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1) Design a DFA to accept string which start with 0 & end with 1

Definition:

From each state for each input symbol, there is exactly one transition.

Aim:

To design a DFA to accept string which start with 0 & end with 1.

Procedure:

step 1: Define 5 tuple and define the input / output values

step 2: Draw rough diagram with the given data.

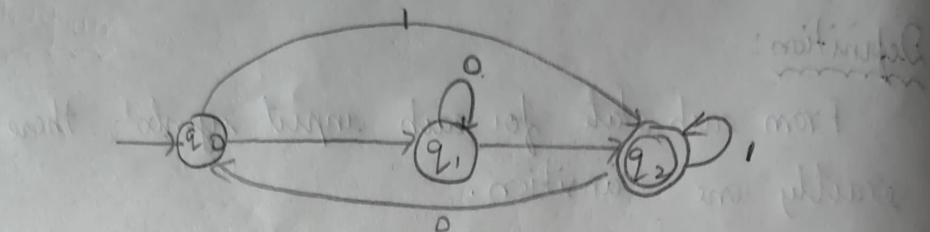
step 3: With the help of diagram, draw transition table.

step 4: With the help of transition table draw the circuit and simulate it with the help of software.

step 5: Define all the required state and select the type which is going to be created and Test whether the given input / output condition is satisfied.

Step 6: If yes, then it gets accepted, If no, then its get rejected.

Diagram: State graph representation of DFA accepting L

$$L = \{01, 001, 101, 11000, 10011, \dots\}$$


Transition table:

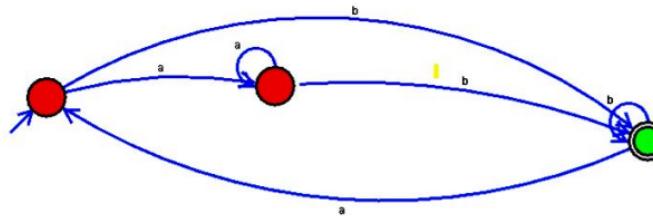
| States | 0 | 1 |
|--------|----|----|
| q0 | q1 | q2 |
| q1 | q0 | q2 |
| q2 | q0 | q2 |

Result: Designing a DFA to accept the string start with 0 and end with 1 is created & executed successfully.



File

Help



| | | | | | | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| a | b | a | b | b | a | b | a | b | b | a | a | a | a | a | b | ▼ |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|

2) Consider DFA $M = \{Q, \Sigma, \delta, q_0, F\}$ where
 $Q = \{A, B, C\}$ $\Sigma = \{0, 1\}$ q_0 is initial C is final.
 $\delta(A, 0) = B$ $\delta(A, 1) = C$
 $\delta(B, 0) = B$ $\delta(B, 1) = C$
 $\delta(C, 0) = A$ $\delta(C, 1) = B$

- i) Draw DFA ii) check string "100110" accepted or not iii) "110" accepted or not.

AIM: To construct DFA & checking strings are accepted or not.

DFA: From each state for each & every input symbol there will be exactly one transition.

Procedure:

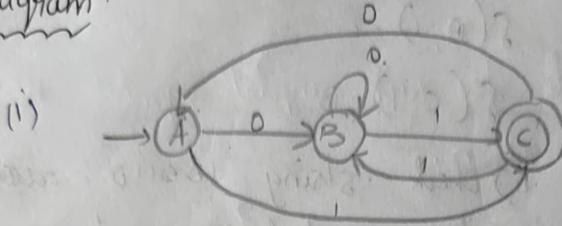
Step 1: Find tuples for DFA $M = (Q, \Sigma, \delta, q_0, F)$

$$Q = \{A, B, C\} . \quad \Sigma = \{0, 1\} . \quad q_0 = A, \quad F = C$$

- 2) Give input 0 from A to B & for input 1 from A to C
- 3) Give input 0 from B to B & for input 1 from B to C
- 4) Give input 0 from C to A & for input 1 from C to B
- 5) To implement this in Automation simulator.
- 6) Get states A, B, C after opening software
- 7) Give transitions according to diagram
- 8) Give input string & check whether it goes to destination or not.

- 9) If it goes to destination, that is accepted
 10) otherwise rejected.

Diagram:



$$\text{(i)} \quad s(A, 100110) = s(C, 00110)$$

$$= s(A, 0110)$$

$$= s(B, 110)$$

$$= s(C, 10)$$

$$= s(B, 0)$$

$$= B$$

B is not final state. So the string "100110" is not accepted by the DFA.

$$\text{(ii)} \quad s(A, 110) = s(C, 10)$$

$$= s(B, 0)$$

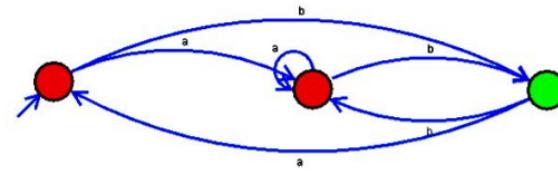
$$= B$$

B is not final state. So the string "110" is not accepted by the DFA.

