

|                  |  |  |                  |   |   |   |   |   |
|------------------|--|--|------------------|---|---|---|---|---|
|                  |  |  | Game Grid/States |   |   |   |   |   |
| Allowed Movement |  |  | 3                | ↔ | 4 | ↔ | 5 |   |
| Up               |  |  | ↓                |   |   | ↓ |   |   |
| Down             |  |  | ↑                |   | 1 | ↑ | 2 | ↑ |
| Left             |  |  | ↔                |   | ↔ | ↔ | ↔ |   |
| Right            |  |  | ↔                |   | ↔ | ↔ | ↔ |   |

| Adjacency Matrix |   |   |   |   |
|------------------|---|---|---|---|
|                  | 0 | 1 | 2 | 3 |
| 0                |   |   |   |   |
| 1                |   |   |   |   |
| 2                |   |   |   |   |
| 3                |   |   |   |   |
| 4                |   |   |   |   |
| 5                |   |   |   |   |

```
def generate_adjacency_matrix(grid_size):
    num_states = grid_size[0] * grid_size[1]
    adjacency_matrix = np.zeros((num_states, 4), dtype=int) - 1
    for i in range(num_states):
        row = i // grid_size[1]
        col = i % grid_size[1]
        if row > 0:
            adjacency_matrix[i, 0] = i - grid_size[1] # Down
        if row < grid_size[0] - 1:
            adjacency_matrix[i, 1] = i + grid_size[1] # Up
        if col > 0:
            adjacency_matrix[i, 2] = i - 1 # Left
        if col < grid_size[1] - 1:
            adjacency_matrix[i, 3] = i + 1 # Right
    return adjacency_matrix
```

