

First Approach

Density of a robber = (number of robber surrounding it + itself) / number of possible places

Case 1

e.g., Density of Robber in the corner = $2 / 4 = 0.50$

Average Density of a formation/placement = $(0.50 \times 3 + 0.56 \times 2 + 0.67 \times 3) / 8 = 0.58$

				R 0.50
			R 0.56	R 0.67
		R	R 0.67	
	R	R		R 0.50

Case 2

Average density of robber in all configurations/formation.

Grid Size	Number of Robbers								
	2	3	4	5	6	7	8	9	10
3 x 3	0.298	0.398	0.498						
4 x 4	0.229	0.284	0.339	0.394	0.449	0.504			
5 x 5	0.195	0.230	0.265	0.299	0.389	0.370	0.405	0.440	

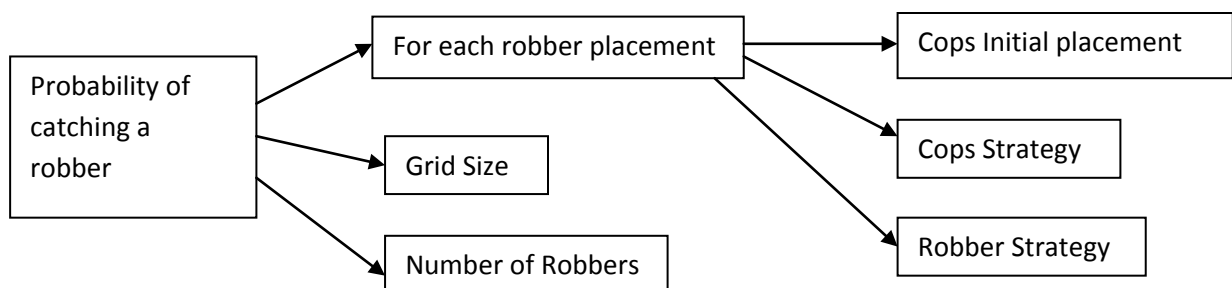
Conclusion

Average density of a single configuration (case 1) cannot say anything about the probability of catching it. Average density of robbers in all configuration/formation (case 2) is similar to the fraction of robber present in the grid.

New Approach

Fraction of the grid occupied/filled by the Robbers, $F_r = \text{Number of Robber} / (\text{Size of the grid} \times \text{Size of the grid})$

We can say that. Fraction of the grid occupied by Robbers $\propto 1 / (\text{Probability of the robbers getting caught})$



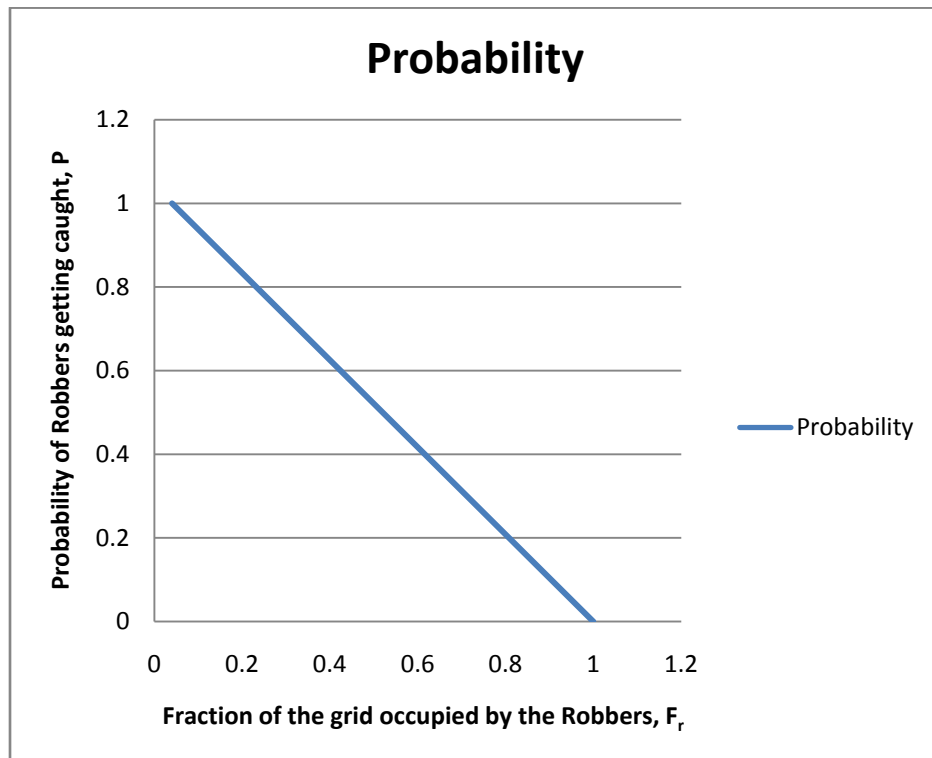
If,

$$P = 1 - K \times F_r$$

P = Probability of robber being caught

F_r = Fraction of the grid occupied by the Robbers

K = constant, Depends on Number of Cops, Cops Strategy and Robber Strategy



The value of K ,

For number of Robber, $R = 1$; Grid Size = 5; Probability, $P = 1$

$$F_r = 1 / 25 = 0.04$$

For number of Robber, $R = 25$; Grid Size = 5; Probability, $P = 0$

$$F_r = 25 / 25 = 1$$

So, $K > 1$.

Conclusion

Working on the value of K .