Transition table:

| States | 0 | 1 |
|--------|---|---|
| A | B | C |
| B | B | C |
| C | A | B |

Result: DFA creation and check whether accepted or not is executed successfully.



I

| | | | | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| a | b | b | b | a | a | a | b | a | a | a | b | a | b | █ |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|

3) Construct NFA which accepts set of all strings with 3 consecutive 0's

Aim: To construct DFA which accepts set of all strings with 3 consecutive 0's.

DFA: From each state q for every input symbol there will be one or more transition.

PROCEDURE:

1) Find tuples for DFA $M = (Q, \Sigma, \delta, q_0, F)$

$$Q = \{q_0, q_1, q_2, q_3\}, \Sigma = \{0, 1\}, q_0 = q_0, F = q_3$$

2) Give input 0 from q_0 to q_0 & q_1 , for input 1 from q_0 to q_0 .

3) Give input 0 from q_1 to q_2 & for input 1 from q_1 to q_0

4) Give input 0 from q_2 to q_3 & for input 1 from q_2 to q_0

5) Give input 0 from q_3 to q_3 & for input 1 from q_3 to q_3

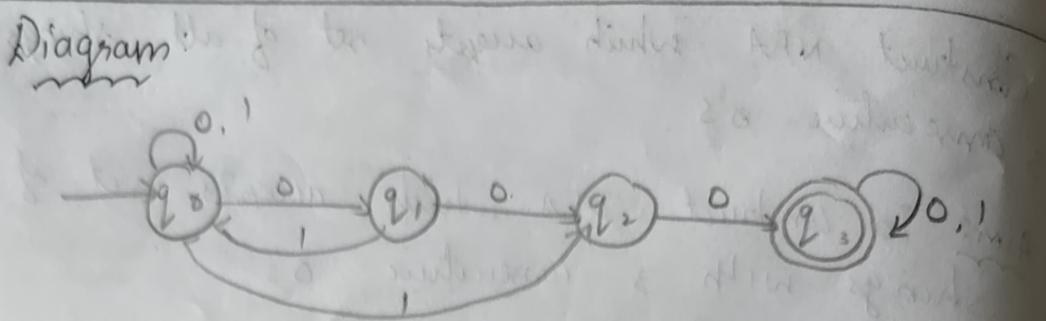
6) To implement this in Automation simulator

7) Get states q_0, q_1, q_2, q_3 after opening slw

8) Give transitions according to diagram.

9) Give input string & check whether it goes to destination or not.

10) If it goes to destination, that is accepted otherwise rejected.

