

Type Checking

- A compiler must do semantic checks in addition to syntactic checks.
- *Type checking* is one of these static checking operations.
 - we may not do all type checking at compile-time.
 - Some systems also use dynamic type checking too.
- A programming language is *strongly-typed*, if every program if compiler accepts, will execute without type errors.
 - In practice, some of type checking operations are done at run-time (so, most of the programming languages are not strongly-typed).
 - Ex: `int x[100]; ... x[i]` → most of the compilers cannot guarantee that `i` will be between 0 and 99

A Simple Type Checking System

$P \rightarrow D;E$

$D \rightarrow D;D$

$D \rightarrow \mathbf{id}:T \quad \{ \text{addtype}(\text{id.entry}, T.\text{type}) \}$

$T \rightarrow \text{char} \quad \{ T.\text{type}=\text{char} \}$

$T \rightarrow \text{int} \quad \{ T.\text{type}=\text{int} \}$

$T \rightarrow \text{real} \quad \{ T.\text{type}=\text{real} \}$

$T \rightarrow \uparrow T_1 \quad \{ T.\text{type}=\text{pointer}(T_1.\text{type}) \}$

$T \rightarrow \text{array}[\mathbf{intnum}] \text{ of } T_1 \quad \{ T.\text{type}=\text{array}(1..\text{intnum.val}, T_1.\text{type}) \}$

Type Checking of Expressions

$E \rightarrow \mathbf{id} \quad \{ E.type = \text{lookup}(\text{id.entry}) \}$

$E \rightarrow \mathbf{charliteral} \quad \{ E.type = \text{char} \}$

$E \rightarrow \mathbf{intliteral} \quad \{ E.type = \text{int} \}$

$E \rightarrow \mathbf{realliteral} \quad \{ E.type = \text{real} \}$

$E \rightarrow E_1 + E_2 \quad \{ \text{if } (E_1.type = \text{int} \text{ and } E_2.type = \text{int}) \text{ then } E.type = \text{int}$
 $\text{else if } (E_1.type = \text{int} \text{ and } E_2.type = \text{real}) \text{ then } E.type = \text{real}$
 $\text{else if } (E_1.type = \text{real} \text{ and } E_2.type = \text{int}) \text{ then } E.type = \text{real}$
 $\text{else if } (E_1.type = \text{real} \text{ and } E_2.type = \text{real}) \text{ then } E.type = \text{real}$
 $\text{else } E.type = \text{type-error} \}$

$E \rightarrow E_1 [E_2] \quad \{ \text{if } (E_2.type = \text{int} \text{ and } E_1.type = \text{array}(s, t)) \text{ then } E.type = t$
 $\text{else } E.type = \text{type-error} \}$

$E \rightarrow E_1 \uparrow \quad \{ \text{if } (E_1.type = \text{pointer}(t)) \text{ then } E.type = t$
 $\text{else } E.type = \text{type-error} \}$

Type Checking of Statements

$S \rightarrow \mathbf{id} = E$ { if ($\mathbf{id.type} = E.type$ then $S.type = \text{void}$
 else $S.type = \text{type-error}$ }

$S \rightarrow \mathbf{if} E \mathbf{then} S_1$ { if ($E.type = \text{boolean}$ then $S.type = S_1.type$
 else $S.type = \text{type-error}$ }

$S \rightarrow \mathbf{while} E \mathbf{do} S_1$ { if ($E.type = \text{boolean}$ then $S.type = S_1.type$
 else $S.type = \text{type-error}$ }

Intermediate Code Generation

- *Intermediate codes* are **machine independent** codes, but they are close to machine instructions.
- The given program in a source language is converted to an equivalent program in an intermediate language by the intermediate code generator.
- **Intermediate language** can be many different languages, and the designer of the compiler decides this intermediate language.
 - **syntax trees** can be used as an intermediate language.
 - **postfix notation** can be used as an intermediate language.
 - **three-address code (Quadruples)** can be used as an intermediate language
 - we will use quadruples to discuss intermediate code generation
 - quadruples are close to machine instructions, but they are not actual machine instructions.
 - some programming languages have well defined intermediate languages.
 - java – java virtual machine
 - prolog – warren abstract machine
 - In fact, there are byte-code emulators to execute instructions in these intermediate languages.

