

Assignment 2

AI1110: Probability and Random Variables

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SUVEDH
CS22BTECH11016

10.15.2.3: A bag contains 5 red balls and some blue balls. If the probability of drawing a blue ball is double that of a red ball, determine the number of blue balls in the bag.

Solution:

Let's assume that there are x blue balls in the bag

Since there are 5 red balls in the bag and a total of $5 + x$ balls.

Let $\Pr(R)$ and $\Pr(B)$ be the probabilities of drawing a red and blue ball.

(a) The probability of drawing a red ball is

$$\Pr(R) = \frac{5}{5 + x} \quad (1)$$

(b) The probability of drawing a blue ball is:

$$\Pr(B) = \frac{5}{5 + x} \quad (2)$$

(c) given the probability of drawing a blue ball is double that of drawing a red ball.

We know that the sum of the probabilities of drawing a red ball and drawing a blue ball is equal to 1

$$\left(\frac{5}{5 + x}\right) + 2\left(\frac{5}{5 + x}\right) = 1 \quad (3)$$

$$(4)$$

$$\frac{5}{5 + x} + \frac{10}{5 + x} = 1 \quad (5)$$

$$(6)$$

$$\frac{15}{5 + x} = 1 \quad (7)$$

$$(8)$$

$$5 + x = 15 \quad (9)$$

$$(10)$$

$$x = 10 \quad (11)$$

Therefore, there are 10 blue balls in the bag.