hochschule mannheim

Understanding Eventual Consistency

MSI Presentation SS2014

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Introduction

" ...the storage system guarantees that if no new updates are made to the object, eventually all accesses will return the last updated value"
–W. Vogels (2009)

Interpretation 1

"When you read data[...], the response might not reflect the results of a recently completed write operation. The response might include some stale data. Consistency across all copies of the data is usually reached within a second; so if you repeat your read request after a short time, the response returns the latest data."

Interpretation 2

"This sort of system we term "single writer eventual consistency". So what are its properties?
(1) A client could read stale data.
(2) The client could see out-of-order write operations. [...] So this is our weakest form of consistency - eventually consistent with out of order reads in the short term."

DynamoDB Documentation

*"When you read data[...], the response might not reflect the results of a recently completed write operation. The response might include **some stale data**. Consistency across all copies of the data is **usually reached within a second**; so if you repeat your read request after a short time, the response returns the latest data."*

MongoDB Documentation

"This sort of system we term "single writer eventual consistency". So what are its properties?
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(2)The client could see out-of-order write operations.[...]
So this is our weakest form of consistency - eventually consistent with **out of order reads** *in the short term."*

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$\Rightarrow$ some sort of formalism is needed to define semantics of Eventual Consistency

Agenda

1 Replicated Data Types

2 Axiomatic Specification Framework

3 Consistency Strengthening Interfaces

4 Conclusion / Discussion

Replicated Data Types

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- two examples: Int Register **intreg**, Counter **ctr**

$$\mathrm{Op}_{\mathrm{ctr}} = \{\mathrm{rd}, \mathrm{inc}\}$$
$$\mathrm{Op}_{\mathrm{intreg}} = \{\mathrm{rd}, \mathrm{wr}(k) | k \in \mathbb{Z}\}$$

Replicated Data Types
Sequential Data Type Specification

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$$\sigma_2 \text{ does not contain wr operations}$$

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$$S_{\mathrm{intreg}}(\sigma \ \mathrm{wr}(k)) = S_{\mathrm{ctr}}(\sigma \ \mathrm{inc}) = \bot;$$

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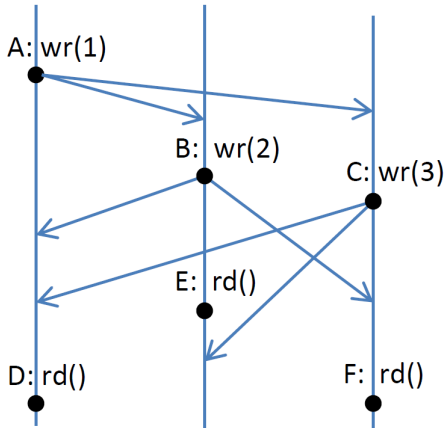
Replicated Data Types
Semantics of Eventual Consistency

- semantics of eventually consistent systems are harder to formalize
- concurrent operations on the same object happen on multiple replicas
- each replica executes operations immediately, updating other replicas later
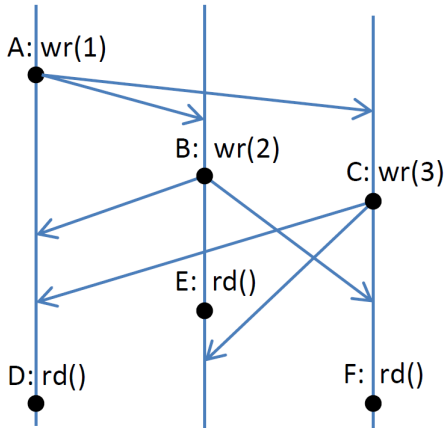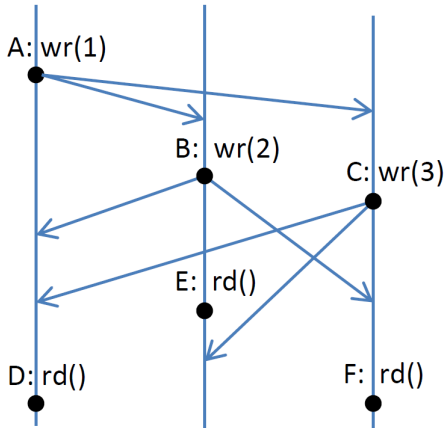- different implementation strategies for replicated data types

