

# Advanced Analytics Capstone CSDA 1050

# **Sprint 3 Report**

Housing Rent Prices for 2-bedroom apartments in the major Canadian Cities

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#### Introduction:

We will be evaluating the cost of living for renters in the major Canadian Cities. This information will provide a better understanding of what drives rent costs. The focus will be to find fact-based insights on meaningful patterns in the housing rental market. Owning a home is an ideal need for young adults in Canada and the social pressures along with increasing opportunities for profit, were driving the growth of the market, causing first time home buyers to struggle in finding a place to live at a reasonable price. Which forces most young adults to rent rather than owning their own home.

#### About the data set:

The datasets were gathered from third-party external source from the Canadian Mortgage and Housing Corporation website. The datasets include Average Income After Tax Renters, Average Rent 2 Bedrooms and Housing market Indicators. They can be found using these links below:

https://www.cmhc-schl.gc.ca/en/data-and-research/data-tables/real-average-after-tax-

https://www.cmhc-schl.gc.ca/en/data-and-research/data-tables/average-rent-2-bedroom-

https://www.cmhc-schl.gc.ca/en/data-and-research/data-tables/housing-market-indicators

# **Objective:**

Our objective is to determine the most cost-effective price for renter's base on their household income. Even though factors, such as rise in unemployment rates increase in some of Canada's major cities, housing prices are still rising. Renting has started to consume over 50% of the average household's monthly income. We conclude that with increases in household debt, stagnant wages and expected rises in interest rates, a decline is inevitable. These factors are also forcing home buyers sell their homes and go back to renting.

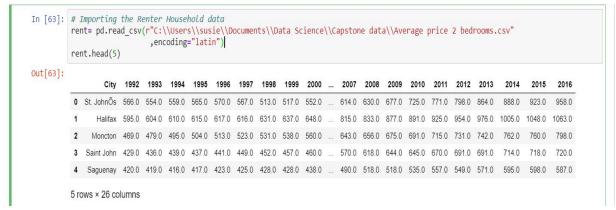
#### **Overview**

Our analysis has been carefully explained to its simplest form to accommodate stakeholders that may not understand various analytical terms. Each step was carefully explained and visualized.

#### **Loading some of the Libraries**

```
In [1]: # Loading packages
   import pandas as pd
   import numpy as np
   import matplotlib.pyplot as plt
   import seaborn as sns
   import os
   from pandas import read_table
   from scipy.stats import norm
   %matplotlib inline
```

# Preparing the Average price per 2 bedrooms data



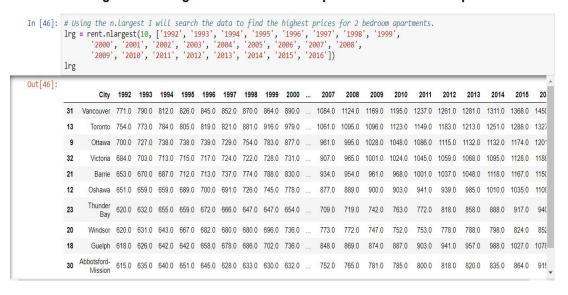
5 rows × 26 columns

Looking at the data above, it seems, we only have mostly numeric values only one column has objects.

#### **Rent data Columns**

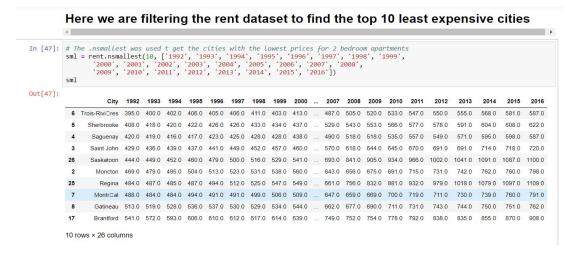
#### Top 10 most expensive cities

#### Finding the to 10 hightest and lowest rent prices for 2 bedroom apartments.



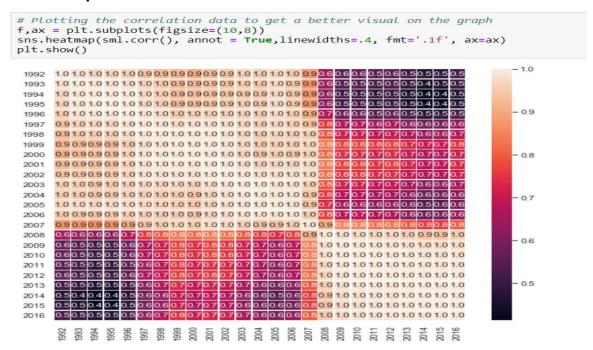
From the output above the most expensive cities are Vancouver, Toronto, Ottawa, Victoria, Barrie, Oshawa, Thunder Bay, Windsor, Guelph and Abbotsford Mission.

#### The top 10 least expensive cities



The Top 10 least expensive cities are Tros-Rivers, Sherbrooke, Saguenay, Saint John, Saskatoon, Moncton, Regina, Montreal, Ga and Bradford. We will be focusing on the least expensive rent prices since our research question is to figure out the most livable cities.

# Correlation plot for the sml data values



In the correlation heatmap it seems as though 2001, 2002,1999 and 2000 have the strongest correlation.

#### Renaming the variables that will be used for modelling

```
In [6]: #Renaming 2001 column name
sml.rename(columns={'2001': 'price1'}, inplace=True)

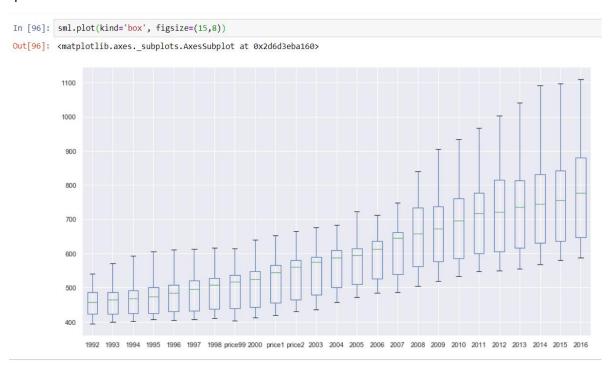
In [8]: # Renameing 2007 column name
sml.rename(columns={'2002': 'price2'}, inplace=True)

In [9]: # Renameing 2007 column name
sml.rename(columns={'1999': 'price99'}, inplace=True)
```

These variables are much easier to work with if they are renamed, because the column names were numbers, we might run into issues later if they aren't renamed before hand.

# **Checking for outliers**

There are certain things, if not done in the EDA phase, can affect further statistical Machine Learning modelling. One of them is finding outliers. We will be using Box plots to help us detect outliers. Box plot is a method for graphically depicting groups of numerical data through their quartiles. They may also have lines extending vertically or horizontally from the indicating variability outside the upper and lower quartiles.