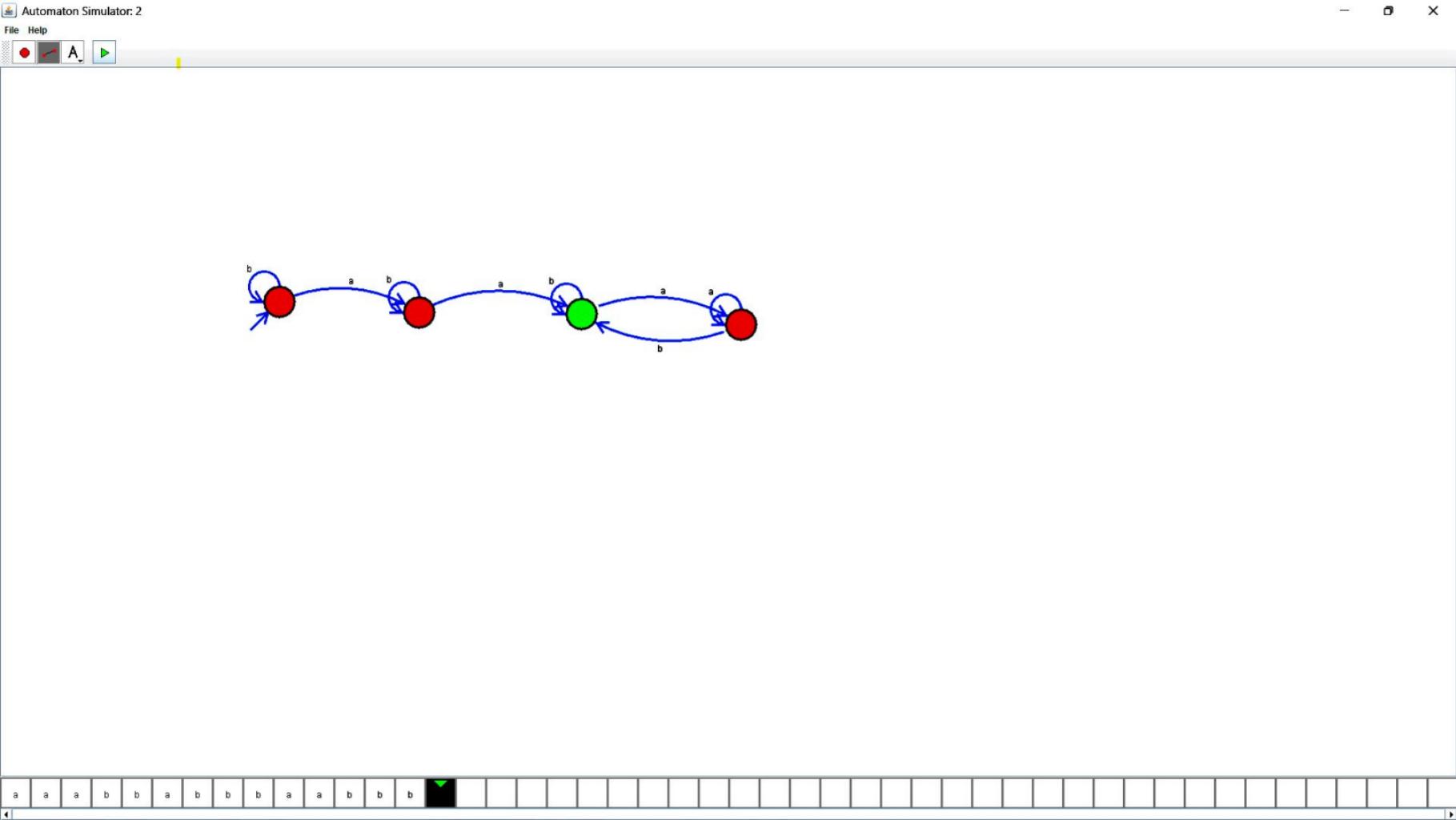


Transition table:

| States | 0 | 1 |
|--------|------------|-------|
| q_0 | q_0, q_1 | q_0 |
| q_1 | q_2 | q_0 |
| q_2 | q_3 | q_0 |
| q_3 | q_3 | q_3 |

Result:

To construct NFA which accepts set of all strings with 3 consecutive 0's is created & executed successfully.



4) Construct DFA which accepts even no. of 0's followed by single 1.

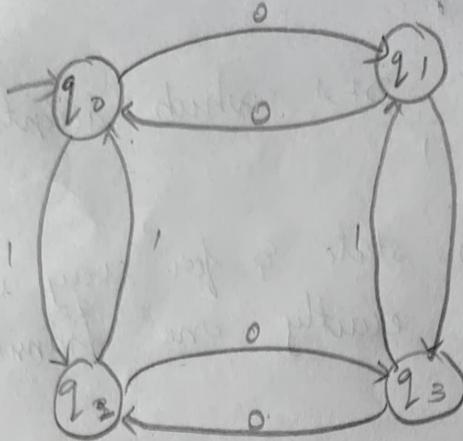
AIM: To construct DFA which accepts even no. of 0's & single 1.

DFA: From each state & for every input symbol there will be exactly one transition.

Procedure:

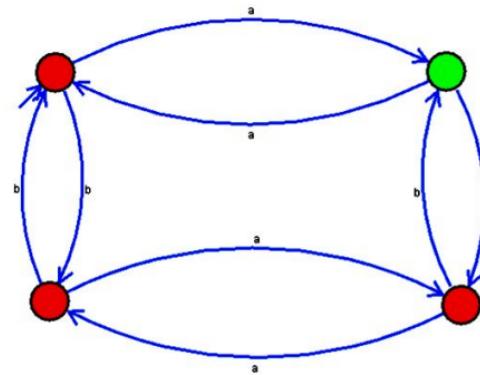
- 1) Find tuples for DFA $M = (\Phi, \Sigma, \delta, q_0, F)$
 $\Phi = \{q_0, q_1, q_2, q_3\}$, $\Sigma = \{0, 1\}$, $q_0 = q_0$, $F = q_1$
- 2) Give input 0 from q_0 to q_1 & for input 1 from q_0 to q_2 .
- 3) Give input 0 from q_1 to q_0 & for input 1 from q_1 to q_3 .
- 4) Give input 0 from q_2 to q_3 & for input 1 from q_2 to q_0 .
- 5) Give input 0 from q_3 to q_2 for input 1 from q_3 to q_1 .
- 6) To implement this in Automator simulator
- 7) Get states q_0, q_1, q_2, q_3 after opening s/w
- 8) Give transitions according to diagram.
- 9) Give input string & check whether it goes to destination or not.
- 10) If it goes to destination, that is accepted otherwise rejected.

Diagram:



Transition table:

| states | 0 | 1 |
|--------|----|----|
| q0 | q1 | q2 |
| q1 | q0 | q3 |
| q2 | q3 | q0 |
| q3 | q2 | q1 |



5) Draw NFA with input symbols $\{0, 1\}$ which accepts all the strings "01".

