

**flex**

# **flex - fast lexical analyzer generator**

- Flex is a tool for generating scanners/lexical analyzers
- Flex source is a table of regular expressions and corresponding program fragments.
- Generates `lex.yy.c` which defines a routine `yylex()`

# Format of the Input File

- The flex input file consists of three sections, separated by a line with just %% in it:

definitions

%%

rules

%%

user code

# Definitions Section

- The definitions section contains declarations of simple name definitions to simplify the scanner specification.
- Name definitions have the form:

`name definition`

- Example:

`DIGIT [0-9]`

`ID [a-z][a-z0-9]*`

# Rules Section

- The rules section of the flex input contains a series of rules of the form:

`pattern action`

- Example:

`{ID} printf( "An identifier: %s\n", yytext );`

- The *yytext* and *yylength* variable.
- If action is empty, the matched token is discarded.

# Action

- If the action contains a `{`, the action spans till the balancing `}` is found, as in C.
- An action consisting only of a vertical bar (`|`) means "same as the action for the next rule."
- The *return* statement, as in C.
- In case no rule matches: simply copy the input to the standard output (A default rule).

# A Simple Example

```
%{  
    int num_lines = 0, num_chars = 0;  
}%  
  
%%  
\n    ++num_lines; ++num_chars;  
.    ++num_chars;  
  
%%  
main()  {  
    yylex();  
    printf( "# of lines = %d, # of chars = %d\n",  
            num_lines, num_chars );  
}
```

# Programming Assignment 1

- Write a lexical analyzer using lex/flex to identify tokens of a typical C program. The program should be able to print series of token-ids for every lexical pattern that it recognizes. Please show the lex specification and the working of the lexical analyzer.
- Time Period : 2 weeks (deadline: 31<sup>st</sup> Jan 2021)

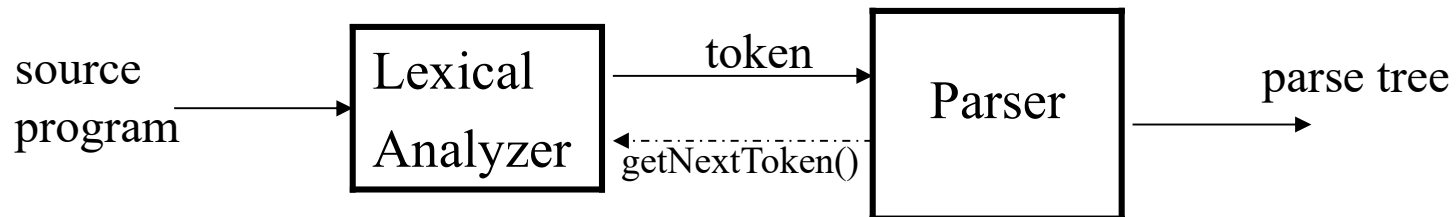


# Syntax Analyzer

- *Syntax Analyzer* creates the syntactic structure of the given source program.
- This syntactic structure is mostly a *parse tree*.
- Syntax Analyzer is also known as *parser*.
- The syntax of a programming is described by a *context-free grammar (CFG)*. We will use BNF (Backus-Naur Form) notation in the description of CFGs.
- The syntax analyzer (parser) checks whether a given source program satisfies the rules implied by a context-free grammar or not.
  - If it satisfies, the parser creates the parse tree of that program.
  - Otherwise the parser gives the error messages.
- A context-free grammar
  - gives a precise syntactic specification of a programming language.
  - the design of the grammar is an initial phase of the design of a compiler.
  - a grammar can be directly converted into a parser by some tools (like yacc/bison)

# Parser

- Parser works on a stream of tokens.
- The smallest item is a token.



# Parsers (cont.)

- We categorize the parsers into two groups:
  - 1. Top-Down Parser**
    - the parse tree is created top to bottom, starting from the root.
  - 2. Bottom-Up Parser**
    - the parse is created bottom to top; starting from the leaves
- Both top-down and bottom-up parsers scan the input from left to right (one symbol at a time).
- Efficient top-down and bottom-up parsers can be implemented only for sub-classes of context-free grammars.
  - LL for top-down parsing
  - LR for bottom-up parsing

# Context-Free Grammars

- Inherently recursive structures of a programming language are defined by a context-free grammar.
- In a context-free grammar, we have:
  - A finite set of terminals (in our case, this will be the set of tokens)
  - A finite set of non-terminals (syntactic-variables)
  - A finite set of productions rules in the following form
    - $A \rightarrow \alpha$       where A is a non-terminal and  
    $\alpha$  is a string of terminals and non-terminals (including the empty string)
  - A start symbol (one of the non-terminal symbol)
- Example:
  - $E \rightarrow E + E \mid E - E \mid E * E \mid E / E \mid - E$
  - $E \rightarrow ( E )$
  - $E \rightarrow \text{id}$

# Derivations

$$E \Rightarrow E+E$$

- $E+E$  derives from  $E$ 
  - we can replace  $E$  by  $E+E$
  - to be able to do this, we must have a production rule  $E \rightarrow E+E$  in our grammar.

$$E \Rightarrow E+E \Rightarrow \text{id}+E \Rightarrow \text{id}+\text{id}$$

- A sequence of replacements of non-terminal symbols is called a **derivation** of  $\text{id}+\text{id}$  from  $E$ .
- In general, a derivation step is

$$\alpha A \beta \Rightarrow \alpha \gamma \beta \quad \text{if there is a production rule } A \rightarrow \gamma \text{ in our grammar}$$

where  $\alpha$  and  $\beta$  are arbitrary strings of terminal and non-terminal symbols

$$\alpha_1 \Rightarrow \alpha_2 \Rightarrow \dots \Rightarrow \alpha_n \quad (\alpha_n \text{ derives from } \alpha_1 \text{ or } \alpha_1 \text{ derives } \alpha_n)$$

$\Rightarrow$  derives in one step

$\Rightarrow$  derives in zero or more steps

$\xRightarrow{+}$  derives in one or more steps

# CFG - Terminology

- $L(G)$  is *the language of G* (the language generated by G) which is a set of sentences.
- *A sentence of  $L(G)$*  is a string of terminal symbols of G.
- If S is the start symbol of G then  
 $\omega$  is a sentence of  $L(G)$  iff  $S \xRightarrow{+} \omega$  where  $\omega$  is a string of terminals of G.
- If G is a context-free grammar,  $L(G)$  is a *context-free language*.
- Two grammars are *equivalent* if they produce the same language.
- $S \xRightarrow{*} \alpha$ 
  - If  $\alpha$  contains non-terminals, it is called as a *sentential* form of G.
  - If  $\alpha$  does not contain non-terminals, it is called as a *sentence* of G