Looking at the graph above there seem to several outliers in the sml dataset from 2008 to 2016 we will take a closer look below.

# **Identifying the outliers**

Before we try to understand whether to ignore the outliers or not, we need to know ways to identify them. Mostly we will try to see visualization methods rather mathematical. Outliers may be plotted as individual points.

Above plot shows 2008 has one point between 800 to 850, the outlier is not included in the box of other observation nowhere near the quartiles. This we will remove, and the same process will be repeated to clean any outlier in the dataset.

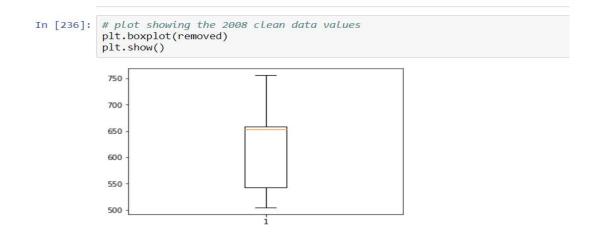
# **Removing Outlier**

```
[234]:
        # Identifyng and removig the outliers from the 2008 values
        from numpy import percentile
        # calculate interquartile range
        q25, q75 = percentile(data, 25), percentile(data, 75)
        iqr = q75 - q25
        print('Percentiles: 25th=%.3f, 75th=%.3f, IQR=%.3f' % (q25, q75, iqr))
        # calculate the outlier cutoff
        cut_off = iqr * 1.5
        lower, upper = q25 - cut off, q75 + cut off
        # identify outliers
        outliers = [x \text{ for } x \text{ in data if } x < lower \text{ or } x > upper]
        print('Identified outliers: %d' % len(outliers))
        # remove outliers
        removed = [x for x in data if x >= lower and x <= upper]
        print('Non-outlier observations: %d' % len(removed))
       Percentiles: 25th=561.750, 75th=672.500, IQR=110.750
       Identified outliers: 1
       Non-outlier observations: 9
```

In the 2008 feature there are 9 non-outlier and one outlier that was identified.

#### Clean data

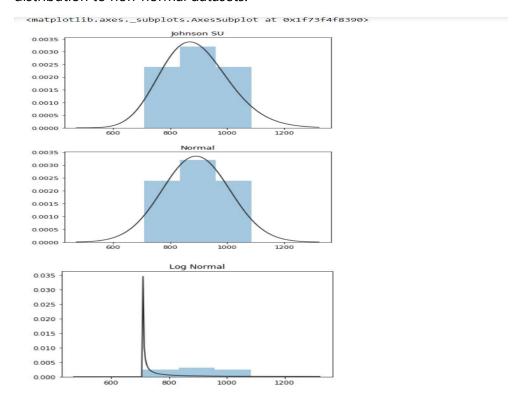
Here is the result of the cleaned data after the outlier was removed if there is an outlier it will plotted as point in boxplot, but other population will be grouped together and display as box. Let's try and see it ourselves.



Even though there was an outlier it seems as though it didn't affected the mean price it remained the same before and after the outlier was removed at around 650.

#### **Johnson SU distribution plot**

The mu and sigma are the mean and the standard deviation of the distribution. The Johnson plot is a transformation of the normal distribution the Johnson SU was developed to in order to apply the established methods and theory of the normal distribution to non-normal datasets.



### **Regression Plot**

The line of best fit is calculated by minimizing the ordinary least squares error function, that Seaborn module does automatically using the regplot function. The shaded area around the line represents 95% confidence intervals. When running a regression,

statwing automatically calculates and plots residuals to help understand and improve the regression model.

```
# Regression plot
               fig, ax = plt.subplots(1,2)
sns.regplot('price1','price2',sml, ax=ax[0], scatter_kws={'alpha':0.4})
sns.regplot('price2','price99',sml,ax=ax[1], scatter_kws={'alpha':0.4})
Out[18]: <matplotlib.axes._subplots.AxesSubplot at 0x218db4cc9b0>
                    600
                                                           550
                    575
                                                           525
                    550
                                                           500
                    525
                   500
                                                           475
                    475
                                                           450
                    450
                                                           425
                    425
                                                           400
                               450
                                        500
                                                  550
                                                                   450
                                                                            500
                                                                                     550
                                                                                             600
```

As you can see from the above plots our data is very clean the points on the model are almost perfect.

#### **Residual Plot**

```
# visualizing the residuals by creating residual plots . fig, ax = plt.subplots(1,2) \,
In [20]:
                ax[0] = sns.residplot('price1', 'price2', sml,ax=ax[0], scatter_kws={'alpha':0.4})
ax[0].set_ylabel('price1 residual')
ax[1]=sns.residplot('price2', 'price99', sml,ax=ax[1], scatter_kws={'alpha':0.4})
                ax[1].set_ylabel('price2 residual')
Out[20]: Text(0, 0.5, 'price2 residual')
                                                                10
                        6
                                                                 5
                  price1 residual
                                                           price2 residual
                       2
                                                                 0
                                                                -5
                      -2
                      -6
                                450
                                          500
                                                                                 500
                                                                                           550
```

The points in the residual plot represent the difference between the sample (y) and the predicted value (y'). Residuals that are greater than zero are points that are underestimated by the model and residuals less than zero are points that are overestimated by the model.

# **Creating a fitted linear model**

```
In [259]: # create a fitted model
import statsmodels.formula.api as smf
model = smf.ols(formula='price1 ~ price2', data=sml).fit()

# print the coefficients
lm1.params

Out[259]: Intercept 12.191914
    price2 0.952636
    dtype: float64

In []: # The price for rent seem to have increased by $95.26 from 2001 to 2002
```

The price for rent seem to have increased by \$95.26 from 2001 to 2002

#### **P Values**

P values represents the probability that the coefficient is actually zero.

# **R Square**

```
In [232]: # print the R-squared value for the model
lm1.rsquared

Out[232]: 0.9907773400504103

In [238]: # create a fitted model with all three features
lm2 = smf.ols(formula='price1 ~ price2 + price98 + price99', data=sml).fit()

# print the coefficients
lm2.params

Out[238]: Intercept -18.816983
price2 0.440564
price98 0.169263
price99 0.444685
dtype: float64
```

Price for rent seem to have decreased by \$18.82 when evaluated againts price2, 98, and 99.