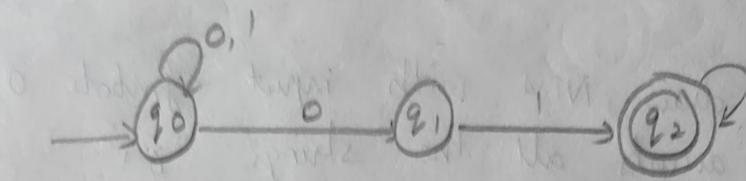
Aim:
To draw NFA with input symbols 0, 1 which accepts all the strings "01".

NFA: From each state for each input symbol we can have 0 or more transitions.

Procedure:

- 1) Find tuples for NFA $M = \{Q, S, \delta, q_0, F\}$
 $Q = \{q_0, q_1, q_2\}$, $S = \{0, 1\}$, $q_0 = q_0$, $F = q_2$.
- 2) Give input 0 from q_0 to q_0 & q_1 , for input 1 from q_0 to q_1 .
- 3) Give input 01 from q_1 to q_2 .
- 4) Give inputs 0 & 1 from q_2 to q_2 itself.
- 5) To implement this in Automation simulator.
- 6) Get states q_0, q_1, q_2 after opening s/w
- 7) Give transitions according to diagram.
- 8) Give input string & check whether it goes to destination or not.
- 9) If it goes to destination, that is accepted.
- 10) otherwise rejected.

Diagram:

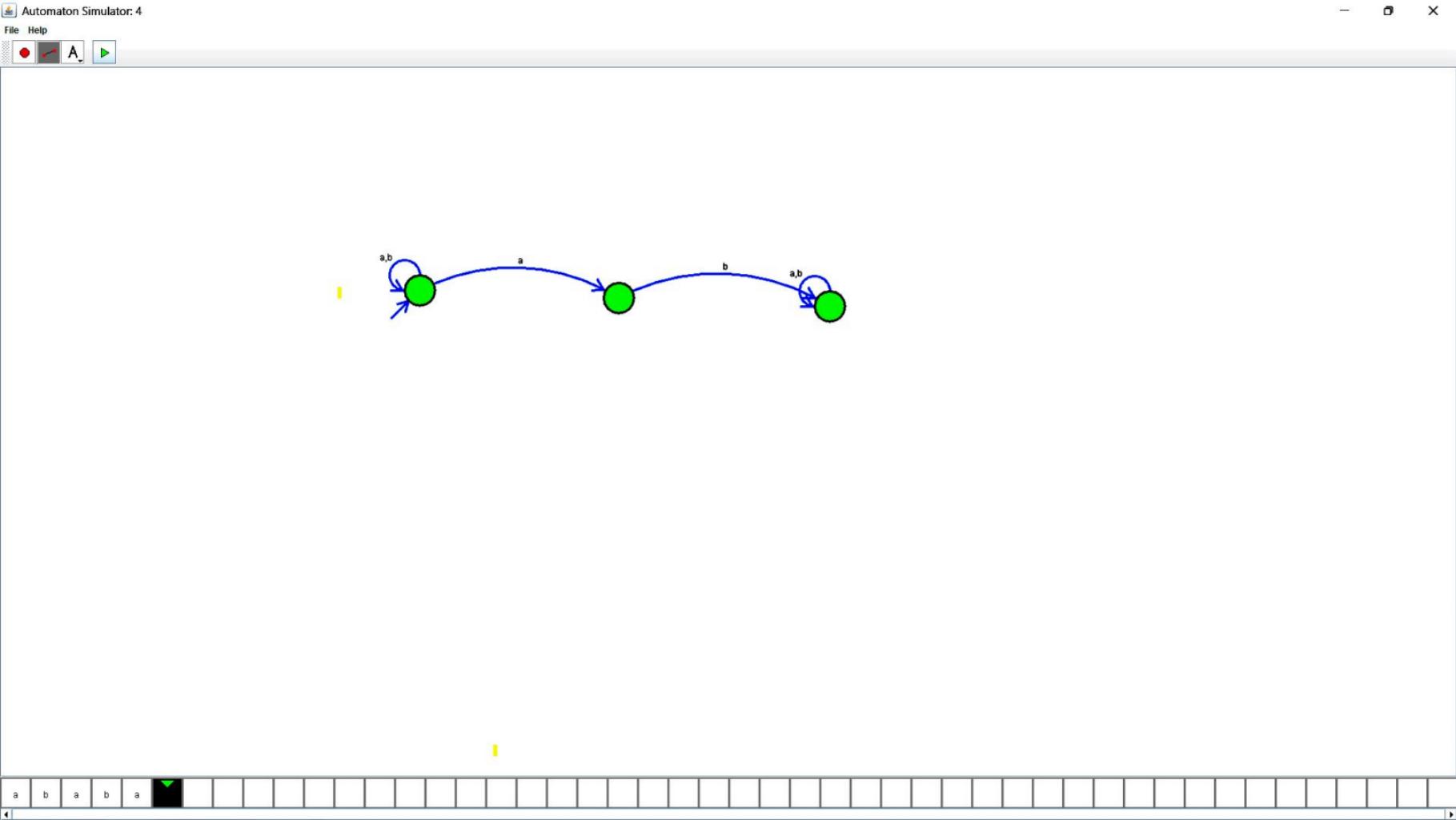


Transition table:

