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Assignment 2

AI1110: Probability and Random Variables INDIAN INSTITUTE OF TECHNOLOGY, HYDERABAD

SUVEDH CS22BTECH11016

10.15.2.3: A bag contains 5 red balls and some blue balls. If the probability of drawing a blue ball is double that if a red ball, determine the number of blue balls in the bag.

Solution:

Let's assume that there are x blue balls in the bag

Since there are 5 red balls in the bag and a total of 5 + x balls.

Let Pr(R) and Pr(B) be the probabilities of drawing a red and blue ball.

(a) The probability of drawing a red ball is

$$\Pr(R) = \frac{5}{5+x} \tag{1}$$

(b) given the probability of drawing a blue ball is double that of drawing a red ball. So,The probability of drawing a blue ball is:

$$\Pr(B) = 2 \times \left(\frac{5}{5+x}\right) \tag{2}$$

(c) We know that the sum of the probabilities of drawing a red ball and drawing a blue ball is equal to 1

$$\left(\frac{5}{5+x}\right) + 2\left(\frac{5}{5+x}\right) = 1\tag{3}$$

$$\frac{5}{5+x} + \frac{10}{5+x} = 1\tag{4}$$

$$\frac{15}{5+x} = 1 {(5)}$$

$$5 + x = 15 \tag{6}$$

$$x = 10 \tag{7}$$

Therefore, there are 10 blue balls in the bag.