

Probability Distributions in R

Continuous

Distributions	root
beta	beta
Cauchy	cauchy
chi-square	chisq
exponential	exp
F	f
gamma	gamma
normal	norm
student's t	t
uniform	unif
Weibull	weibull

In the continuous case, **droot** returns the density, **proot** a cumulative probability, **qroot** a quantile, **rroot** a random number.

Probability

If X follows $N(0, 1)$, then to find $P(X \leq 1.25) = \Phi(1.25)$, that is, the amount of area under the standard normal density curve to the left of $x = 1.25$,

```
> pnorm(1.25)
```

By default, the **norm** function assumes $\mu = 0, \sigma = 1$ (that is, you are working with the standard normal distribution). For other means and standard deviations, specify them in the argument. For example, if $X \sim N(\mu = 2, \sigma = 3)$, then to find $F(2.8) = P(X \leq 2.8)$,

```
> pnorm(2.8, 2, 3)
```

If X follows a chi-square distribution with 25 degrees of freedom then to compute $F(13.9) = P(X \leq 13.9)$,

```
> pchisq(13.9, 25)
```

If X follows an exponential distribution with parameter $\lambda = 10$, then to compute $P(X > 4)$,

```
> 1 - pexp(4, 10)
```

or

```
> pexp(4, 10, lower.tail=FALSE)
```

If T follows a t-distribution with 7 degrees of freedom, then to find the probability that $T \leq 3.9$, type

```
> pt(3.9, 7) # pt(t-value, d.f)
```

Quantiles

To find the 25th percentile, that is, the value q such that $P(X \leq q) = .25$ for X from $N(0, 1)$,

```
> qnorm(.25)
[1] -0.6744898
```

In other words, the amount of area under the pdf to the left of $x = -0.6744$ is 0.25. Or, if F denotes the cdf of the distribution, then $F^{-1}(0.25) = -0.6744$.

The .75 quantile for $N(2, 3)$ can be found by

```
> qnorm(.75, 2, 3)
[1] 4.023469
```

In other words, the amount of area under the density curve and to the left of $x = 4.023469$ is .75, or if F denotes the cdf, then $F^{-1}(0.75) = 4.023469$.

For T from a t-distribution with 13 degrees of freedom, to find value t such that $P(T > t) = .025$, which is equivalent to $F(t) = P(T \leq t) = 0.975$, type

```
> qt(.975, 13)
```

Random numbers

To generate 100 random numbers from the normal distribution $N(0, 1)$, type

```
> rnorm(100)
> x <- rnorm(100)
> hist(x)
```

Ten random numbers from the chi-square distribution with 23 degrees of freedom,

```
> rchisq(10, 23)
```

Plotting the density curve (pdf)

To plot the pdf for $N(0, 1)$ for $-3 \leq x \leq 3$, use the `curve` function with the pdf `dnorm` provided as an argument.

```
> curve(dnorm(x), from = -3, to = 3)
> w <- rnorm(50) # random sample from N(0,1)
> hist(w, freq = TRUE) # scale to area 1
> curve(dnorm(x), add = TRUE) # impose normal density
```

```
> hist(w, freq = TRUE, ylim = c(0, .5)) # widen y-axis range
> curve(dnorm(x), add=TRUE)
```

To plot the pdf for the chi-square distribution with 14 degrees of freedom,

```
> curve(dchisq(x, 14), from = 0, to = 20)
```

Discrete

Distribution	root
binomial	binom
geometric	geom
hypergeometric	hyper
negative binomial	nbinom
Poisson	pois

Preface each of the above roots with either **d**, **p**, **q** or **r**.

droot is the probability mass function so returns a probability, **proot** returns a cumulative probability (cmf), and **qroot** returns a quantile, and **rroot** returns a random number.

The quantile function is the inverse of the CDF, $F(t) = P(X \leq t) = \sum_{k \leq t} P(X = k)$.

Example Binomial

Suppose you have a biased coin that has a probability of 0.8 of coming up heads.

The probability of getting 5 heads in 16 tosses of this coin is

```
> dbinom(5,16, .8)
```

Check this answer by calculating directly

$$\binom{16}{5} .8^5 \cdot .2^{11},$$

```
> choose(16,5)*.8^5*.2^11
```

The probability of getting at most 5 heads in 16 tosses is

```
> pbinom(5,16,.8)
```

In other words, `pbinom(5, 16, .8)` is computing: `dbinom(0,16,.8)+dbinom(1,16,.8)+dbinom(2,16,.8)+dbinom(3,16,.8)+dbinom(4,16,.8)+dbinom(5,16,.8)`

The 0.25 quantile is

```
> qbinom(.25,16,.8)
```

```
[1] 12
```

This is the smallest number of successes such that the probability of at most this many successes is greater than or equal to .25.

Check this:

```
> pbinom(11, 16, .8)
> pbinom(12, 16, .8)
```

Example (cont.) Geometric

Find the probability of getting the first head on the fourth toss. This is the geometric distribution. The arguments to `geom` are `geom(failures, p)`.

```
> dgeom(3, .8)
```

The probability that the first head occurs on one of the first four tosses (that is, on the first, second, third or fourth toss) is

```
> pgeom(3, .8)
```

Example Poisson

Suppose a certain region of California experiences about 5 earthquakes a year. Assume occurrences follow a Poisson distribution. What is the probability of 3 earthquakes in a given year?

Here $\lambda = 5$

```
> dpois(3,5)
```

Check the answer:

```
> 5^3*exp(-5)/(3*2)
```

Random numbers

To generate random numbers from a particular distribution, preface the root name with an `r`.

For example, we continue our previous example of a biased coin with $p = .8$ of coming up heads. Toss this coin 25 times. The command `rbinom(1,25,.8)` will return a random number of successes.

```
> rbinom(1,25,.8)
```

Now, let's run this experiment 10 times (that is, we do 10 sets of tossing a coin 25 times) and record the number of successes.

```
> set.seed(0)
```

This sets the seed for the random number generator so that we all get the same results.

```
> heads <- rbinom(10, 25, .8)
> heads
```

```
[1] 17 19 21 18 20 18 22 18 22 17  #output will vary
```

In the first experiment of tossing the coin 25 times, 17 heads occurred. In the second experiment of tossing the coin 25 times, 19 heads occurred, etc.

```
> table(heads)
```

```
> barplot(table(heads))
```

Repeat the above, except now run the experiment 100 times.

```
> heads2 <- rbinom(100, 25, .8)
```