#### **Model creation**

Adding 3 more models to do our evaluation which includes price1(2001) and price2(2002). Model2 includes price98(1998) and price99(1999) as well as model 3 which includes price1, price2, price98, price99, and price00(2000).

```
In [113]: # Next we'll want to fit a linear regression model. We need to choose variables that we think we'll be good predictors for the d
# This can be done by checking the correlation(s) between variables, on what variables are good predictors of y.

import statsmodels.api as sm
    X = sml["pricet"]
    y = sml["pricet"]

# Note the difference in argument order
model = sm.015(y, x).fit()
predictions = model.predict(X) # make the predictions by the model

In [116]: # # Next we'll want to fit a linear regression model by adding a constant.
    X = sml["price9s"] ## X usually means our input variables (or independent variables)
    y = sml["price9s"] ## X usually means our output/dependent variable
    X = sm.add_constant(X) ## Let's add an intercept (beta_0) to our model.

# Note the difference in argument order
model2 = sm.015(y, X).fit() ## sm.015(output, input)
predictions = model2.predict(X)

In [125]: # set input and output variables to use in regression model
    x = sm.[['price2', 'price98', 'price99', 'price00']]
    y = sml['price1']

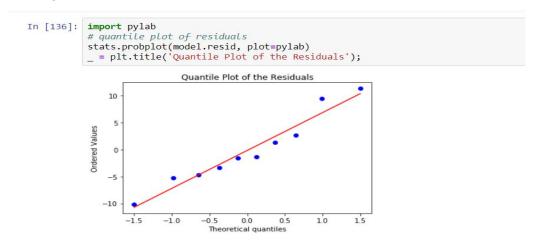
# add intercept to input variable
    x = sm.add_constant(x)

# fit regression model, using statsmodels GLM uses a different method but gives the same results
#model = sm.015(y, x).fit()
model3 = sm.015(y, x).fit()
```

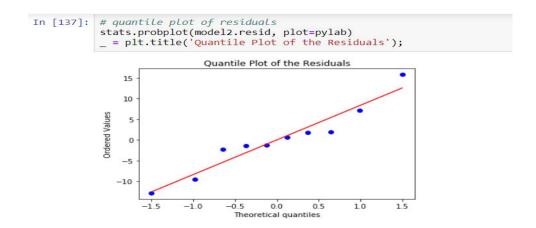
# Quantile residual plots for all 3 models

Quantile regression models is the relation between a set of predictor variables and specific percentiles or quantiles of the response variable. It specifies changes in the quantiles of the response. Quantile regression makes no assumptions about the distribution of the residuals.

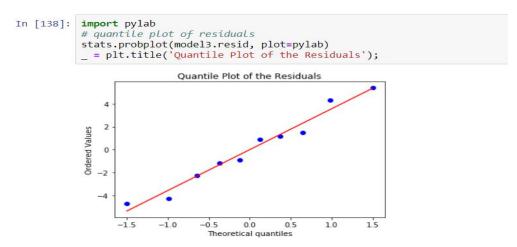
# Plotting Model1



# Plotting Model2



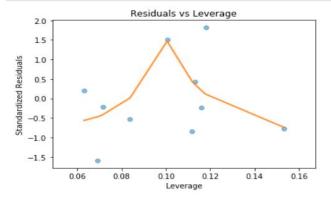
# Plotting Model3

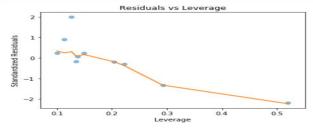


From the quantile plots above all 3 plots are close to perfect but model3 seem to be the most fitted plot.

# Normalizing the residuals for the models

The standardized residual is a measure of the strength of the difference between observed and expected values. It's a measure of how significant your cells are to the chi-square value. When you compare the cells, the standardized residual makes it easy to see which cells are contributing the most to the value, and which are contributing the least.





If the residual is less than -2, the cell's observed frequency is less than the expected frequency. Greater than 2 and the observed frequency is greater than the expected frequency.

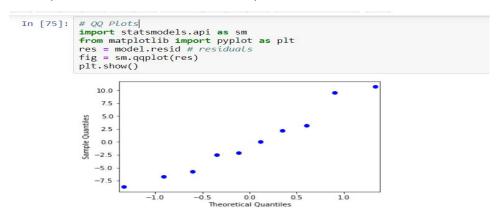
# **Model3 Partial Regression Variable plots**

Partial regression plots attempt to show the effect of adding an additional variable to the model given that one or more independent variables are already in the model. Partial regression plots are formed by:

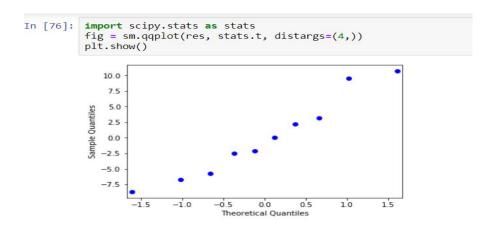
```
In [126]: # model3 variable plots
               fig = plt.figure(figsize=(8,8))
               fig = sm.graphics.plot partregress grid(model3, fig=fig)
      e(price1 | X)
                                                                  e(price1 | X)
           0
          -2
                                                  0.05
                                                                                                                15
            -0.15
                     -0.10
                               -0.05
                                         0.00
                                                                           -10
                                                                                                         10
                                                                                           e(price2 | X)
                                                                     5.0
                                                                     2.5
      e(price1 | X)
           2
                                                                e(price1 | X)
                                                                     0.0
           0
                                                                   -25
          -2
                                                                   -5.0
                                   ó
                                                                             -5.0
                                                                                   -2.5
                                                                                            0.0
                                                                                                  2.5
                                                                                          e(price99 | X)
                              e(price98 | X)
      e(price1 | X)
           2
           0
                                     2.5
                                              5.0
                              e(price00 | X)
```

# **QQ Plots**

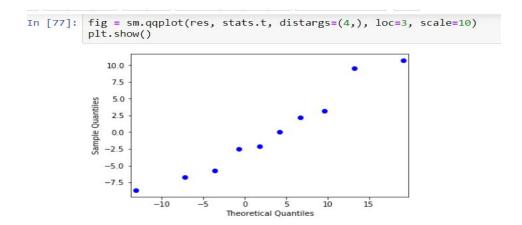
The Q-Q plot, or quantile-quantile plot, is a graphical tool to help us assess if a set of data plausibly came from some theoretical distribution such as a Normal or exponential. For example, if we run a statistical analysis that assumes our dependent variable is Normally distributed, we can use a Normal Q-Q plot to check that assumption. It's just a visual check, not an air-tight proof, so it is somewhat subjective. But it allows us to see at-a-glance if our assumption is plausible, and if not, how the assumption is violated and what data points contribute to the violation.