**Note:**  $\alpha, \beta, \gamma$  and other initial Greek alphabets are used to denote string of terminals and non-terminals (sentential forms) while  $\omega$  and other last Greek alphabets denote string of only terminals (sentence)

# Derivation Example

$E \Rightarrow -E \Rightarrow -(E) \Rightarrow -(E+E) \Rightarrow -(id+E) \Rightarrow -(id+id)$

OR

$E \Rightarrow -E \Rightarrow -(E) \Rightarrow -(E+E) \Rightarrow -(E+id) \Rightarrow -(id+id)$

- At each derivation step, we can choose any of the non-terminal in the sentential form of G for the replacement.
- If we always choose the left-most non-terminal in each derivation step, this derivation is called as **left-most derivation**.
- If we always choose the right-most non-terminal in each derivation step, this derivation is called as **right-most derivation**.

# Left-Most and Right-Most Derivations

## Left-Most Derivation

$$E \xRightarrow{\text{lm}} -E \xRightarrow{\text{lm}} -(E) \xRightarrow{\text{lm}} -(E+E) \xRightarrow{\text{lm}} -(id+E) \xRightarrow{\text{lm}} -(id+id)$$

## Right-Most Derivation

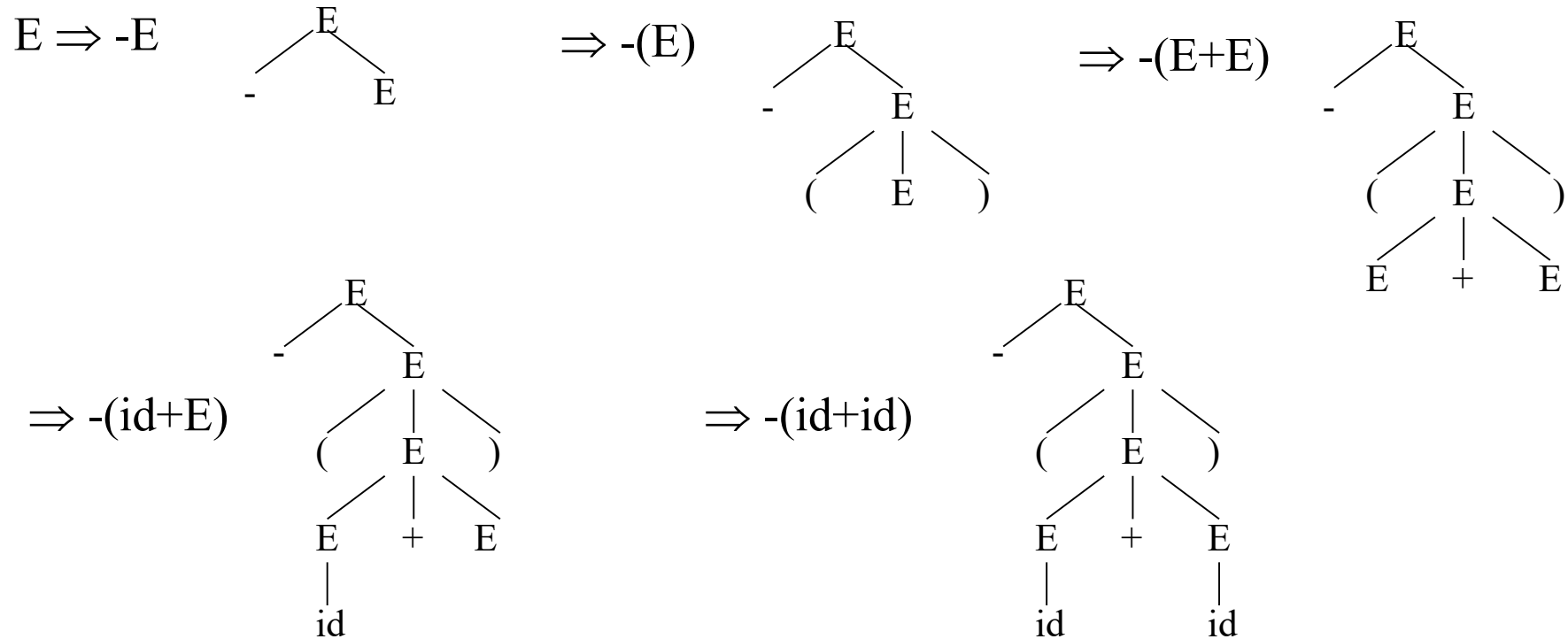
$$E \xRightarrow{\text{rm}} -E \xRightarrow{\text{rm}} -(E) \xRightarrow{\text{rm}} -(E+E) \xRightarrow{\text{rm}} -(E+id) \xRightarrow{\text{rm}} -(id+id)$$

- We will see that the top-down parsers try to find the left-most derivation of the given source program.
- We will see that the bottom-up parsers try to find the right-most derivation of the given source program in the reverse order.



# Parse Tree

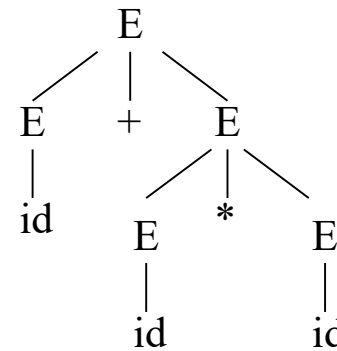
- Inner nodes of a parse tree are non-terminal symbols.
- The leaves of a parse tree are terminal symbols.
- A parse tree is a graphical representation of a derivation.



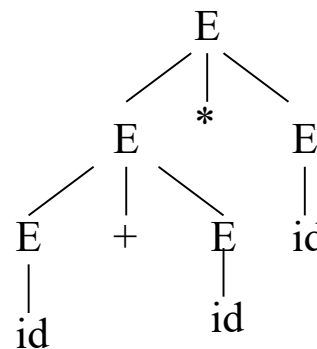
# Ambiguity

- A grammar produces more than one parse tree for a sentence is called as an *ambiguous* grammar.