Three-Address Code (Quadraples)

- A quadraple is:

$$x := y \text{ op } z$$

where x , y and z are names, constants or compiler-generated temporaries; **op** is any operator.

- But we may also the following notation for quadraples (much better notation because it looks like a machine code instruction)

$$\text{op } y, z, x$$

apply operator op to y and z , and store the result in x .

- We use the term “three-address code” because each statement usually contains three addresses (two for operands, one for the result).

Three-Address Statements

Binary Operator: `op y, z, result` or `result := y op z`

where `op` is a binary arithmetic or logical operator. This binary operator is applied to `y` and `z`, and the result of the operation is stored in `result`.

Ex:

```
add    a, b, c
gt     a, b, c
addi   a, b, c
```

Unary Operator: `op y, , result` or `result := op y`

where `op` is a unary arithmetic or logical operator. This unary operator is applied to `y`, and the result of the operation is stored in `result`.

Ex:

```
uminus    a, , c
not        a, , c
inttoreal a, , c
```

Three-Address Statements (cont.)

Move Operator: `mov y, , result` or `result := y`

where the content of `y` is copied into `result`.

Ex: `mov a, , c`
 `movi a, , c`
 `movr a, , c`

Unconditional Jumps: `jmp , , L` or `goto L`

We will jump to the three-address code with the label `L`, and the execution continues from that statement.

Ex: `jmp , , L1` // jump to L1
 `jmp , , 7` // jump to the statement 7

Three-Address Statements (cont.)

Conditional Jumps: `jmp relop y, z, L` or `if y relop z goto L`

We will jump to the three-address code with the label L if the result of `y relop z` is true, and the execution continues from that statement. If the result is false, the execution continues from the statement following this conditional jump statement.

Ex:

<code>jmpgt</code>	<code>y, z, L1</code>	<code>// jump to L1 if y>z</code>
<code>jmpgte</code>	<code>y, z, L1</code>	<code>// jump to L1 if y>=z</code>
<code>jmpe</code>	<code>y, z, L1</code>	<code>// jump to L1 if y==z</code>
<code>jmpne</code>	<code>y, z, L1</code>	<code>// jump to L1 if y!=z</code>

Our relational operator can also be a unary operator.

<code>jmpnz</code>	<code>y, , L1</code>	<code>// jump to L1 if y is not zero</code>
<code>jmpz</code>	<code>y, , L1</code>	<code>// jump to L1 if y is zero</code>
<code>jmpt</code>	<code>y, , L1</code>	<code>// jump to L1 if y is true</code>
<code>jmpf</code>	<code>y, , L1</code>	<code>// jump to L1 if y is false</code>

Three-Address Statements (cont.)

Procedure Parameters: param x,, or param x

Procedure Calls: call p,n, or call p,n

where x is an actual parameter, we invoke the procedure p with n parameters.

Ex:

param x₁,,

param x₂,,

→ p(x₁, ..., x_n)

param x_n,,

call p,n,

f(x+1, y) → add x,1,t1
 param t1,,
 param y,,
 call f,2,

Three-Address Statements (cont.)

Indexed Assignments:

move $y[i], , x$ or $x := y[i]$
move $x, , y[i]$ or $y[i] := x$

Address and Pointer Assignments:

moveaddr $y, , x$ or $x := \&y$
movecont $y, , x$ or $x := *y$

Syntax-Directed Translation into Three-Address Code

$S \rightarrow \mathbf{id} := E$	$S.\text{code} = E.\text{code} \parallel \text{gen}(\text{'mov' } E.\text{place ',, ' id.place})$
$E \rightarrow E_1 + E_2$	$E.\text{place} = \text{newtemp}();$ $E.\text{code} = E_1.\text{code} \parallel E_2.\text{code} \parallel \text{gen}(\text{'add' } E_1.\text{place ',' } E_2.\text{place ',' } E.\text{place})$
$E \rightarrow E_1 * E_2$	$E.\text{place} = \text{newtemp}();$ $E.\text{code} = E_1.\text{code} \parallel E_2.\text{code} \parallel \text{gen}(\text{'mult' } E_1.\text{place ',' } E_2.\text{place ',' } E.\text{place})$
$E \rightarrow - E_1$	$E.\text{place} = \text{newtemp}();$ $E.\text{code} = E_1.\text{code} \parallel \text{gen}(\text{'uminus' } E_1.\text{place ',, ' } E.\text{place})$
$E \rightarrow (E_1)$	$E.\text{place} = E_1.\text{place};$ $E.\text{code} = E_1.\text{code}$
$E \rightarrow \mathbf{id}$	$E.\text{place} = \mathbf{id}.\text{place};$ $E.\text{code} = \text{null}$

Syntax-Directed Translation (cont.)