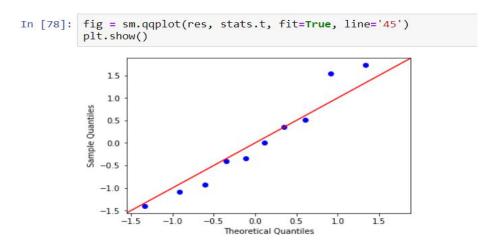
Qq plot of the residuals against quantiles of t-distribution with 4 degrees of freedom



Qqplot against same as above, but with mean 3 and std 10



Automatically determine parameters for t distribution including the loc and scale:



# **Probability Class**

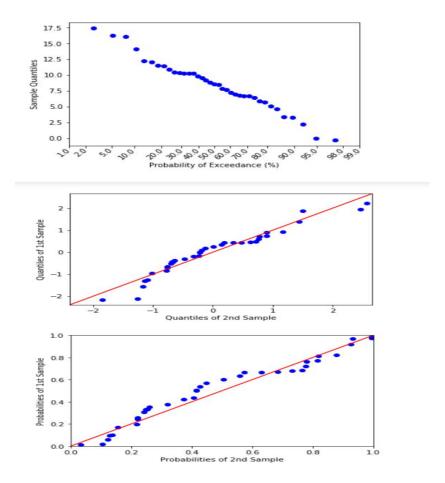
Randomly generate data from a standard Normal distribution and then find the quantiles.

```
In [79]: # |probPlot class
    x = np.random.normal(loc=8.25, scale=3.5, size=37)
    y = np.random.normal(loc=8.00, scale=3.25, size=37)
    pp_x = sm.ProbPlot(x, fit=True)
    pp_y = sm.ProbPlot(y, fit=True)

# probability of exceedance
fig2 = pp_x.probplot(exceed=True)

# compare x quantiles to y quantiles
fig3 = pp_x.qqplot(other=pp_y, line='45')

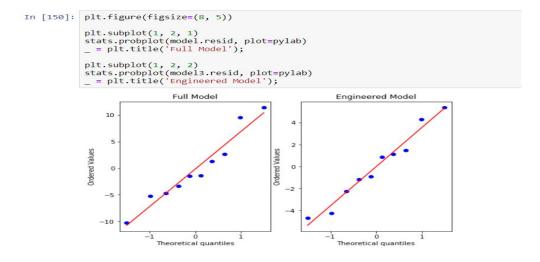
# same as above with probabilities/percentiles
fig4 = pp_x.ppplot(other=pp_y, line='45')
```

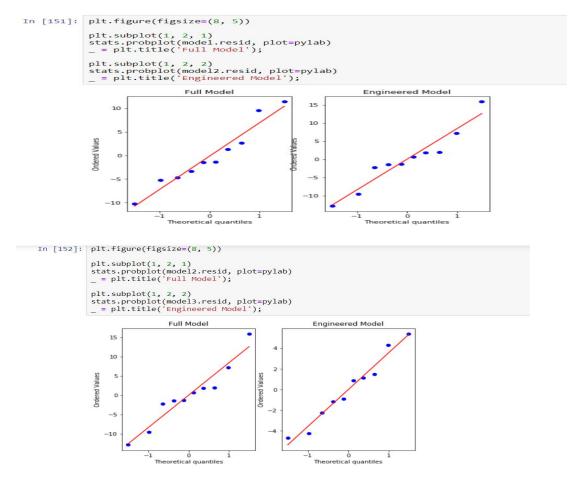


The results above is from the qq plot line 45

# **Probability Plots using all 3 models**

Generates a probability plot of sample data against the quantiles of a specified theoretical distribution the normal distribution by default. probplot optionally calculates a best-fit line for the data and plots the results.





# **Handling Categorical Features**

My goal to handel the categorical data was to be able to evaluate the cities, but when indexing there are only 2 categories which is 0 and 1. The error was spotted after creating the code because the dataset we are evaluating has 10 different cities it's challenging to evaluate the cities using indexing.

```
In [278]: # set a seed for reproducibility
np.random.seed(12345)

# create a Series of booleans in which roughly half are True
nums = np.random.rand(len(sml))
mask_large = nums > 0.5

# initially set Size to small, then change roughly half to be large
sml['City'] = 'Brantford'

# set a seed for reproducibility

# series.loc is a purely label-location based indexer for selection by label
sml.loc[mask_large, 'City'] = 'Sherbrooke'
sml.loc[mask_large, 'City'] = 'Sherbrooke'
sml.loc[mask_large, 'City'] = 'Saint John'
sml.loc[mask_large, 'City'] = 'Regina'
sml.loc[mask_large, 'City'] = 'Regina'
sml.loc[mask_large, 'City'] = 'Honoton'
sml.loc[mask_large, 'City'] = 'Honoton'
sml.loc[mask_large, 'City'] = 'Gatineau'
sml.loc[ma
```

# **Model Summary**

OLS stands for Ordinary Least Squares and the method "Least Squares" means that we're trying to fit a regression line that would minimize the square of distance from the regression line.

# Model1

n [281]:	<pre>print(model.summary())</pre>											
	OLS Regression Results											
	Dep. Variabl	e:	pric	e1	R-squa	red:		0.993				
	Model:		C	LS	Adj. R	-squared:		0.992				
	Method:		Least Squar	es	F-stat		1124.					
	Date:	F	ri, 30 Aug 20	19	Prob (	F-statistic)	:	6.84e-10				
	Time:		00:19:	32	Log-Li	kelihood:		-31.966				
	No. Observat	ions:		10	AIC:			67.93				
	Df Residuals	:		8	BIC:			68.54				
	Df Model:			1								
	Covariance T	ype:	nonrobu	ist	170 PK - 17-W - 270 A 92 PK - 270 A							
		coef	std err		 t	P> t	[0.025	0.975]				
	Intercept	12.1919	15.376	ø.	793	0.451	-23.265	47.648				
	price2	0.9526	0.028	33.	527	0.000	0.887	1.018				
	Omnibus:		0.8	36	===== Durbin	-Watson:		1.765				
	Prob(Omnibus	):	0.658		Jarque	-Bera (JB):		0.677				
	Skew:		-0.3	41	Prob()	B):		0.713				
	Kurtosis:		1.9	23	Cond.		3.98e+03					