$E \Rightarrow E + E \Rightarrow id + E \Rightarrow id + E * E$   
 $\Rightarrow id + id * E \Rightarrow id + id * id$



$E \Rightarrow E * E \Rightarrow E + E * E \Rightarrow id + E * E$   
 $\Rightarrow id + id * E \Rightarrow id + id * id$



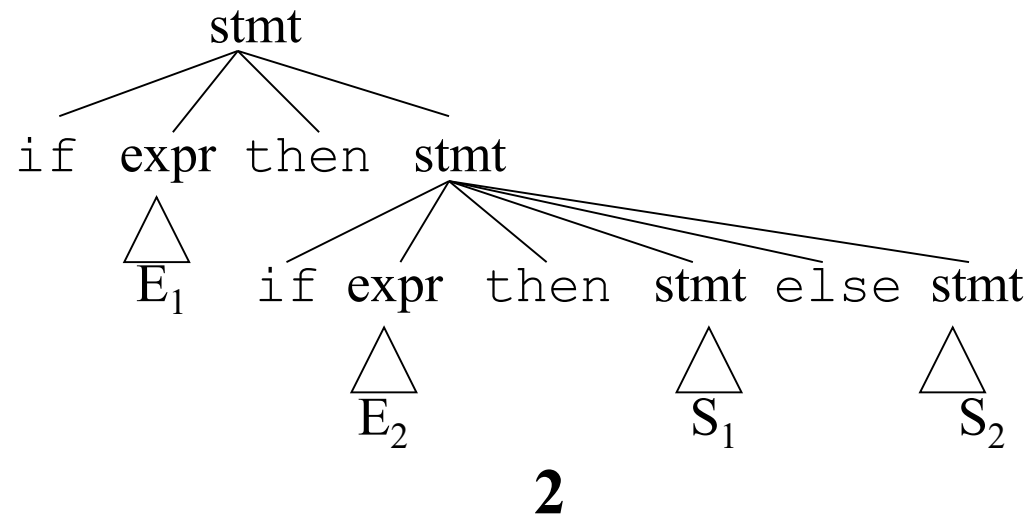
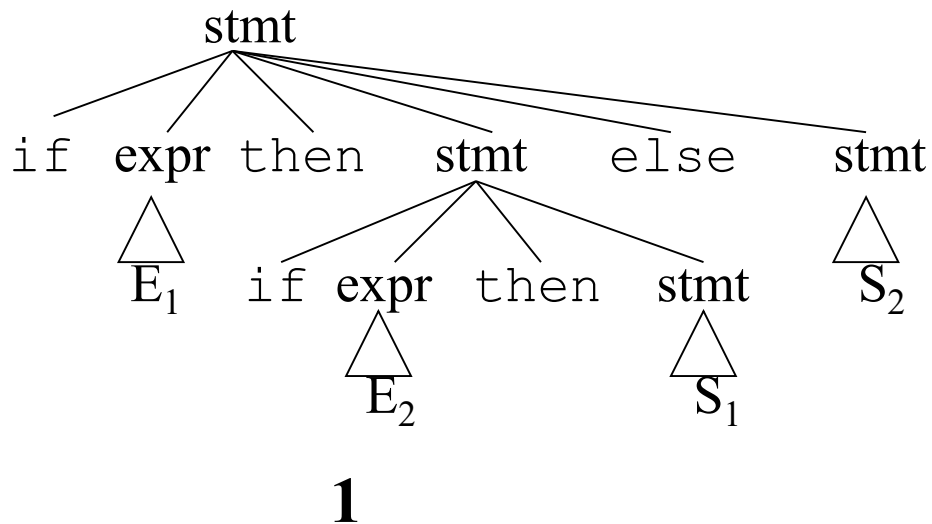
## Ambiguity (cont.)

- For the most parsers, the grammar must be unambiguous.
- unambiguous grammar
  - ➔ unique selection of the parse tree for a sentence
- We should eliminate the ambiguity in the grammar during the design phase of the compiler.
- An unambiguous grammar should be written to eliminate the ambiguity
- We must prefer one of the parse trees of a sentence (generated by an ambiguous grammar) to disambiguate that grammar to restrict to this choice

# Ambiguity (cont.)

`stmt`  $\rightarrow$  `if` `expr` `then` `stmt` |  
`if` `expr` `then` `stmt` `else` `stmt` | `otherstmts`

`if`  $E_1$  `then` `if`  $E_2$  `then`  $S_1$  `else`  $S_2$



## Ambiguity (cont.)

- We prefer the second parse tree (else matches with closest if).
- So, we must disambiguate our grammar to reflect this choice.
- The unambiguous grammar will be:

`stmt → matchedstmt | unmatchedstmt`

`matchedstmt → if expr then matchedstmt else matchedstmt | otherstmts`

`unmatchedstmt → if expr then stmt |  
                  if expr then matchedstmt else unmatchedstmt`

# Ambiguity – Operator Precedence

- Ambiguous grammars (because of ambiguous operators) can be disambiguated according to the precedence and associativity rules.

$$E \rightarrow E+E \mid E * E \mid E^E \mid \text{id} \mid (E)$$

disambiguate the grammar



precedence:

$\wedge$  (right to left)

$*$  (left to right)

$+$  (left to right)

$$E \rightarrow E+T \mid T$$

$$T \rightarrow T * F \mid F$$

$$F \rightarrow G^F \mid G$$

$$G \rightarrow \text{id} \mid (E)$$

# Left Recursion

- A grammar is *left recursive* if it has a non-terminal  $A$  such that there is a derivation:

$$A \xRightarrow{+} A\alpha \quad \text{for some string } \alpha$$

- Top-down parsing techniques **cannot** handle left-recursive grammars
- So, we must convert left-recursive grammar into an equivalent grammar which is not left-recursive.
- The left-recursion may appear in a single step of the derivation (*immediate left-recursion*) or may appear in more than one step of the derivation.