| state | 0 | 1 |
|-------|------|----|
| q0 | q0q1 | q0 |
| q1 | ∅ | q2 |
| q2 | q2 | q2 |

Result:

NFA with input symbol $\{0, 1\}$ which accepts all strings "01" is created and executed successfully.



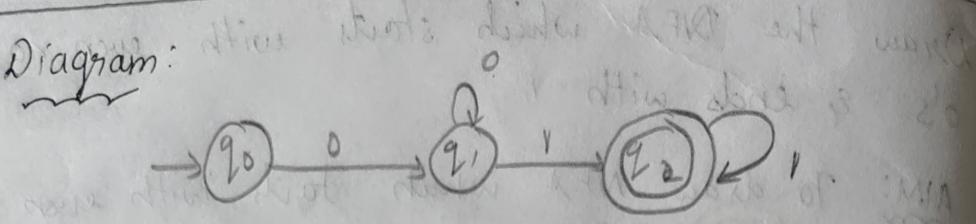
6) Draw the DFA which starts with even no. of 0's & ends with 1.

AIM: To draw NFA which starts with even no. of 0's & ends with 1.

NFA: From each state for each input symbol we can have 0 or more transitions.

Procedure:

- 1) Find tuples for NFA $M = (Q, \Sigma, \delta, q_0, F)$
 $Q = \{q_0, q_1, q_2\}$, $\Sigma = \{0, 1\}$, $q_0 = q_0$, $F = q_2$.
- 2) Give input 0 from q_0 to q_1 & for input 1 from q_0 to q_2 .
- 3) Give 0 from q_1 to q_1 for input 1 from q_1 to q_2 .
- 4) Give input 1 from q_2 to q_2 .
- 5) To implement this in Automation Simulator.
- 6) Get states q_0, q_1, q_2 after opening the file.
- 7) Give transitions according to diagram.
- 8) Give input string & check whether it goes to destination or not.
- 9) If it goes to destination that is accepted
- 10) otherwise rejected.



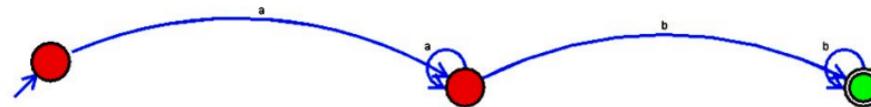
Transition table:

| states | 0 | 1 |
|--------|----|----|
| q0 | q1 | ∅ |
| q1 | q2 | q2 |
| q2 | ∅ | q2 |

Result:

DFA which starts from even no of 0's and ends with 1 is created & executed successfully.

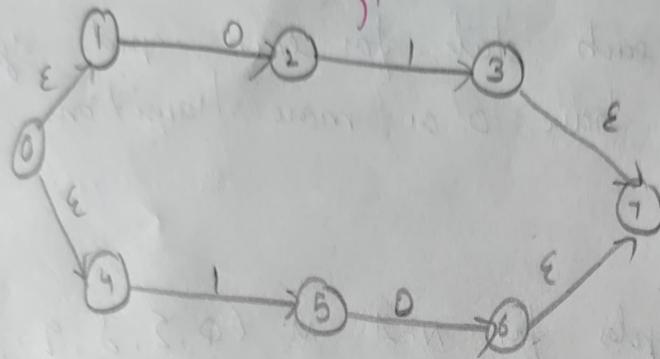
NFA which starts with even number of zeros and end with one



