



Normalization

Second Normal Form

- A relation is in the second normal form if it fulfills the following two requirements:
 - It is in **first normal form**
 - It does not have any **non-prime attribute** that is **functionally dependent** on any **proper subset** of any **candidate key** of the relation
- **A non-prime attribute of a relation** is an attribute that is not a part of any candidate key of the relation
- Put simply, a relation is in 2NF if it is in 1NF and every non-prime attribute of the relation is dependent on the whole of every candidate key
- Note that it does not put any restriction on the non-prime to non-prime attribute dependency; that is addressed in **third normal form**

Second Normal Form

- Example:
 - Consider following functional dependencies in relation R (A, B, C, D)
 - $AB \rightarrow C$ [A and B together determine C]
 - $C \rightarrow D$ [C determines D]
 - In the above relation, AB is the only candidate key and there is no partial dependency, i.e., any proper subset of AB doesn't determine any non-prime attribute
- **A normal form of historical significance:**
 - “
 - You may have noted that we skipped second normal form
 - It is of historical significance only and, in practice, one of third normal form or BCNF is always a better choice
 - First normal form pertains to attribute domains, not decomposition
 - ”

Lossless Decomposition

- We can use functional dependencies to show when certain decomposition are lossless
- For the case of $R = (R_1, R_2)$, we require that for all possible relations r on schema R
$$r = \Pi_{R_1}(r) \bowtie \Pi_{R_2}(r)$$
- A decomposition of R into R_1 and R_2 is lossless decomposition if at least one of the following dependencies is in F^+ :

$$R_1 \cap R_2 \rightarrow R_1$$

$$R_1 \cap R_2 \rightarrow R_2$$

- The above functional dependencies are a sufficient condition for lossless join decomposition
- The dependencies are a necessary condition only if all constraints are functional dependencies

Example

- $R = (A, B, C)$
 $F = \{A \rightarrow B, B \rightarrow C\}$
- $R_1 = (A, B), R_2 = (B, C)$
 - Lossless decomposition:

$$R_1 \cap R_2 = \{B\} \text{ and } B \rightarrow BC$$

- $R_1 = (A, B), R_2 = (A, C)$
 - Lossless decomposition:

$$R_1 \cap R_2 = \{A\} \text{ and } A \rightarrow AB$$

- *Note:*
 - $B \rightarrow BC$ is a shorthand notation for $B \rightarrow \{B, C\}$

Boyce-Codd Normal Form

- A relation schema R is in BCNF with respect to a set F of functional dependencies if for all functional dependencies in F^+ of the form

$$\alpha \rightarrow \beta$$

where $\alpha \subseteq R$ and $\beta \subseteq R$, at least one of the following holds:

- $\alpha \rightarrow \beta$ is trivial (i.e., $\beta \subseteq \alpha$)
 - α is a superkey for R
- *Example schema not in BCNF*
 - *in_dep(ID, name, salary, dept_name, building, budget)*
 - *Because dept_name \rightarrow building, budget holds on in_dep, but dept_name is not a superkey*

Decomposing a Schema into BCNF

- Let R be a schema R that is not in BCNF
- Let $\alpha \rightarrow \beta$ be the FD that causes a violation of BCNF
- We decompose R into:
 - $(\alpha \cup \beta)$
 - $(R - (\beta - \alpha))$
- In our example of in_dep ,
 - $\alpha = dept_name$
 - $\beta = building, budget$
 - $dept_name \rightarrow building, budget$
- and in_dep is replaced by
 - $(\alpha \cup \beta) = (dept_name, building, budget)$
 - $dept_name \rightarrow building, budget$
 - $(R - (\beta - \alpha)) = (ID, name, dept_name, salary)$
 - $ID \rightarrow name, salary, dept_name$

Example

- $R = (A, B, C)$
 $F = \{A \rightarrow B, B \rightarrow C\}$
- $R_1 = (A, B), \quad R_2 = (B, C)$
 - Lossless-join decomposition:

$$R_1 \cap R_2 = \{B\} \quad \text{and} \quad B \rightarrow BC$$

- Dependency preserving
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- $R_1 = (A, B), \quad R_2 = (A, C)$
 - Lossless-join decomposition:
 - Not dependency preserving
 (cannot check $B \rightarrow C$ without computing $R_1 \bowtie R_2$)

BCNF and Dependency Preservation

- It is not always possible to achieve both BCNF and dependency preservation
- Consider a schema: *dept_advisor(s_ID, i_ID, department_name)*

- With function dependencies:

$$\begin{aligned}i_ID &\rightarrow dept_name \\s_ID, dept_name &\rightarrow i_ID\end{aligned}$$

- In the above design, we are forced to repeat the department name once for each time an instructor participates in a *dept_advisor* relationship
- dept_advisor* is not in BCNF
 - i_ID* is not a superkey
- To fix this, we need to decompose *dept_advisor*
- Any decomposition of *dept_advisor* will not include all the attributes in
$$s_ID, dept_name \rightarrow i_ID$$
- Thus, the composition is NOT be dependency preserving

Dependency Preservation

- Testing functional dependency constraints each time the database is updated can be costly
- It is useful to design the database in a way that constraints can be tested efficiently
- If testing a functional dependency can be done by considering just one relation, then the cost of testing this constraint is low
- When decomposing a relation it is possible that it is no longer possible to do the testing without having to perform a Cartesian Product
- A decomposition that makes it computationally hard to enforce functional dependency is said to be NOT **dependency preserving**

BCNF and Dependency Preservation

- Constrains, including functional dependencies, are costly to check in practice unless they pertain to only one relation
- If it is sufficient to test only those dependencies on each individual relation of a decomposition in order to ensure that **all** functional dependencies hold, then the decomposition is dependency preserving
- Because it is not always possible to achieve both BCNF and dependency preservation, we consider a weaker normal form, known as *third normal form*

Next Lecture

Normalization

Thank you for your attention...

Any question?

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