# Immediate Left-Recursion

$A \rightarrow A \alpha \mid \beta$  where  $\beta$  does not start with  $A$

$\Downarrow$

eliminate immediate left recursion

$A \rightarrow \beta A'$

$A' \rightarrow \alpha A' \mid \varepsilon$  an equivalent grammar

In general,

$A \rightarrow A \alpha_1 \mid \dots \mid A \alpha_m \mid \beta_1 \mid \dots \mid \beta_n$  where  $\beta_1 \dots \beta_n$  do not start with  $A$

$\Downarrow$

eliminate immediate left recursion

$A \rightarrow \beta_1 A' \mid \dots \mid \beta_n A'$

$A' \rightarrow \alpha_1 A' \mid \dots \mid \alpha_m A' \mid \varepsilon$  an equivalent grammar



# Immediate Left-Recursion -- Example

$$E \rightarrow E+T \mid T$$

$$T \rightarrow T*F \mid F$$

$$F \rightarrow \text{id} \mid (E)$$



eliminate immediate left recursion

$$E \rightarrow T E'$$

$$E' \rightarrow +T E' \mid \varepsilon$$

$$T \rightarrow F T'$$

$$T' \rightarrow *F T' \mid \varepsilon$$

$$F \rightarrow \text{id} \mid (E)$$

# Left-Recursion -- Problem

- A grammar cannot be immediately left-recursive, but it still can be left-recursive.
- By just eliminating the immediate left-recursion, we may not get a grammar which is not left-recursive.

$$S \rightarrow Aa \mid b$$

$A \rightarrow Sc \mid d$       This grammar is not immediately left-recursive,  
but it is still left-recursive.

$$\underline{S} \Rightarrow Aa \Rightarrow \underline{S}ca$$

$$\underline{A} \Rightarrow Sc \Rightarrow \underline{A}ac$$

or

causes to a left-recursion

- So, we must eliminate all left-recursions from our grammar

# Left-Factoring

- A predictive parser (a top-down parser without backtracking) insists that the grammar must be *left-factored*.

grammar  $\rightarrow$  a new equivalent grammar suitable for predictive parsing

$stmt \rightarrow if\ expr\ then\ stmt\ else\ stmt \mid$   
 $if\ expr\ then\ stmt$

- when we see `if`, we cannot know which production rule to choose to re-write *stmt* in the derivation.

## Left-Factoring (cont.)

- In general,

$A \rightarrow \alpha\beta_1 \mid \alpha\beta_2$       where  $\alpha$  is non-empty and the first symbols of  $\beta_1$  and  $\beta_2$  (if they have one) are different.

- when processing  $\alpha$  we cannot know whether expand

$A$  to  $\alpha\beta_1$     or

$A$  to  $\alpha\beta_2$

- But if we re-write the grammar as follows

$A \rightarrow \alpha A'$

$A' \rightarrow \beta_1 \mid \beta_2$

so, we can immediately expand  $A$  to  $\alpha A'$

# Left-Factoring -- Algorithm

- For each non-terminal  $A$  with two or more alternatives (production rules) with a common non-empty prefix, let say

$$A \rightarrow \alpha\beta_1 \mid \dots \mid \alpha\beta_n \mid \gamma_1 \mid \dots \mid \gamma_m$$

convert it into

$$A \rightarrow \alpha A' \mid \gamma_1 \mid \dots \mid \gamma_m$$

$$A' \rightarrow \beta_1 \mid \dots \mid \beta_n$$

# Left-Factoring – Example1

$$A \rightarrow \underline{a}bB \mid \underline{a}B \mid cdg \mid cdeB \mid cdfB$$



$$A \rightarrow aA' \mid \underline{cd}g \mid \underline{cde}B \mid \underline{cdf}B$$

$$A' \rightarrow bB \mid B$$



$$A \rightarrow aA' \mid cdA''$$

$$A' \rightarrow bB \mid B$$

$$A'' \rightarrow g \mid eB \mid fB$$

## Left-Factoring – Example2

$$A \rightarrow ad \mid a \mid ab \mid abc \mid b$$



$$A \rightarrow aA' \mid b$$

$$A' \rightarrow d \mid \varepsilon \mid b \mid bc$$



$$A \rightarrow aA' \mid b$$

$$A' \rightarrow d \mid \varepsilon \mid bA''$$

$$A'' \rightarrow \varepsilon \mid c$$

# Non-Context Free Language Constructs

- There are some language constructions in the programming languages which are not context-free. This means that, we cannot write a context-free grammar for these constructions.
- $L1 = \{ \omega c \omega \mid \omega \text{ is in } (a|b)^* \}$  is not context-free
  - ➔ declaring an identifier and checking whether it is declared or not later. We cannot do this with a context-free language. We need semantic analyzer (which is not context-free).
- $L2 = \{ a^n b^m c^n d^m \mid n \geq 1 \text{ and } m \geq 1 \}$  is not context-free
  - ➔ declaring two functions (one with  $n$  parameters, the other one with  $m$  parameters), and then calling them with actual parameters.



# Top-Down Parsing

- The parse tree is created top to bottom.
- Top-down parser
  - Recursive-Descent Parsing
    - Backtracking is needed (If a choice of a production rule does not work, we backtrack to try other alternatives.)
    - It is a general parsing technique, but not widely used.
    - Not efficient
    - Maybe bigger than LL(1) but may not terminate
  - Predictive Parsing
    - No backtracking
    - Efficient
    - Needs a special form of grammars (LL(1) grammars).
    - Recursive Predictive Parsing is a special form of Recursive Descent parsing without backtracking.
    - Non-Recursive (Table Driven) Predictive Parser is also known as LL(1) parser.

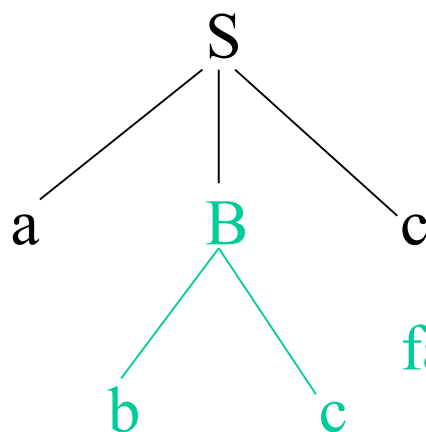
# Recursive-Descent Parsing (uses Backtracking)

- Backtracking is needed.
- It tries to find the left-most derivation.