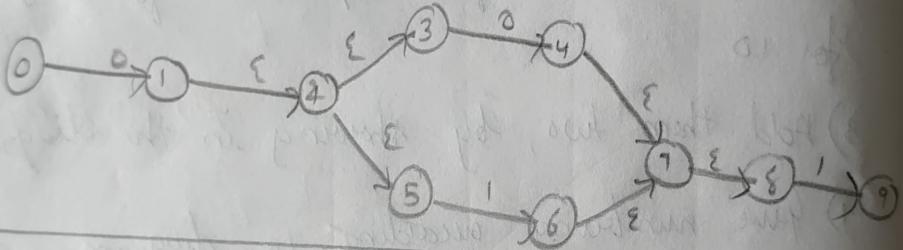
- 7) Draw NFA with epsilon for the regular expression
a) $01 + 10$ b) $0(0+1)^* 1$
- Aim: To draw NFA with epsilon for the RE
- NFA: From each state for each input symbol we can have 0 or more transitions.
- PROCEDURES:
- 1) Find tuples for NFA $M = (\Phi, \Sigma, \delta, q_0, F)$
 $\Phi = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9\}$, $\Sigma = \{0, 1\}$, $q_0 = 0$, $F = \{9, 7\}$
 - 2) First construct Regular expression for 01 & then for 10
 - 3) Add them two, by showing in the diagram.
 - 4) Give numbering according to diagram
 - 5) To implement this in Automata simulator
 - 6) Get states after opening the slw
 - 7) Give transitions as shown in diagram.
 - 8) Give input string & check whether it goes to destination or not
 - 9) If it goes to destination that is accepted
 - 10) otherwise Rejected

Diagram:

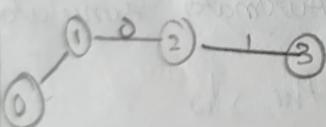
a) $01 + 10$.



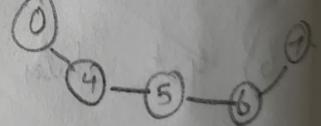
b) $0(0+1)^*$



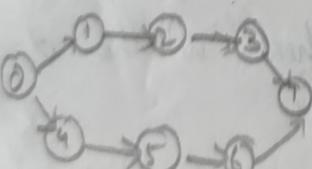
a) step 1



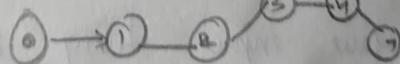
step 2:



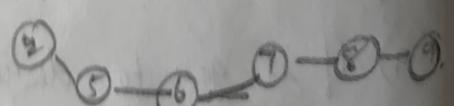
b) step 3



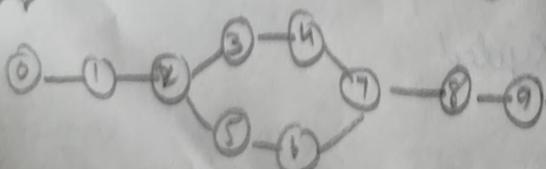
b) step 1



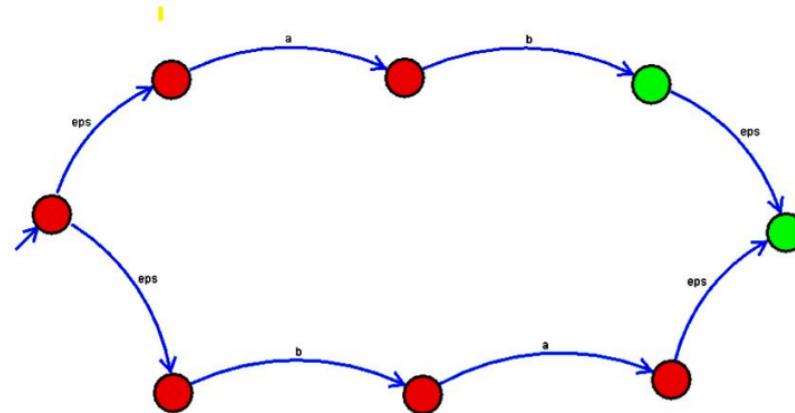
step 2

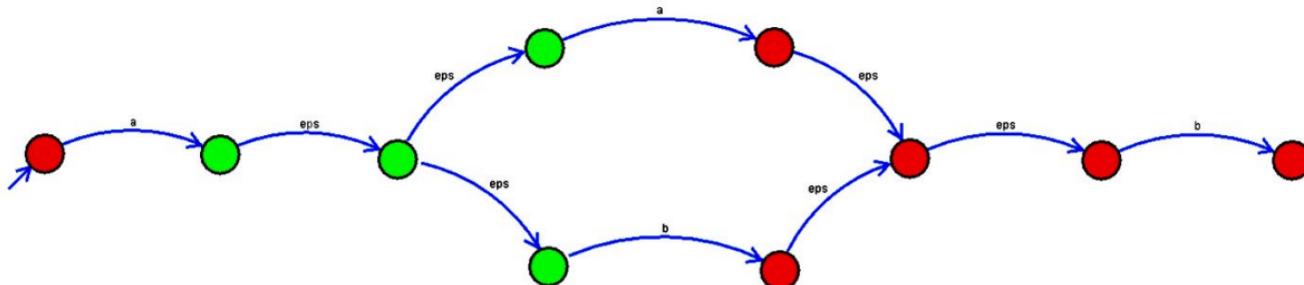


step 3



Result: NFA with epsilon regular expression is created and executed successfully.





8) Convert finite Automata for the regular expression
 $0^* 1^*$

Aim: To convert finite automata for the given regular expression.

Finite Automata:

It's a mathematical model of a system with discrete inputs & outputs.