$S \rightarrow \text{while } E \text{ do } S_1$	<pre>S.begin = newlabel(); S.after = newlabel(); S.code = gen(S.begin ":") E.code gen('jmpf' E.place ',', S.after) S₁.code gen('jmp' ',', S.begin) gen(S.after ':')</pre>
$S \rightarrow \text{if } E \text{ then } S_1 \text{ else } S_2$	<pre>S.else = newlabel(); S.after = newlabel(); S.code = E.code gen('jmpf' E.place ',', S.else) S₁.code gen('jmp' ',', S.after) gen(S.else ':') S₂.code gen(S.after ':')</pre>

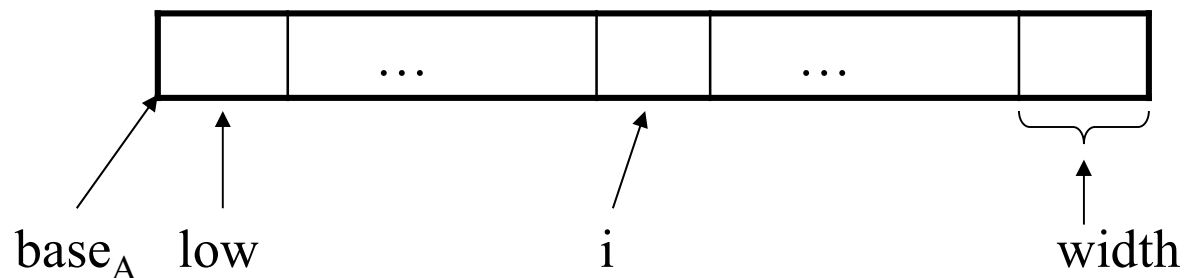
Translation Scheme to Produce Three-Address Code

$S \rightarrow \mathbf{id} := E$	{ p = lookup(id.name); if (p is not nil) then emit('mov' E.place ',', p) else error("undefined-variable") }	a = b+ -c
$E \rightarrow E_1 + E_2$	{ E.place = newtemp(); emit('add' E ₁ .place ',', E ₂ .place ',', E.place) }	ICG will generate
$E \rightarrow E_1 * E_2$	{ E.place = newtemp(); emit('mult' E ₁ .place ',', E ₂ .place ',', E.place) }	uminus c,, t1 add b, t1, t2 mov t2,,a
$E \rightarrow - E_1$	{ E.place = newtemp(); emit('uminus' E ₁ .place ',', E.place) }	
$E \rightarrow (E_1)$	{ E.place = E ₁ .place; }	
$E \rightarrow \mathbf{id}$	{ p = lookup(id.name); if (p is not nil) then E.place = id .place else error("undefined-variable") }	

Arrays

- Elements of arrays can be accessed quickly if the elements are stored in a block of consecutive locations.

A one-dimensional array **A**:



base_A is the address of the first location of the array **A**,

width is the width of each array element.

low is the index of the first array element

location of $A[i] \rightarrow \text{base}_A + (i - \text{low}) * \text{width}$

Arrays (cont.)

$\text{base}_A + (i - \text{low}) * \text{width}$

can be re-written as $\underbrace{i * \text{width}}_{\text{should be computed at run-time}} + \underbrace{(\text{base}_A - \text{low} * \text{width})}_{\text{can be computed at compile-time}}$

should be computed at run-time

can be computed at compile-time

- So, the location of $A[i]$ can be computed at the run-time by evaluating the formula $i * \text{width} + c$ where c is $(\text{base}_A - \text{low} * \text{width})$ which is evaluated at compile-time.
- Intermediate code generator should produce the code to evaluate this formula $i * \text{width} + c$ (one multiplication and one addition operation).