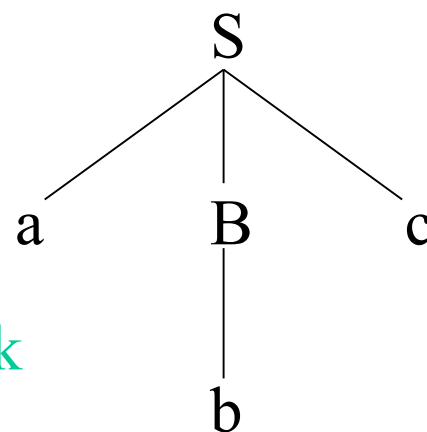
$S \rightarrow aBc$

$B \rightarrow bc \mid b$

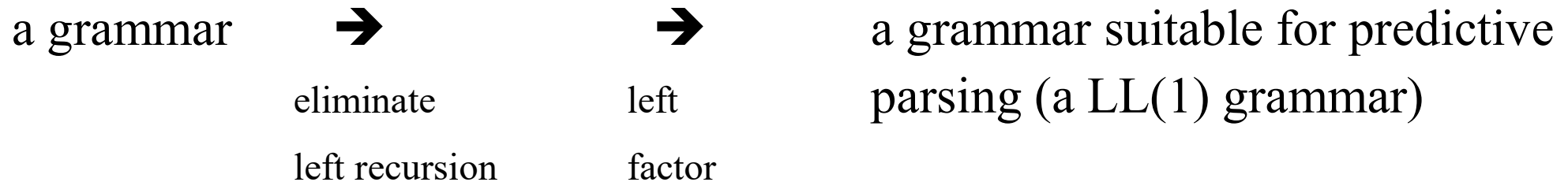
input: abc



fails, backtrack



# Predictive Parser



- When re-writing a non-terminal in a derivation step, a predictive parser can uniquely choose a production rule by just looking the current symbol in the input string.

$A \rightarrow \alpha_1 \mid \dots \mid \alpha_n$

input: ... a .....

↑  
current token

# Recursive Predictive Parsing

- Each non-terminal corresponds to a procedure.

Ex:  $A \rightarrow aBb$  (This is only the production rule for A)

```
proc A {  
    - match the current token with a, and move to the next token;  
    - call 'B';  
    - match the current token with b, and move to the next token;  
}
```

## Recursive Predictive Parsing (cont.)

$A \rightarrow aBb \mid bAB$

```
proc A {  
  case of the current token {  
    'a': - match the current token with a, and move to the next token;  
         - call 'B';  
         - match the current token with b, and move to the next token;  
    'b': - match the current token with b, and move to the next token;  
         - call 'A';  
         - call 'B';  
  }  
}
```

## Recursive Predictive Parsing (cont.)

- When to apply  $\varepsilon$ -productions.

$$A \rightarrow aA \mid bB \mid \varepsilon$$

- If all other productions fail, we should apply an  $\varepsilon$ -production. For example, if the current token is not a or b, we may apply the  $\varepsilon$ -production.
- Most correct choice: We should apply an  $\varepsilon$ -production for a non-terminal A when the current token is in the follow set of A (which terminals can follow A in the sentential forms).

# Recursive Predictive Parsing (Example)

$A \rightarrow aBe \mid cBd \mid C$

$B \rightarrow bB \mid \varepsilon$

$C \rightarrow f$

```

proc A {
  case of the current token {
    a: - match the current token with a,
        and move to the next token;
        - call B;
        - match the current token with e,
        and move to the next token;
    c: - match the current token with c,
        and move to the next token;
        - call B;
        - match the current token with d,
        and move to the next token;
    f: - call C
  }
}
  
```

**first set of C** (points to 'f')

```

proc C {
  match the current token with f,
  and move to the next token;
}
  
```

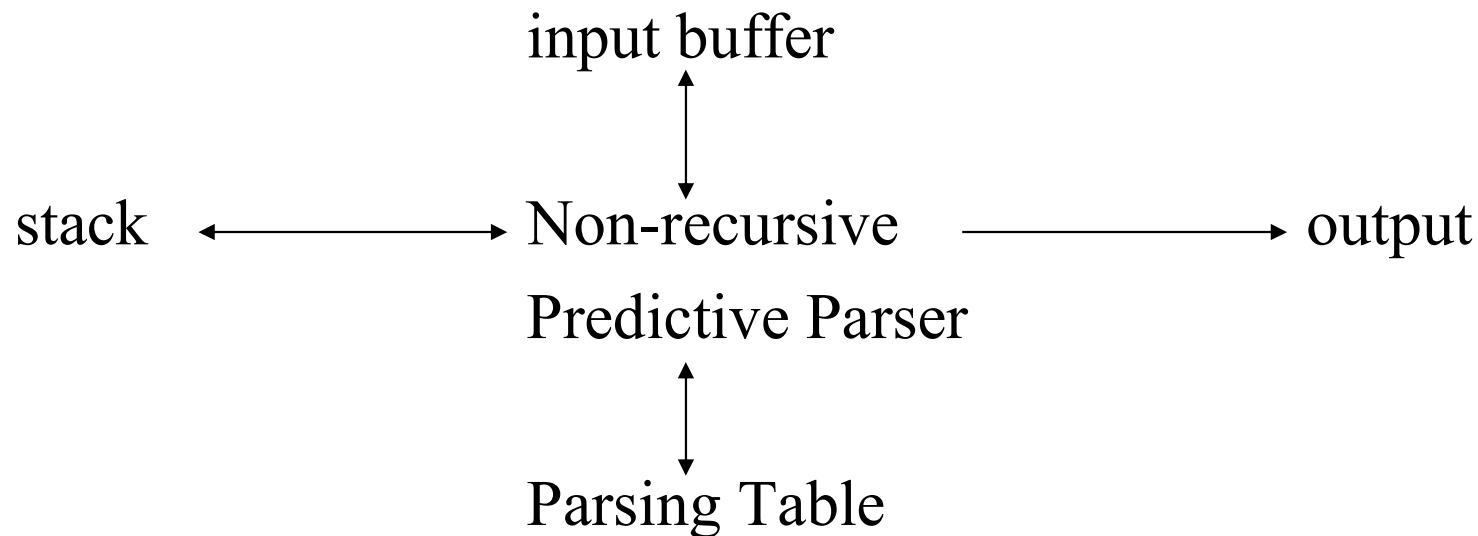
```

proc B {
  case of the current token {
    b: - match the current token with b,
        and move to the next token;
        - call B
    e,d: do nothing
  }
}
  
```

**follow set of B** (points to 'e,d')

# Non-Recursive Predictive Parsing -- LL(1) Parser

- Non-Recursive predictive parsing is a table-driven parser.
- It is a top-down parser.
- It is also known as LL(1) Parser.





# LL(1) Parser

## input buffer

- our string to be parsed. We will assume that its end is marked with a special symbol \$.

## output

- a production rule representing a step of the derivation sequence (left-most derivation) of the string in the input buffer.

## stack

- contains the grammar symbols
- at the bottom of the stack, there is a special end marker symbol \$.
- initially the stack contains only the symbol \$ and the starting symbol S.       $\$S \leftarrow$  initial stack
- when the stack is emptied (ie. only \$ left in the stack), the parsing is completed.

## parsing table

- a two-dimensional array  $M[A,a]$
- each row is a non-terminal symbol
- each column is a terminal symbol or the special symbol \$
- each entry holds a production rule.