### Model2

	OLS Regression Results												
Dep. Varia	======== ble:	pric	e99	R-squa	red:	-=======	0.985						
Model:					R-squared:		0.984						
Method:		Least Squa	res	F-stat		540.3							
Date:	Th	u, 29 Aug 2	019	Prob (	F-statistic	:):	1.25e-08						
Time:		13:43	:37	Log-Li	kelihood:		-34.456						
No. Observ	ations:		10	AIC:			72.91						
Df Residua	ls:	8		BIC:			73.52						
Df Model:			1										
Covariance	Type:	nonrob	ust										
	coef	std err		t	P> t	[0.025	0.975]						
const	-15.1279	22.280	-6	.679	0.516	-66.506	36.251						
price98	1.0405	0.045	23	.245	0.000	0.937	1.144						
Omnibus:		1.	===== 181	Durbin	 Watson:		1.262						
Prob(Omnib	Prob(Omnibus):		554	Jarque	-Bera (JB):		0.166						
Skew:		0.	309	Prob()	IB):		0.92						

# Model3

OLS Regression Results											
Dep. Varia		pric	e1 R-sa	======== uared:		0,998					
Model:	Jic.			R-squared:		0.996					
Method:		Least Squar				623.7					
Date:	Th	11 29 Aug 20	19 Proh	(F-statistic	-).	6.25e-07					
Time:		13:48:	34 100-	Likelihood:	-).	-25.656					
No. Observa	ations:		10 AIC:	LIKCIIII0001		61.31					
Df Residua			5 BIC:			62.82					
Df Model:			4			02.02					
Covariance	Type:	nonrobu	st								
	coef	std err	t	P> t	[0.025	0.975]					
const	-17.2774	21.621	-0.799	0.460	-72.857	38.302					
price2	0.4473	0.162	2.759	0.040	0.030	0.864					
price98	0.1458	0.320	0.455	0.668	-0.677	0.969					
price99	0.4239	0.315	1.344	0.237	-0.387	1.235					
price00	0.0330	0.353	0.094	0.929	-0.873	0.940					
========											
Omnibus:		0.2	48 Durb	in-Watson:		1.603					
Prob(Omnib	us):	0.8		ue-Bera (JB):		0.403					
Skew:		0.1		(JB):		0.818					
Kurtosis:		2.0	68 Cond	. No.		1.58e+04					

### **Model Interpretation**

**Omnibus/Prob(Omnibus)** is a test of the skewness and kurtosis of the residual. We hope to see a value close to zero which would indicate normalcy. The Prob (Omnibus) performs a statistical test indicating the probability that the residuals are normally distributed. We hope to see something close to 1 here. In this case Omnibus is relatively low and the Prob (Omnibus) is relatively high so the data is somewhat normal.

**Skew** is a measure of data symmetry. We want to see something close to zero, indicating the residual distribution is normal. This value also drives the Omnibus. This result has a small, and therefore good, skew.

**Kurtosis** is a measure of "peakiness", or curvature of the data. Higher peaks lead to greater Kurtosis. Greater Kurtosis can be interpreted as a tighter clustering of residuals around zero, implying a better model with few outliers.

**Durbin-Watson** tests for homoscedasticity characteristic. We hope to have a value between 1 and 2. In this case, the data is close, but within limits.

**Jarque-Bera (JB)/Prob(JB)** like the Omnibus test in that it tests both skew and kurtosis. We hope to see in this test a confirmation of the Omnibus test. In this case we do.

**Condition Number** This test measures the sensitivity of a function's output as compared to its input. When we have multicollinearity, we can expect much higher fluctuations to small changes in the data, hence, we hope to see a relatively small number, something below 30. In this case we are well below 30.

In looking at the data we see an okay though not great set of characteristics. This would indicate that the OLS approach has some validity, but we can probably do better with a nonlinear model.

# **Model1 Accuracy**

```
In [38]: from sklearn.dummy import DummyRegressor
    from sklearn.metrics import mean_absolute_error
    from sklearn.metrics import r2_score
    from sklearn.model_selection import train_test_split
    y = price1
    X = price2
    X_train,X_test,y_train,y_test = train_test_split(X,y,test_size=0.2,random_state=100)
    dummy_median = DummyRegressor(strategy='mean')
    dummy_regressor = dummy_median.fit(X_train,y_train)
    dummy_predicts = dummy_regressor.predict(X_test)
    print("Model Accuracy:", dummy_regressor.score(X_test,y_test)*100)
Model Accuracy: -565.585963182117
```

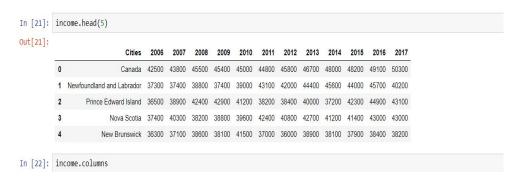
#### **Model Selection**

We have decided to use model3 as our final model as our final model. The reason is because model3 is making it's predictions working against several other variables.

# Loading in the income dataset

The income dataset is very similar to the rent dataset most of the same steps will be repeated to evaluate the income dataset that was used previously to evaluate the ren dataset. To avoid repetition we wont be explaining the outputs if they have already been explained previously.

# Looking at the head of the dataset



The income dataset is also made up of mostly numeric variable only one column has objects.

#### Income dataset columns

The dataset has 29 rows and 13 columns

#### Checking for missing data

There are no missing values in the income data

# Finding the cities with the lowest and highest income bracket

Top 10 cities with the highest income bracket

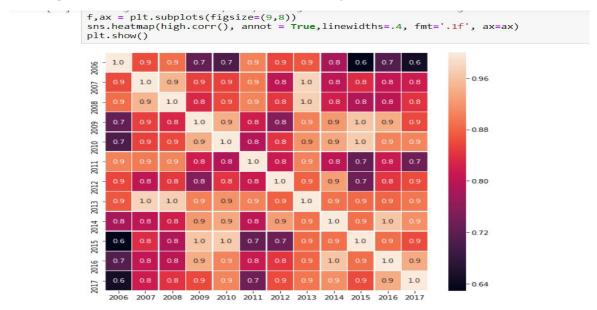
```
# Finding the hightest and lowest income ranges for top 10 cities.
         For the income dataset we will be forcusing on the the cities with the highest income bracket
In [ ]: # Filtering the data to find the cities with the lowest income
In [24]: # Using the n.smallest I will search the data to find cities with the highest income.
         low = income.nsmallest(10, ['2006', '2007', '2008', '2009', '2010', '2011', '2012',
                '2013', '2014', '2015', '2016', '2017'])
         low
Out[24]:
                       Cities 2006 2007 2008 2009 2010 2011 2012 2013 2014 2015 2016
                                                                                              2017
          17
                  Trois-Rivières 28700 36800 35800 36500 34800 34300 31300 34100 33600 31800 38500 36200
          14
                     Saguenay 31600 33100 33800 34100 35400 38400 37000 38200 33000 35400 37800 35100
          16
                    Sherbrooke 32900 34800 36100 35400 36600 34100 32600 35300 36200 41500 37700 35800
          11
                     St John's 34400 33000 38000 38300 40000 42300 42900 48400 49500 48300 45700 43400
          33
                       Regina 36000 44000 43700 44100 53400 51600 53300 53900 57600 53700 54600 53400
                 New Brunswick 36300 37100 38600 38100 41500 37000 36000 38900 38100 37900 38400 38200
          2 Prince Edward Island 36500 38900 42400 42900 41200 38200 38400 40000 37200 42300 44900 43100
                     Manitoba 36800 40000 38600 38000 39200 43600 41900 43700 45200 44100 45500 44400
          31
                   Thunder Bay 37100 38900 35000 39400 42800 36800 40500 39000 38800 45500 42800
                     Winnipeg 37200 40400 38100 37600 39300 42900 42100 42800 43700 42400 44600 43700
In [ ]: # Filtering the data to find the cities with the lowest income
```

