found to connect vertices between `T` and `V - T`. In this case, the statement

```
if (v != -1)
    T.add(v); // Add a new vertex to the tree
else
    break; // The tree is not connected, a partial MST is found
```

causes the while loop in line 95 to end.

Hide Answer

▼ 29.4.5

Show the output of the following code:

```
public class Test {
    public static void main(String[] args) {
        WeightedGraph<Character> graph = new WeightedGraph<>();
        graph.addVertex('U');
        graph.addVertex('V');
        graph.addVertex('X');
        int indexForU = graph.getIndex('U');
        int indexForV = graph.getIndex('V');
        int indexForX = graph.getIndex('X');
        System.out.println("indexForU is " + indexForU);
        System.out.println("indexForV is " + indexForV);
        System.out.println("indexForX is " + indexForV);
        graph.addEdge(indexForU, indexForV, 3.5);
        graph.addEdge(indexForV, indexForU, 3.5);
        graph.addEdge(indexForU, indexForX, 2.1);
        graph.addEdge(indexForX, indexForU, 2.1);
        graph.addEdge(indexForV, indexForX, 3.1);
        graph.addEdge(indexForX, indexForV, 3.1);
        WeightedGraph<Character>.MST mst
            = graph.getMinimumSpanningTree();
        graph.printWeightedEdges();
        System.out.println(mst.getTotalWeight());
        mst.printTree();
    }
}
```

```
indexForU is 0
indexForV is 1
indexForX is 1
U (0): (0, 1, 3.5) (0, 2, 2.1)
V (1): (1, 0, 3.5) (1, 2, 3.1)
X (2): (2, 0, 2.1) (2, 1, 3.1)
5.2
Root is: U
Edges: (X, V) (U, X)
```

Hide Answer

Section 29.5

▼ 29.5.1

Trace Dijkstra's algorithm for finding shortest paths from Boston to all other cities in Figure 29.1.

See the text.

Hide Answer

▼ 29.5.2

Is a shortest path between two vertices unique if all edges have different weights?

No.

Hide Answer

▼ 29.5.3

If you use an adjacency matrix to represent weighted edges, what would be the time complexity for Dijkstra's algorithm?

$O(n^2 \log n)$, n is the number of vertices.

Hide Answer

▼ 29.5.4

What happens to the `getShortestPath()` method in `WeightedGraph` if the source vertex cannot reach all vertices in the graph? Verify your answer by writing a test program that creates an unconnected graph and invoke the `getShortestPath()` method.

Line 185 in `WeightedGraph.java`, the loop

```
while (T.size() < numberOfVertices) {
```

continues if `T.size() < numberOfVertices`. If the graph is not connected, the `v` is set to `-1` in line 185, if no edges are found to connect vertices between `T` and `V - T`, `-1` will add to `T` in line 208. The statement

```
if (v != -1)
    T.add(v); // Add a new vertex to the tree
else
    break; // The tree is not connected, a partial MST is found
```

causes the while loop in line 185 to end.

Hide Answer

▼ 29.5.5

If there is no path from vertex `v` to the source vertex, what will be `cost[v]`?

`cost[v]` will be infinity.

Hide Answer

▼ 29.5.6

Assume that the graph is connected; will the `getShortestPath` method find the shortest paths correctly if lines 159-161 in `WeightedGraph` are deleted?

No. `cost[i]` will be zero for `i`.

Hide Answer

▼ 29.5.7

Show the output of the following code:

```
public class Test {
    public static void main(String[] args) {
        WeightedGraph<Character> graph = new WeightedGraph<>();
        graph.addVertex('U');
```

```

graph.addVertex('V');
graph.addVertex('X');
int indexForU = graph.getIndex('U');
int indexForV = graph.getIndex('V');
int indexForX = graph.getIndex('X');
System.out.println("indexForU is " + indexForU);
System.out.println("indexForV is " + indexForV);
System.out.println("indexForX is " + indexForV);
graph.addEdge(indexForU, indexForV, 3.5);
graph.addEdge(indexForV, indexForU, 3.5);
graph.addEdge(indexForU, indexForX, 2.1);
graph.addEdge(indexForX, indexForU, 2.1);
graph.addEdge(indexForV, indexForX, 3.1);
graph.addEdge(indexForX, indexForV, 3.1);
WeightedGraph<Character>.ShortestPathTree tree =
    graph.getShortestPath(1);
graph.printWeightedEdges();
tree.printTree();
}
}

```

```

indexForU is 0
indexForV is 1
indexForX is 1
U (0): (0, 1, 3.5) (0, 2, 2.1)
V (1): (1, 0, 3.5) (1, 2, 3.1)
X (2): (2, 0, 2.1) (2, 1, 3.1)
Root is: V
Edges: (V, U) (V, X)

```

Hide Answer

Section 29.6

▼ 29.6.1

Why is the tree data field in NineTailModel in Listing 28.13 defined protected?

The tree data field in NineTailModel is accessed in WeightedTailModel. A new tree is created in WeightedTailModel.

Hide Answer

▼ 29.6.2

How are the nodes created for the graph in WeightedNineTailModel?

See the text.

Hide Answer

▼ 29.6.3

How are the edges created for the graph in WeightedNineTailModel?

See the text.

Hide Answer