# LL(1) Parser – Parser Actions

- The symbol at the top of the stack (say  $X$ ) and the current symbol in the input string (say  $a$ ) determine the parser action.
- There are four possible parser actions.
  1. If  $X$  and  $a$  are  $\$$   $\rightarrow$  parser halts (successful completion)
  2. If  $X$  and  $a$  are the same terminal symbol (different from  $\$$ )  
 $\rightarrow$  parser pops  $X$  from the stack and moves the next symbol in the input buffer.
  3. If  $X$  is a non-terminal  
 $\rightarrow$  parser looks at the parsing table entry  $M[X,a]$ . If  $M[X,a]$  holds a production rule  $X \rightarrow Y_1 Y_2 \dots Y_k$ , it pops  $X$  from the stack and pushes  $Y_k, Y_{k-1}, \dots, Y_1$  into the stack. The parser also outputs the production rule  $X \rightarrow Y_1 Y_2 \dots Y_k$  to represent a step of the derivation.
  4. none of the above  $\rightarrow$  error
    - all empty entries in the parsing table are errors.
    - If  $X$  is a terminal symbol different from  $a$ , this is also an error case.

# LL(1) Parser – Example1

$S \rightarrow aBa$

$B \rightarrow bB \mid \varepsilon$

	a	b	\$
S	$S \rightarrow aBa$		
B	$B \rightarrow \varepsilon$	$B \rightarrow bB$	

LL(1) Parsing  
Table

stack

\$S

\$aBa

\$aB

\$aBb

\$aB

\$aBb

\$aB

\$a

\$

input

abba\$

abba\$

bba\$

bba\$

ba\$

ba\$

a\$

a\$

\$

output

$S \rightarrow aBa$

$B \rightarrow bB$

$B \rightarrow bB$

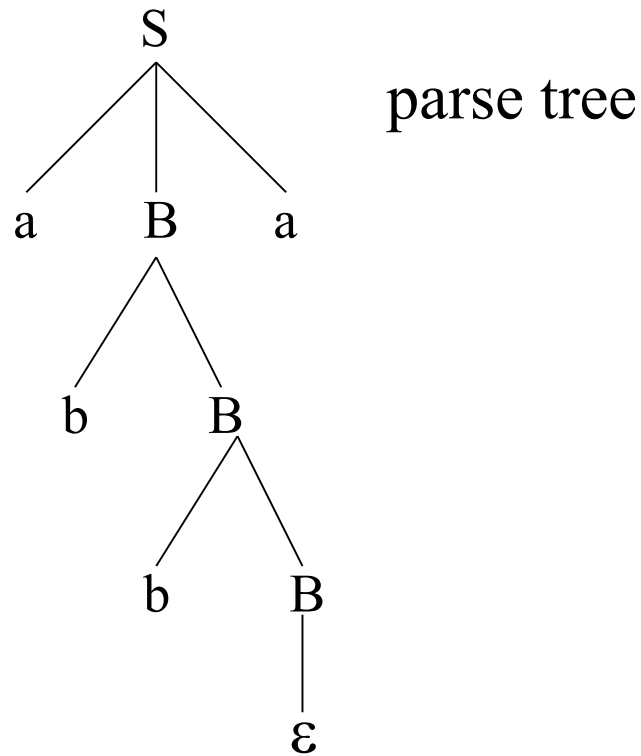
$B \rightarrow \varepsilon$

accept, successful completion

## LL(1) Parser – Example1 (cont.)

Outputs:  $S \rightarrow aBa$      $B \rightarrow bB$      $B \rightarrow bB$      $B \rightarrow \varepsilon$

Derivation(left-most):  $S \Rightarrow aBa \Rightarrow abBa \Rightarrow abbBa \Rightarrow abba$



# LL(1) Parser – Example2

$E \rightarrow TE'$

$E' \rightarrow +TE' \mid \varepsilon$

$T \rightarrow FT'$

$T' \rightarrow *FT' \mid \varepsilon$

$F \rightarrow (E) \mid id$

	id	+	*	(	)	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow id$			$F \rightarrow (E)$		

# LL(1) Parser – Example2

<u>stack</u>	<u>input</u>	<u>output</u>
\$E	id+id\$	$E \rightarrow TE'$
\$E'T	id+id\$	$T \rightarrow FT'$
\$E'T'F	id+id\$	$F \rightarrow id$
\$E'T'id	id+id\$	
\$E'T'	+id\$	$T' \rightarrow \varepsilon$
\$E'	+id\$	$E' \rightarrow +TE'$
\$E'T+	+id\$	
\$E'T	id\$	$T \rightarrow FT'$
\$E'T'F	id\$	$F \rightarrow id$
\$E'T'id	id\$	
\$E'T'	\$	$T' \rightarrow \varepsilon$
\$E'	\$	$E' \rightarrow \varepsilon$
\$	\$	accept

# Constructing LL(1) Parsing Tables

- Two functions are used in the construction of LL(1) parsing tables:
  - FIRST FOLLOW
- **FIRST( $\alpha$ )** is a set of the terminal symbols which occur as first symbols in strings derived from  $\alpha$  where  $\alpha$  is any string of grammar symbols.
- if  $\alpha$  derives to  $\varepsilon$ , then  $\varepsilon$  is also in FIRST( $\alpha$ ) .
- **FOLLOW(A)** is the set of the terminals which occur immediately after (follow) the *non-terminal*  $A$  in the strings derived from the starting symbol.
  - a terminal  $a$  is in FOLLOW(A) if  $S \xRightarrow{*} \alpha A a \beta$
  - \$ is in FOLLOW(A) if  $S \xRightarrow{*} \alpha A$

# Compute FIRST for Any String X

- If X is a terminal symbol  $\rightarrow$   $\text{FIRST}(X) = \{X\}$
- If X is a non-terminal symbol and  $X \rightarrow \varepsilon$  is a production rule  
 $\rightarrow$   $\varepsilon$  is in  $\text{FIRST}(X)$ .
- If X is a non-terminal symbol and  $X \rightarrow Y_1 Y_2 \dots Y_n$  is a production rule  
 $\rightarrow$  if a terminal **a** in  $\text{FIRST}(Y_i)$  and  $\varepsilon$  is in all  $\text{FIRST}(Y_j)$  for  $j=1, \dots, i-1$  then **a** is in  $\text{FIRST}(X)$ .  
 $\rightarrow$  if  $\varepsilon$  is in all  $\text{FIRST}(Y_j)$  for  $j=1, \dots, n$  then  $\varepsilon$  is in  $\text{FIRST}(X)$ .
- If X is  $\varepsilon$   $\rightarrow$   $\text{FIRST}(X) = \{\varepsilon\}$
- If X is  $Y_1 Y_2 \dots Y_n$   
 $\rightarrow$  if a terminal **a** in  $\text{FIRST}(Y_i)$  and  $\varepsilon$  is in all  $\text{FIRST}(Y_j)$  for  $j=1, \dots, i-1$  then **a** is in  $\text{FIRST}(X)$ .  
 $\rightarrow$  if  $\varepsilon$  is in all  $\text{FIRST}(Y_j)$  for  $j=1, \dots, n$  then  $\varepsilon$  is in  $\text{FIRST}(X)$ .