### Top 10 cities with the highest income brackets

```
high
Out[23]:
                          Cities 2006 2007 2008 2009 2010 2011 2012 2013 2014 2015 2016 2017
                         Calgary 58000 65800 71000 61800 61700 63200 67300 70000 66500 63900 63400 66700
                         Alberta 54400 59800 62200 63300 62200 60000 64700 66000 67500 68600 64200 65400
         36
                       Edmonton 50100 58400 56900 66800 65800 58600 57900 61800 67800 72200 66800 66200
                       Abbotsford 49200 44000 42100 47700 42500 47000 53100 44900 55300 46800 55400 53900
         39
                        Victoria 47400 47300 47200 45300 38900 52900 45300 47000 45400 42700 54500 54900
                       Vancouver 46600 50600 47800 45800 49000 47300 54000 51100 51300 53000 54200
         10 British Columbia 46600 48400 48500 46000 46700 47900 50900 49600 49700 49500 53000 57700
         21 Ottawa - Gatineau (Québec) 46400 44800 42100 42200 38600 46600 37100 41800 37600 44400 44600 44200
         27 Kitchener 45800 50800 46100 50800 42900 45100 40200 49800 46300 54000 54000 55800
                         Toronto 45600 45700 50200 51900 51100 46200 47900 49200 53300 55500 55900 59800
```

For this dataset will be focusing on the cities with the highest income brackets. Usually cities with the highest income bracket would also have higher housing costs, but there are also other factors that affects the cost of living. The top 10 cities with the highest income brackets are Calgary, Alberta, Edmonton, Abbotsford, Victoria, British Columbia, Ottawa, Kitchener and Toronto.

# Plotting a heat map to find the most correlated years



In the correlation heatmap it seems as though 2013, 2010,2007, 2008and 2017 have the strongest correlation.

### Renaming the columns

```
In [183]:
            #Renaming 2013 column name
            high.rename(columns={'2013': 'income13'}, inplace=True)
            #Renaming 2015 column name
high.rename(columns={'2008': 'income8'}, inplace=True)
In [184]:
            #Renaming 2009 column name
high.rename(columns={'2007': 'income7'}, inplace=True)
In [185]:
In [187]:
            #Renaming 2009 column name
            high.rename(columns={'2010': 'income10'}, inplace=True)
            #Renaming 2009 column name
high.rename(columns={'2017': 'income17'}, inplace=True)
In [192]:
```

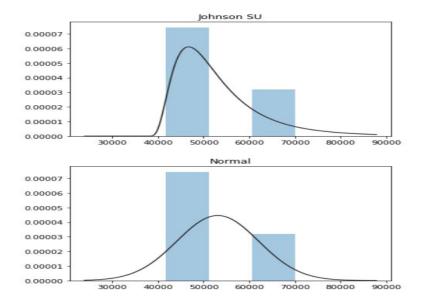
These variables are much easier to work with if they are renamed, because the column names were numbers, we might run into issues later if they aren't renamed before hand.

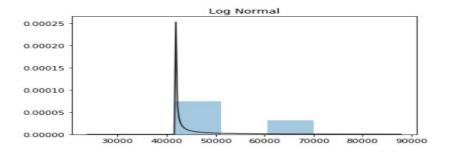
# Johnson SU distribution plot

The mu and sigma are the mean and the standard deviation of the distribution. The Johnson plot is a transformation of the normal distribution the Johnson SU was developed to in order to apply the established methods and theory of the normal distribution to non-normal datasets.

```
In [45]: # Johnson Su distribution plot for 2005
         import scipy.stats as st
         y = high[['income13']]
         plt.figure(1); plt.title('Johnson SU')
         sns.distplot(y, kde=False, fit=st.johnsonsu)
         plt.figure(2); plt.title('Normal')
          sns.distplot(y, kde=False, fit=st.norm)
         plt.figure(3); plt.title('Log Normal')
         sns.distplot(y, kde=False, fit=st.lognorm)
```







#### **Regression Plot**

The line of best fit is calculated by minimizing the ordinary least squares error function, that Seaborn module does automatically using the regplot function. The shaded area around the line represents 95% confidence intervals. When running a regression, statwing automatically calculates and plots residuals to help understand and improve the regression model.

```
In [47]:
              # Regression plot
               fig, ax = plt.subplots(1,2)
sns.regplot('income9','income13',high, ax=ax[0], scatter_kws={'alpha':0.4})
sns.regplot('income13','incom15',high,ax=ax[1], scatter_kws={'alpha':0.4})
Out[47]: <matplotlib.axes._subplots.AxesSubplot at 0x22551a04550>
                   75000
                                                         80000
                   70000
                   65000
                   60000
                                                        60000
                   55000
                   50000
                                                        50000
                   45000
                                                         40000
                   40000
                                      income9
                                                                          income13
```

### **Residual Plot**

The points in the residual plot represent the difference between the sample (y) and the predicted value (y'). Residuals that are greater than zero are points that are underestimated by the model and residuals less than zero are points that are overestimated by the model.

```
In [48]: # visualizing the residuals by creating residual plots . fig, ax = plt.subplots(1,2)
             ax[0]= sns.residplot('income9','income13', high,ax=ax[0], scatter_kws={'alpha':0.4})
ax[0].set_ylabel('income9 residual')
             ax[1]=sns.residplot('income13','incom15',high,ax=ax[1], scatter_kws={'alpha':0.4})
ax[1].set_ylabel('income13 residual')
Out[48]: Text(0, 0.5, 'income13 residual')
                  8000
                  6000
                                                    5000
                  4000
                                                    4000
                  2000
                                                   2000
                                                      0
                 -2000
                                                     000
                 -4000
                                                    000
                               50000
                                        60000
                                                               50000
                                                                       60000
                                                                                 70000
                                  income9
```

### **Model Creation**

# Creating a fitted linear model

Income seem to have increased by \$77.08 from 2008 to 2010

#### **P Values**

P values represents the probability that the coefficient is actually zero.