Translation Scheme for Arrays

- If we use the following grammar to calculate addresses of array elements, we need inherited attributes.

$$L \rightarrow \mathbf{id} \mid \mathbf{id} [\text{Elist}]$$
$$\text{Elist} \rightarrow \text{Elist} , E \mid E$$

- Instead of this grammar, we will use the following grammar to calculate addresses of array elements so that we do not need inherited attributes (we will use only synthesized attributes).

$$L \rightarrow \mathbf{id} \mid \text{Elist}]$$
$$\text{Elist} \rightarrow \text{Elist} , E \mid \mathbf{id} [E$$

Translation Scheme for Arrays (cont.)

$S \rightarrow L := E$ { if (L.offset is null) emit('mov' E.place ',', L.place)
 else emit('mov' E.place ',', L.place '[' L.offset ']') }

$E \rightarrow E_1 + E_2$ { E.place = newtemp();
 emit('add' E₁.place ',', E₂.place ',', E.place) }

$E \rightarrow (E_1)$ { E.place = E₁.place; }

$E \rightarrow L$ { if (L.offset is null) E.place = L.place)
 else { E.place = newtemp();
 emit('mov' L.place '[' L.offset ']' ',', E.place) } }

Translation Scheme for Arrays (cont.)

$L \rightarrow \mathbf{id} \quad \{ L.place = \mathbf{id}.place; L.offset = \text{null}; \}$

$L \rightarrow \text{Elist }]$

$\{ L.place = \text{newtemp}(); L.offset = \text{newtemp}();$
 $\text{emit}(\text{'mov' } c(\text{Elist.array}) \text{' ,,' } L.place);$
 $\text{emit}(\text{'mult' } \text{Elist.place} \text{' ,'} \text{width}(\text{Elist.array}) \text{' ,'} L.offset) \}$

$\text{Elist} \rightarrow \text{Elist}_1, E$

$\{ \text{Elist.array} = \text{Elist}_1.array; \text{Elist.place} = \text{newtemp}(); \text{Elist.ndim} = \text{Elist}_1.ndim + 1;$
 $\text{emit}(\text{'mult' } \text{Elist}_1.place \text{' ,'} \text{limit}(\text{Elist.array}, \text{Elist.ndim}) \text{' ,'} \text{Elist.place});$
 $\text{emit}(\text{'add' } \text{Elist.place} \text{' ,'} E.place \text{' ,'} \text{Elist.place}); \}$

$\text{Elist} \rightarrow \mathbf{id} [E$

$\{ \text{Elist.array} = \mathbf{id}.place; \text{Elist.place} = E.place; \text{Elist.ndim} = 1; \}$

Translation Scheme for Arrays – Example1

- A one-dimensional double array A : 5..100
→ $n_1=95$ width=8 (double) low₁=5
- Intermediate codes corresponding to $x := A[y]$

```
mov    c, , t1           // where c=baseA-(5)*8
mult   y, 8, t2
mov     t1[t2], , t3
mov     t3, , x
```

Declarations

$P \rightarrow M D$

$M \rightarrow \epsilon \quad \{ \text{offset}=0 \}$

$D \rightarrow D ; D$

$D \rightarrow \mathbf{id} : T \quad \{ \text{enter}(\mathbf{id.name}, T.\text{type}, \text{offset}); \text{offset}=\text{offset}+T.\text{width} \}$

$T \rightarrow \text{int} \quad \{ T.\text{type}=\text{int}; T.\text{width}=4 \}$

$T \rightarrow \text{real} \quad \{ T.\text{type}=\text{real}; T.\text{width}=8 \}$

$T \rightarrow \text{array}[\text{num}] \text{ of } T_1 \quad \{ T.\text{type}=\text{array}(\text{num.val}, T_1.\text{type});$
 $\quad T.\text{width}=\text{num.val} * T_1.\text{width} \}$

$T \rightarrow \uparrow T_1 \quad \{ T.\text{type}=\text{pointer}(T_1.\text{type}); T.\text{width}=4 \}$

where *enter* creates a symbol table entry with given values.