# FIRST Example

$$E \rightarrow TE'$$

$$E' \rightarrow +TE' \mid \varepsilon$$

$$T \rightarrow FT'$$

$$T' \rightarrow *FT' \mid \varepsilon$$

$$F \rightarrow (E) \mid \text{id}$$

$$\text{FIRST}(F) = \{ (, \text{id} \}$$

$$\text{FIRST}(T') = \{ *, \varepsilon \}$$

$$\text{FIRST}(T) = \{ (, \text{id} \}$$

$$\text{FIRST}(E') = \{ +, \varepsilon \}$$

$$\text{FIRST}(E) = \{ (, \text{id} \}$$

$$\text{FIRST}(TE') = \{ (, \text{id} \}$$

$$\text{FIRST}(+TE') = \{ + \}$$

$$\text{FIRST}(\varepsilon) = \{ \varepsilon \}$$

$$\text{FIRST}(FT') = \{ (, \text{id} \}$$

$$\text{FIRST}(*FT') = \{ * \}$$

$$\text{FIRST}(\varepsilon) = \{ \varepsilon \}$$

$$\text{FIRST}((E)) = \{ ( \}$$

$$\text{FIRST}(\text{id}) = \{ \text{id} \}$$

## Compute FOLLOW (for non-terminals)

- If  $S$  is the start symbol  $\rightarrow$   $\$$  is in  $\text{FOLLOW}(S)$
- if  $A \rightarrow \alpha B \beta$  is a production rule  
 $\rightarrow$  everything in  $\text{FIRST}(\beta)$  is  $\text{FOLLOW}(B)$  except  $\epsilon$
- If (  $A \rightarrow \alpha B$  is a production rule ) or  
(  $A \rightarrow \alpha B \beta$  is a production rule and  $\epsilon$  is in  $\text{FIRST}(\beta)$  )  
 $\rightarrow$  everything in  $\text{FOLLOW}(A)$  is in  $\text{FOLLOW}(B)$ .

We apply these rules until nothing more can be added to any follow set.

## FOLLOW Example

$$E \rightarrow TE'$$

$$E' \rightarrow +TE' \mid \varepsilon$$

$$T \rightarrow FT'$$

$$T' \rightarrow *FT' \mid \varepsilon$$

$$F \rightarrow (E) \mid \text{id}$$

$$\text{FOLLOW}(E) = \{ \$, ) \}$$

$$\text{FOLLOW}(E') = \{ \$, ) \}$$

$$\text{FOLLOW}(T) = \{ +, ), \$ \}$$

$$\text{FOLLOW}(T') = \{ +, ), \$ \}$$

$$\text{FOLLOW}(F) = \{ +, *, ), \$ \}$$

# Constructing LL(1) Parsing Table -- Algorithm

- for each production rule  $A \rightarrow \alpha$  of a grammar  $G$ 
  - for each terminal  $a$  in  $\text{FIRST}(\alpha)$ 
    - ➔ add  $A \rightarrow \alpha$  to  $M[A,a]$
  - If  $\epsilon$  in  $\text{FIRST}(\alpha)$ 
    - ➔ for each terminal  $a$  in  $\text{FOLLOW}(A)$  add  $A \rightarrow \alpha$  to  $M[A,a]$
  - If  $\epsilon$  in  $\text{FIRST}(\alpha)$  and  $\$$  in  $\text{FOLLOW}(A)$ 
    - ➔ add  $A \rightarrow \alpha$  to  $M[A,\$]$
- All other undefined entries of the parsing table are error entries.

# Constructing LL(1) Parsing Table -- Example

$E \rightarrow TE'$	$FIRST(TE') = \{ (, id \}$	$\rightarrow E \rightarrow TE' \text{ into } M[E, (] \text{ and } M[E, id]$
$E' \rightarrow +TE'$	$FIRST(+TE') = \{ + \}$	$\rightarrow E' \rightarrow +TE' \text{ into } M[E', +]$
$E' \rightarrow \varepsilon$	$FIRST(\varepsilon) = \{ \varepsilon \}$ but since $\varepsilon$ in $FIRST(\varepsilon)$ and $FOLLOW(E') = \{ \$, ) \}$	$\rightarrow$ none $\rightarrow E' \rightarrow \varepsilon \text{ into } M[E', \$] \text{ and } M[E', )]$
$T \rightarrow FT'$	$FIRST(FT') = \{ (, id \}$	$\rightarrow T \rightarrow FT' \text{ into } M[T, (] \text{ and } M[T, id]$
$T' \rightarrow *FT'$	$FIRST(*FT') = \{ * \}$	$\rightarrow T' \rightarrow *FT' \text{ into } M[T', *]$
$T' \rightarrow \varepsilon$	$FIRST(\varepsilon) = \{ \varepsilon \}$ but since $\varepsilon$ in $FIRST(\varepsilon)$ and $FOLLOW(T') = \{ \$, ), + \}$	$\rightarrow$ none $\rightarrow T' \rightarrow \varepsilon \text{ into } M[T', \$], M[T', )] \text{ and } M[T', +]$
$F \rightarrow (E)$	$FIRST((E)) = \{ ( \}$	$\rightarrow F \rightarrow (E) \text{ into } M[F, (]$
$F \rightarrow id$	$FIRST(id) = \{ id \}$	$\rightarrow F \rightarrow id \text{ into } M[F, id]$

# LL(1) Grammars

- A grammar whose parsing table has no multiply-defined entries is said to be LL(1) grammar.

one input symbol used as a look-head symbol to determine parser action  
↓  
LL(1) — left most derivation  
↑  
input scanned from left to right

- The parsing table of a grammar may contain more than one production rule. In this case, we say that it is not a LL(1) grammar.