# **R Square**

```
In [289]: # print the R-squared value for the model
lm3.rsquared

Out[289]: 0.6854910493220028
```

```
In [291]: # create a fitted model with all three features
lm4 = smf.ols(formula='income7 ~ income8 + income10 + income17', data=high).fit()
# print the coefficients
lm4.params

Out[291]: Intercept 9418.317847
income8 0.635990
income10 0.933458
income17 0.130803
dtype: float64
```

# **Model Summary**

OLS stands for Ordinary Least Squares and the method "Least Squares" means that we're trying to fit a regression line that would minimize the square of distance from the regression line.

#### Lm3

[293]:	# Print out the statistics print(lm3.summary())  OLS Regression Results											
	Dep. Variab	ole:	income	8 R-squ	ared:		0.685					
	Model:		OL	S Adj.	Adj. R-squared: F-statistic: Prob (F-statistic): Log-Likelihood:							
	Method:		Least Square	es F-sta								
	Date:	F	ri, 30 Aug 201	19 Prob								
	Time:		14:07:1	L4 Log-L								
	No. Observa		1	LØ AIC:								
	Df Residual	Ls:		8 BIC:			201.2					
	Df Model:			1								
	Covariance	Type:	nonrobus	st								
		coef	std err	t	P> t	[0.025	0.975]					
	Intercept	1.261e+04	9174.635	1.374	0.207	-8548.700	3.38e+04					
	income10	0.7708	0.185	4.176	0.003	0.345	1.197					
	Omnibus:		6.86	7 Durbi	n-Watson:		2.147					
	Prob(Omnibu	ıs):	0.03	33 Jarqu	e-Bera (JB	):	2.586					
	Skew:		1.19	2 Prob(	Prob(JB): Cond. No.							
	Kurtosis:		3.95	60 Cond.								

#### LM4

	<pre>print(lm4.summary())</pre>												
	OLS Regression Results												
Dei	o. Variab	ole:	income	7 R-sau	ıared:		0.880						
	del:		OL		R-squared:		0.821 14.72 0.00357 -91.244						
Me	thod:		Least Square		tistic:								
Da	te:	F	ri, 30 Aug 201		(F-statisti	c):							
Tir	me:		14:22:5		ikelihood:								
No	. Observa	tions:	1	Ø AIC:			190.5						
Df	Residual	s:		6 BIC:			191.7						
Df	Model:			3									
Co	Covariance Type:		nonrobus	t									
==:		coef	std err	t	P> t	[0.025	0.975]						
In	tercept	9418.3178	8509.815	1.107	0.311	-1.14e+04	3.02e+04						
in	come8	0.6360	0.211	3.020	0.023	0.121	1.151						
in	come10	0.0335	0.224	0.150	0.886	-0.514	0.580						
in	come17	0.1308	0.268	0.487	0.643	-0.526	0.788						
Omi	ibus:		4.12	3 Durbi	n-Watson:		2.173						
Pro	ob(Omnibu	is):	0.12	7 Jarqu	ie-Bera (JB)	:	1.301						
	ew:	MORE CONTROL	-0.83				0.522						
Kui	rtosis:		3.57				8.54e+05						

The statistics in the last table are testing the normality of our data. If the Prob(Omnibus) is very small, and I took this to mean <.05 as this is standard statistical practice, then our data is probably not normal. This is a more precise way than graphing our data to determine if our data is normal.

Statsmodels also helps us determine which of our variables are statistically significant through the p-values. If our p-value is <.05, then that variable is statistically significant. This is a useful tool to tune your model. In the case of the iris data set we can put in all of our variables to determine which would be the best predictor.

# **Model Interpretation**

**Omnibus/Prob(Omnibus)** is a test of the skewness and kurtosis of the residual. We hope to see a value close to zero which would indicate normalcy. The Prob (Omnibus) performs a statistical test indicating the probability that the residuals are normally distributed. We hope to see something close to 1 here. In this case Omnibus is relatively low and the Prob (Omnibus) is relatively high so the data is somewhat normal.

**Skew** is a measure of data symmetry. We want to see something close to zero, indicating the residual distribution is normal. This value also drives the Omnibus. This result has a small, and therefore good, skew.

**Kurtosis** is a measure of "peakiness", or curvature of the data. Higher peaks lead to greater Kurtosis. Greater Kurtosis can be interpreted as a tighter clustering of residuals around zero, implying a better model with few outliers.

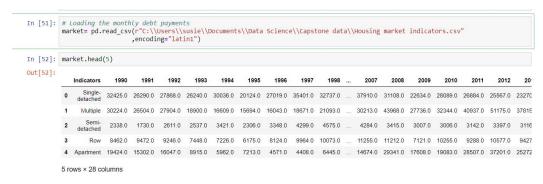
**Durbin-Watson** tests for homoscedasticity characteristic. We hope to have a value between 1 and 2. In this case, the data is close, but within limits.

**Jarque-Bera (JB)/Prob(JB)** like the Omnibus test in that it tests both skew and kurtosis. We hope to see in this test a confirmation of the Omnibus test. In this case we do.

**Condition Number** This test measures the sensitivity of a function's output as compared to its input. When we have multicollinearity, we can expect much higher fluctuations to small changes in the data, hence, we hope to see a relatively small number, something below 30. In this case we are well below 30.

In looking at the data we see an okay though not great set of characteristics. This would indicate that the OLS approach has some validity, but we can probably do better with a nonlinear model.

