

• an episode may never finish.

Then, it is possible that iterative policy evaluation will not converge, and this is because the state-value function may not be well-defined! To see this, note that in this case, calculating a state value could involve adding up an infinite number of (expected) rewards, where the sum may not **converge**.

In case it would help to see a concrete example, consider an MDP with:

- ullet two states  $s_1$  and  $s_2$ , where  $s_2$  is a terminal state
- one action a (Note: An MDP with only one action can also be referred to as a Markov Reward Process (MRP).)
- $p(s_1, 1|s_1, a) = 1$

In this case, say the agent's policy  $\pi$  is to "select" the only action that's available, so  $\pi(s_1)=a$ . Say  $\gamma=1$ . According to the one-step dynamics, if the agent starts in state  $s_1$ , it will stay in that state forever and never encounter the terminal state  $s_2$ .

In this case,  $v_{\pi}(s_1)$  is not well-defined. To see this, remember that  $v_{\pi}(s_1)$  is the (expected) return after visiting state  $s_1$ , and we have that

$$v_{\pi}(s_1) = 1 + 1 + 1 + 1 + \dots$$

which **diverges** to infinity. (Take the time now to convince yourself that if either of the two convergence conditions were satisfied in this example, then  $v_{\pi}(s_1)$  would be well-defined. As a **very optional** next step, if you want to verify this mathematically, you may find it useful to review **geometric series** and the **negative binomial distribution**.)

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