# A Grammar which is not LL(1)

$S \rightarrow i C t S E \mid a$

$E \rightarrow e S \mid \varepsilon$

$C \rightarrow b$

$\text{FOLLOW}(S) = \{ \$, e \}$

$\text{FOLLOW}(E) = \{ \$, e \}$

$\text{FOLLOW}(C) = \{ t \}$

$\text{FIRST}(iCtSE) = \{ i \}$

$\text{FIRST}(a) = \{ a \}$

$\text{FIRST}(eS) = \{ e \}$

$\text{FIRST}(\varepsilon) = \{ \varepsilon \}$

$\text{FIRST}(b) = \{ b \}$

	<b>a</b>	<b>b</b>	<b>e</b>	<b>i</b>	<b>t</b>	<b>\$</b>
<b>S</b>	$S \rightarrow a$			$S \rightarrow iCtSE$		
<b>E</b>			$E \rightarrow e S$ $E \rightarrow \varepsilon$			$E \rightarrow \varepsilon$
<b>C</b>		$C \rightarrow b$				

two production rules for  $M[E, e]$

Problem  $\rightarrow$  ambiguity

## A Grammar which is not LL(1) (cont.)

- What do we have to do if the resulting parsing table contains multiply defined entries?
  - If we didn't eliminate left recursion, eliminate the left recursion in the grammar.
  - If the grammar is not left factored, we have to left factor the grammar.
  - If its (new grammar's) parsing table still contains multiply defined entries, that grammar is ambiguous or it is inherently not a LL(1) grammar.
- A left recursive grammar cannot be a LL(1) grammar.
  - $A \rightarrow A\alpha \mid \beta$ 
    - ➔ any terminal that appears in  $\text{FIRST}(\beta)$  also appears  $\text{FIRST}(A\alpha)$  because  $A\alpha \Rightarrow \beta\alpha$ .
    - ➔ If  $\beta$  is  $\epsilon$ , any terminal that appears in  $\text{FIRST}(\alpha)$  also appears in  $\text{FIRST}(A\alpha)$  and  $\text{FOLLOW}(A)$ .
- A grammar is not left factored, it cannot be a LL(1) grammar
  - $A \rightarrow \alpha\beta_1 \mid \alpha\beta_2$ 
    - ➔ any terminal that appears in  $\text{FIRST}(\alpha\beta_1)$  also appears in  $\text{FIRST}(\alpha\beta_2)$ .
- An ambiguous grammar cannot be a LL(1) grammar.



# Error Recovery in Predictive Parsing

- An error may occur in the predictive parsing (LL(1) parsing)
  - if the terminal symbol on the top of stack does not match with the current input symbol.
  - if the top of stack is a non-terminal  $A$ , the current input symbol is  $a$ , and the parsing table entry  $M[A,a]$  is empty.
- What should the parser do in an error case?
  - The parser should be able to give an error message (as much as possible meaningful error message).
  - It should be recover from that error case, and it should be able to continue the parsing with the rest of the input.

# Error Recovery Techniques

- **Panic-Mode Error Recovery**
  - Skipping the input symbols until a synchronizing token is found.
- **Phrase-Level Error Recovery**
  - Each empty entry in the parsing table is filled with a pointer to a specific error routine to take care that error case.
- **Error-Productions**
  - If we have a good idea of the common errors that might be encountered, we can augment the grammar with productions that generate erroneous constructs.
  - When an error production is used by the parser, we can generate appropriate error diagnostics.
  - Since it is almost impossible to know all the errors that can be made by the programmers, this method is not practical.
- **Global-Correction**
  - Ideally, we we would like a compiler to make as few change as possible in processing incorrect inputs.
  - We have to globally analyze the input to find the error.
  - This is an expensive method, and it is not in practice.

# Panic-Mode Error Recovery in LL(1) Parsing

- In panic-mode error recovery, we skip all the input symbols until a synchronizing token is found.
- What is the synchronizing token?
  - All the terminal-symbols in the follow set of a non-terminal can be used as a synchronizing token set for that non-terminal.
- So, a simple panic-mode error recovery for the LL(1) parsing:
  - All the empty entries are marked as ***synch*** to indicate that the parser will skip all the input symbols until a symbol in the follow set of the non-terminal A which on the top of the stack. Then the parser will pop that non-terminal A from the stack. The parsing continues from that state.
  - To handle unmatched terminal symbols, the parser pops that unmatched terminal symbol from the stack and it issues an error message saying that that unmatched terminal is inserted.

# Panic-Mode Error Recovery - Example

$S \rightarrow AbS \mid e \mid \varepsilon$

$A \rightarrow a \mid cAd$

$\text{FOLLOW}(S) = \{\$ \}$

$\text{FOLLOW}(A) = \{b, d\}$

	a	b	c	d	e	\$
S	$S \rightarrow AbS$	<i>sync</i>	$S \rightarrow AbS$	<i>sync</i>	$S \rightarrow e$	$S \rightarrow \varepsilon$
A	$A \rightarrow a$	<i>sync</i>	$A \rightarrow cAd$	<i>sync</i>	<i>sync</i>	<i>sync</i>

<u>stack</u>	<u>input</u>	<u>output</u>
\$S	aab\$	$S \rightarrow AbS$
\$SbA	aab\$	$A \rightarrow a$
\$Sba	aab\$	
\$Sb	ab\$	Error: missing b, inserted
\$S	ab\$	$S \rightarrow AbS$
\$SbA	ab\$	$A \rightarrow a$
\$Sba	ab\$	
\$Sb	b\$	
\$S	\$	$S \rightarrow \varepsilon$
\$	\$	accept

<u>stack</u>	<u>input</u>	<u>output</u>
\$S	ceadb\$	$S \rightarrow AbS$
\$SbA	ceadb\$	$A \rightarrow cAd$
\$SbdAc	ceadb\$	
\$SbdA	eadb\$	Error: unexpected e (illegal A)
(Remove all input tokens until first b or d, pop A)		
\$Sbd	db\$	
\$Sb	b\$	
\$S	\$	$S \rightarrow \varepsilon$
\$	\$	accept

# Phrase-Level Error Recovery

- Each empty entry in the parsing table is filled with a pointer to a special error routine which will take care that error case.
- These error routines may:
  - change, insert, or delete input symbols.
  - issue appropriate error messages
  - pop items from the stack.
- We should be careful when we design these error routines, because we may put the parser into an infinite loop.