#### **Loading the market indicator dataset**



#### Missing values

```
In [27]: # We have to sure we set the data up in order
# lets take a look at the null values
print(market.isnull().sum().to_string())
                  Indicators
                  1990
1991
                  1992
                                            4
                  1994
                  1995
                                            4443333333222211111
                  1997
                  1998
1999
                  2000
                  2001
                  2002
                  2003
                  2004
                  2006
                  2007
                  2009
                  2011
                  2012
                  2014
                  2015
```

#### Plotting the missing values

```
In [54]: # Here we have a visual of the missing data
missing = market.isnull().sum()
missing = missing[missing > 0]
missing.sort_values(inplace=True)
missing.plot.bar()

Out[54]: <matplotlib.axes._subplots.AxesSubplot at 0x22551b2f7b8>
```

# Replacing missing values with NAN

```
In [104]: # Replacing missing values with NAN
import numpy
# mark zero values as missing or NaN
                          dataset = market.replace(0, numpy.NaN)
  In [105]: # print the first 20 rows of data
print(market.head(20))
                                                                                                                  Indicators
                                                                                                                                           32425.00
30224.00
2338.00
8462.00
                                                                                                                                                                 26290.00
26504.00
1730.00
9472.00
                                                                                                       Single-detached
                                                                                                           Multiple
Semi-detached
Row
                                                                                                                    Apartment
                                                                                                                                           19424.00
                                                                                                                                                                 15302.00
                                                                    Starts by intended market total
Homeownership freehold
                                                                                                                                            53341.00
28104.00
                                                                                                                                                                 46123.00
24813.00
                                                                                                                         Rental
                                                                                                                                            12158.00
                                                                                                                                                                 14519.00
                                              Rental
Homeownership condominium
Other co-op and unknown
Completions total
Residential Building Permits
Residential Building Permits $ thousands
Newly completed and unabsorbed homes
                                                                                                                                           11435.00
1644.00
80562.00
                                                                                                                                                                 4240.00
2551.00
59622.00
                         11
                                                                                                                                            61578.00
                                                                                                                                                                 60093.00
                                                                                                                                             6302.92
NaN
                                                                                                                                                                   6205.22
NaN
                                 Newly completed and unabsorbed nomes
Single and semi-detached
Row and apartment
Rental vacancy rate %
Rental availability rate %
Vacancy Rate Standard Spaces in Seniors Rental
New Housing Price Index % change
                         14
                                                                                                                                                     NaN
                                                                                                                                                                           NaN
                                                                                                                                                   NaN
1.40
NaN
                                                                                                                                                                         NaN
2.20
NaN
                                                                                                                                                      NaN
                                                                                                                                                                           NaN
                                                                                                                                                  -1.33
                                                                                                                                                                     -10.70
```

The top 10 highest market indicators

# The market indicators are what drives cost of living

t			rgest(10, 1998', '1 2007', '2	['1991', 999', '20	'1992', 100', '200	'1993', ' 1', '2002	1994', '1 '', '2003'	995', '19	996', '2005',	t affects	houssing	co.	st.			
55]:		Indicators	1990	1991	1992	1993	1994	1995	1996	1997	1998		2007	2008	2009	
	11	Residential Building Permits	61578.000	60093.000	54272.000	45480.000	49404.000	38610.000	46437.000	61070.000	59675.000		73271.000	70031.000	57653.000	(
	10	Completions total	80562.000	59622.000	63134.000	51130.000	49106.000	36278.000	40729.000	51297.000	48403.000		64139.000	67737.000	54900.000	
	5	Starts by intended market total	53341.000	46123.000	48693.000	38847.000	41560.000	31893.000	39512.000	49972.000	50088.000		62775.000	71923.000	47939.000	3.
	1	Multiple	30224.000	26504.000	27904.000	18900.000	16609.000	15694.000	16043.000	18671.000	21093.000		30213.000	43968.000	27736.000	
	0	Single-detached	32425.000	26290.000	27868.000	26240.000	30036.000	20124.000	27019.000	35401.000	32737.000		37910.000	31108.000	22634.000	
	6	Homeownership freehold	28104.000	24813.000	27917.000	26332.000	32516.000	22685.000	31634.000	40925.000	39649.000		45626.000	38613.000	28460.000	
	4	Apartment	19424.000	15302.000	16047.000	8915.000	5962.000	7213.000	4571.000	4408.000	6445.000		14674.000	29341.000	17608.000	
	7	Rental	12158.000	14519.000	13798.000	7974.000	4148.000	2884.000	1289.000	790.000	1181.000		2994.000	3867.000	4811.000	
:	29	Population on July 1 (thousands)	10295.832	10431.316	10572.205	10690.038	10819.146	10950.119	11082.903	11227.651	11365.901		12764.195	12882.625	12997.687	
	3	Row	8462.000	9472.000	9246.000	7448.000	7226.000	6175.000	8124.000	9964.000	10073.000		11255.000	11212.000	7121.000	

# The top 10 lowest market indicators

	'2006', ' '2015', '	nallest(10, 1998', '19 2007', '20	['1990', 999', '2000	'1991', ': 0', '2001	1992', '19 ', '2002',	93' 1994 '2003'		'1996', 05',	ects nous	ing cost.		
56]:	Indicators	1990	1991	1992	1993	1994	1995	1996	1997	1998	 2007	2008
19	New Housing Price Index % change	-1.330000	-10.700000	-3.21000	-1.710000	-0.280000	-0.020000	-1.010000	2.080000	2.500000	 2.620000	3.510000
31	Employment (% change)	-0.093768	-3.409135	-1.67844	0.105078	1.531143	1.722633	1.291011	2.416188	3.084520	1.443405	0.98987
16	Rental vacancy rate %	1.400000	2.200000	2.60000	2.700000	2.400000	2.300000	3.000000	2.800000	2.600000	3.300000	2.70000
23	Rental accommodation costs % change	3.990000	3.420000	2.92000	2.590000	2.090000	1.740000	1.440000	1.490000	1.260000	0.980000	0.85000
20	Consumer Price Index % change	4.820000	4.640000	1.02000	1.780000	0.050000	2.470000	1.520000	1.880000	0.930000	1.830000	2.27000
32	Unemployment rate %	6.200000	9.500000	10.80000	10.900000	9.600000	8.700000	9.000000	8.400000	7.200000	6.400000	6.60000
22	Owned accommodation costs % change	6.630000	2.110000	-0.43000	-0.840000	-1.390000	1.460000	-0.830000	-0.780000	0.400000	3.240000	3.64000
30	Labour force participation rate %	69.541667	68.533333	67.35000	66.683333	65.916667	65.475000	65.541667	65.733333	65.933333	67.750000	67.71666
24	Bachelor	417.000000	443.000000	456.00000	470.000000	479.000000	490.000000	496.000000	507.000000	531.000000	668.000000	691.00000
25	One bedroom	508.000000	538.000000	557.00000	573.000000	586.000000	601.000000	609.000000	616.000000	645.000000	797.000000	820.00000

# **Insights**

Abbotsford was the only city that appeared in 2 different search it appeared in the top 10 for the least expensive 2 bedroom rental price and in the top 10 in cities with the highest income bracket.

### **Conclusion**

This dataset was very chanlenging to work with. Not only was the dataset small but the dataset didn't have much variable options to work with. Year was being used againts year to do the evaluating which is not a realistic approach. This approach ended up giving all perfect plots for our modeling section. With the project being analysing rent prices it's evident that the price will go up every year. To be able to have a more solid model we suggest using a much more stronger dataset that has more variable options to work with.