Replicated Data Types
Conflict Resolution Strategies

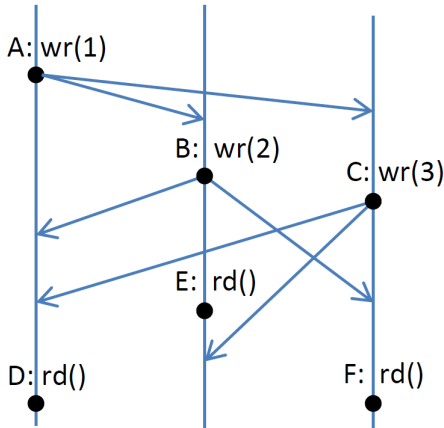1. make concurrent operations commutative

Replicated Data Types
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C: wr(3)

E: rd()

D: rd()

F: rd()

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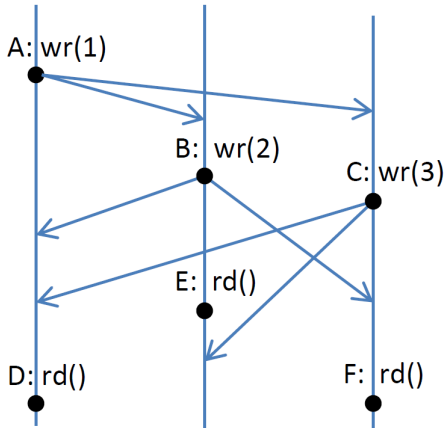3. flag conflicts (let the user decide)

Replicated Data Types
Conflict Resolution Strategies

1. make concurrent operations commutative
2. order concurrent operations
3. flag conflicts (let the user decide)
4. resolve conflicts semantically

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- visibility and order of preceding operations have to be included

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example: Strategy **Make Concurrent Calls Commutative**

$F_{\text{ctr}}(\text{inc}, V, \text{vis}, \text{ar}) = \bot;$

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example: Strategy **Order Concurrent Operations**

$$F_{\mathrm{intreg}}(\mathrm{inc}, V, \mathrm{vis}, \mathrm{ar}) = S_{\mathrm{intreg}}(V^{\mathrm{ar}} f)$$

Axiomatic Specification Framework

Session and Action

- clients wish to perform operations in a common context
- **sessions** provide a way to track client identity for operations
- an **action** is a tuple $(e, s, [x.f : k])$
    - e: unique identifier
    - s: session id $\in \mathrm{SId}$
    - $[x.f : k]$: object, operation and return value

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example:

$$a = (1af3c, 17, [x.rd : k]); \ \mathrm{type}(x) = \mathrm{intreg}$$

Axiomatic Specification Framework

History and Execution

- the set of all actions that happen in a database is denoted as Act
- a **history** (A, so) is a set of actions $A \subseteq \mathrm{Act}$ and a **session order** relation $\mathrm{so} \subseteq A \times A$
- an **execution** $X = (A, \mathrm{so}, \mathrm{vis}, \mathrm{ar})$ enhances the history with visibility and arbitration relations
- we can now extract an operation context for any action in any session, providing a deterministic return value

Axiomatic Specification Framework
Levels of Eventual Consistency

- with these replicated data types we can define multiple forms of Eventual Consistency
  - Basic Eventual Consistency
  - Session Guarantees
  - Causality
- every form contains multiple axioms
- more axioms mean stronger consistency