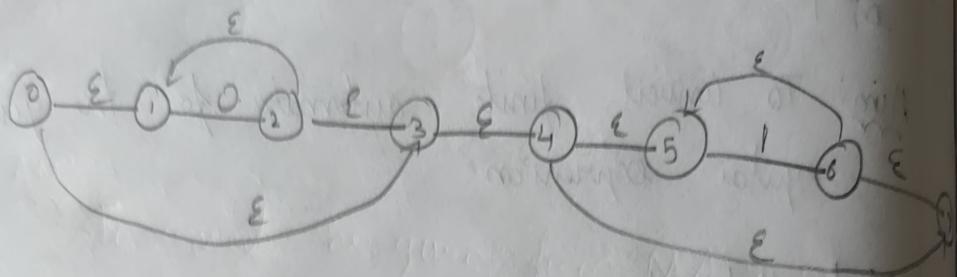
Regular Expression:

The languages accepted by finite automata are described by simple expressions called "RE".

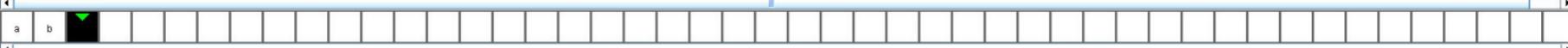
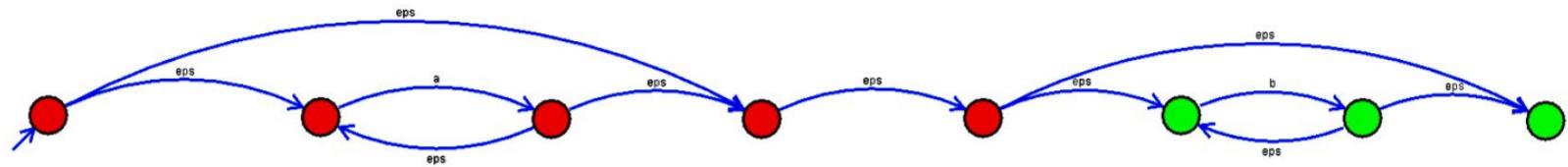
Procedure:

- 1) Construct regular expression for 0 with *
- 2) Construct regular expression for 1 with *
- 3) Combine these two as shown in diagram
- 4) To implement this in Automata simulate.
- 5) Get states after opening the software
- 6) Give transition as shown in diagram
- 7) Give input string & check whether it goes to destination or not.
- 8) If it goes to destination that is accepted.
- 9) Otherwise rejected

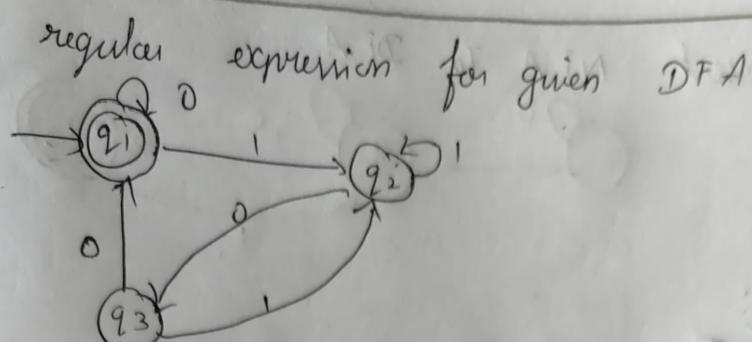
Diagram:



Result: Conversion of finite Automata is created & executed successfully.



9) Find



AIM: To find regular expression for given DFA

Arden's theorem:

If P & q are two RE over input Σ & if P does not contain then the following equation