Axiomatic Specification Framework

Basic Eventual Consistency Axioms

- axioms a database implementation has to enforce to offer **basic eventual consistency**
- Well Formedness Axioms
    - SOwf: **so** *is the union of transitive, irreflexive and total orders on actions by each session*
    - VISwf: $\forall a, b.\ a \xrightarrow{\text{vis}} b \Rightarrow obj(a) = obj(b)$
    - ARwf: $\forall a, b.\ a \xrightarrow{\text{ar}} b \Rightarrow obj(a) = obj(b)$

Axiomatic Specification Framework

Basic Eventual Consistency Axioms

- Data Type Axiom(RVAL):
  $\forall a \in A.\ \mathrm{rval}(a) = F_{\mathrm{type(a)}}(\mathrm{ctxt}(a))$
- Basic Eventual Consistency axioms:
    - THINAIR:
      so $\cup$ vis is anticyclic
    - EVENTUAL:
      $\forall a \in A.\ \neg(\exists \text{infinitely many } b \in A.\ \mathrm{same}(a,b)) \wedge \neg(a \xrightarrow{\mathsf{vis}} b))$

Axiomatic Specification Framework

Problem with basic eventual consistency

TODO: Image explaining photo/noboss example from paper

Axiomatic Specification Framework
Session guarantees

- with basic eventual consistency we still might be reading values out of order
- axioms that formalise that all operation within a session keep the current context consistent:
  - Read Your Writes: *An operation sees all previous operations by the same session*
  - Writes Follow Reads in Visibility: *Arbitration orders an operation after other operations previously seen by the same session*
  - ... etc.

Axiomatic Specification Framework
Causality Axioms

- Per-object-causal-visibility: *POCV guarantees that an operation sees all operations on the same object that causally affect it*

- Per-object-causal-arbitration: *POCA correspondingly restricts the arbitration relation*

Consistency Strengthening Interfaces
Online Shopping

- almost everybody does online shopping
  - we put items in our shopping cart
  - we pay them
  - we continue shopping.. or not

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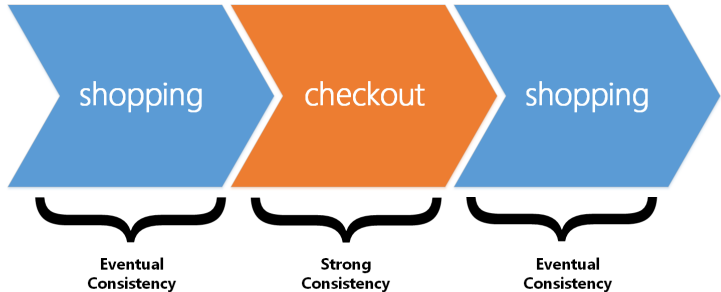
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Eventual Consistency	**Strong Consistency**	**Eventual Consistency**

Consistency Strengthening Interfaces

Consistency Annotations

- every **action** accepted by the database has to marked with a **consistency annotation**

$$(e, s, [x.f_\mu : k])\mu \in \{ORD, CSL\}$$

- either **ordinary** or **causal**
- ordinary actions behave like we defined previously
- causal actions make all operations performed before the annotations visible to all previous actions

Consistency Strengthening Interfaces
Fences

- instead of annotating every single action, a **fence** can be used
- a **fence** is an **action** where the executing replica forces all its updates on every other replica in the cluster

$$\text{action a} = (e, s, \text{fence})$$

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- the execution of other actions is halted until all replicas acknowledge the receipt
- this violates the **A** in **CAP**!

Conclusion

- the paper provides a way to **precisely specify eventually consistent systems** in a common notation
- **Every aspect of a system is covered**, from data types to client interaction
- specifications are **independent of implementation details**
- still **very theoretical**, no tools available to map between specifications and implementation
- the framework is **not suitable for programmers**, as it is very abstract and not easily understandable and applicable
- the paper is still "work in progress"

Discussion