" $R = \emptyset + RP^*$ " has unique solution $\boxed{R = \emptyset P^*}$

$$q_1 = q_1 \cdot 0 + q_3 \cdot 0 \rightarrow ①$$

$$q_2 = q_1 \cdot 1 + q_2 \cdot 1 + q_3 \cdot 1 \rightarrow ②$$

$$q_3 = q_2 \cdot 0 \rightarrow ③$$

sub ③ in ① & ②

$$q_1 = q_1 \cdot 0 + q_2 \cdot 0 \cdot 0 \rightarrow ④$$

$$q_2 = q_2 \cdot 1 + q_1 \cdot 1 + q_2 \cdot 0 \cdot 1 \rightarrow ⑤$$

$$q_2 = q_1 \cdot 1 + q_2 \cdot (1 + 0 \cdot 1)$$

$$R = \emptyset + R P^* \Rightarrow \boxed{R = \emptyset P^*}$$

$$q_2 = q_1 \cdot 1 \cdot (1 + 0 \cdot 1)^*$$

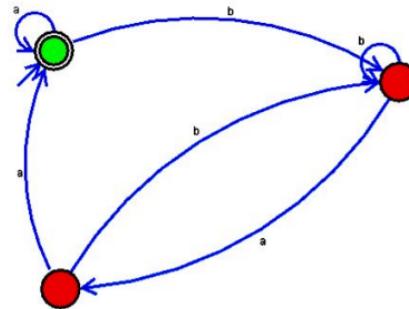
sub ④ in ①

$$q_1 = q_1 \cdot 0 + q_1 \cdot 1 \cdot (1 + 0 \cdot 1)^* \cdot 0 \cdot 1$$

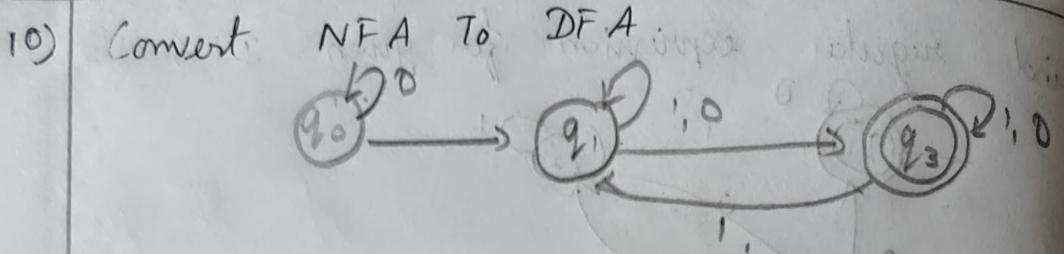
$$q_1 = q_1 \cdot 0 \cdot (1 + 1 \cdot (1 + 0 \cdot 1)^* \cdot 0 \cdot 1)^* \cdot \emptyset$$

$$q_1 = [0 \cdot (1 + 1 \cdot (1 + 0 \cdot 1)^* \cdot 0 \cdot 1)]^*$$

Result: regular expression for given DFA is created and solved successfully.



a b b b a b a a []



AIM:

To convert the given from NFA to DFA

PROCEDURE:

$$\Phi = q_0, q_1, q_2$$

$$\Sigma = \{0, 1\}$$

| δ | states | 0 | 1 |
|----------|--------|------------|------------|
| | q_0 | q_0 | q_1 |
| | q_1 | q_1, q_2 | q_1 |
| | q_2 | q_2 | q_1, q_3 |
| | q_0 | q_0 | |

$$F = q_2$$

Let M' be the DFA ' δ' ' be the New transition

$$\delta'(q_0, 0) = \delta'(q_0, 0) = \{q_0\}$$

$$\delta'(q_0, 1) = \delta(q_0, 1) = \{q_1\}$$

$$\delta'(q_0, 0) = \delta(q_1, 0) = \{q_1, q_0\}$$

$$\delta'(q_1, q_2, 0) = \delta(q_1, 0) \cup \delta'(q_2, 0) = q_1, q_2$$

$$\delta'(q_1, q_2, 1) = \delta(q_1, q_2, 1) = q_1, q_2$$

$$\delta'(q_1, 1) = \delta'(q_1, 1) = \{q_1\}$$

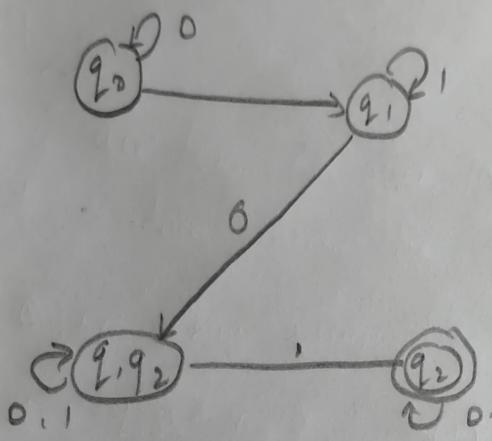
$$\delta'(q_2, 0) = \delta'(q_2, 0) = \{q_2\}$$

$$\delta'(q_2, 1) = \delta'(q_2, 1) = q_2$$

$$\delta^1 =$$

| state | 0 | 1 |
|------------|------------|------------|
| q_0 | q_0 | q_1 |
| q_1 | q_1, q_2 | q_1 |
| q_1, q_2 | q_1, q_2 | q_1, q_2 |
| q_2 | q_2 | q, q_2 |

DFA:

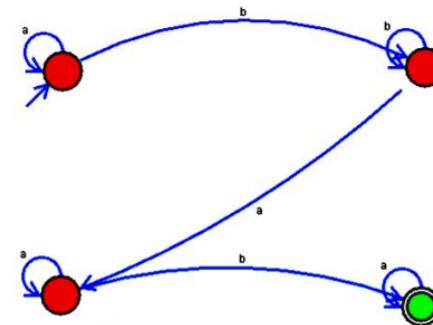


Design?

Result: Conversion of NFA to DFA is created
 has been successfully.

Automaton Simulator

File Help



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a b b a b a a

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