IT300 Assignment 2

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TOPIC: STABLE MATCHING AND

DIVIDE & CONQUER

NOTE: Codes have been put as multiple continued images. Please follow via line numbers if it is difficult to read.

Q1. Implementation of a stable marriage problem.

SOLUTION:

```
    Men will propose to women in this program
    There can be multiple perfect matches, one of them is computed

unordered map<string, int> id;
void matching(int n,vector<string> people,vector<vector<int>>> preference)
    vector < bool > engaged(n, false); // stores whether a man has been engaged or not int free=n; //number of free men left
    while(free>0) //until all men have been paired
         int man;//find the man who is not engaged
              if(!engaged[i])
                  man=i:
         for(int i=0;i<n;i++)
             if(engaged[man]) break;// if he's already engaged
             if(partner[preference[man][i]-n]==-1)
                  //engage both of them
                  partner[preference[man][i]-n] = man;
                  engaged[man]=true;
                  int prev_man = partner[preference[man][i]-n]; //the man shes engaged with
                  int temp;
                  for(int j=0;j<n;j++)
                       if(preference[preference[man][i]][j]==prev_man or preference[preference[man][i]][j]==man)
                           temp = preference[preference[man][i]][j];
```

```
partner[preference[man][i]-n] = man;
                            engaged[prev_man] = false;
engaged[man] = true;
//Final answer is stored in our parnter array
cout<<"\nFINAL MATCHING IS: (Format: (woman,man)):\n";</pre>
for(int i=0;i<n;i++)
int n;
cout<<"Number of men/women: ";</pre>
vector-string> people(2*n);
cout<="Enter names of men ("<<n<" space seperated strings):\n";
for(int i=0;i<n;i++) cin>people[i];
cout<="Enter names of women ("<n<<" space seperated strings):\n";
for(int i=0;i<n;i++) cin>people[i+n];
//assign ids to men and women in order
for(int i=0;i<2*n;i++)</pre>
       id[people[i]]=i;
//Stores preferences of men and women in order vector<vector<int>> preference(2*n,vector<int> (n,-1)); cout<<"\nEnter preference list of MEN.. \nNOTE:("<<n<" Space seperated strings of women from highest to lowest preference)\n";
       string sender=people[i];
cout<="Preference list of "<<sender<<":\n";
for(int j=0;j<n;j++)</pre>
              string pref;
              cin>>pref;
preference[id[sender]][j]=id[pref];
 cout<<"\nEnter preference list of WOMEN.. \nNOTE:("<<n<<" Space seperated strings of men from highest to lowest preference)\n";
for(int i=n;i<2*n;i++)</pre>
       string receiver=people[i];
cout<<"Preference list of "<<receiver<<":\n";
for(int j=0;j<n;j++)</pre>
              cin>>pref;
preference[id[receiver]][j]=id[pref];
```

Fig 1. Code for Question 1 (above 3 images combined)

```
ubuntu@suyash-18-04:~/Desktop/Sem 5/IT300/Assignment2$ g++ stablemarriage.cpp
ubuntu@suyash-18-04:~/Desktop/Sem 5/IT300/Assignment2$ ./a.out
Number of men/women: 2
Enter names of men (2 space seperated strings):
m1 m2
Enter names of women (2 space seperated strings):
w1 w2
Enter preference list of MEN..
NOTE:(2 Space seperated strings of women from highest to lowest preference)
Preference list of m1:
w1 w2
Preference list of m2:
w1 w2
Enter preference list of WOMEN...
NOTE: (2 Space seperated strings of men from highest to lowest preference)
Preference list of w1:
m1 m2
Preference list of w2:
m1 m2
FINAL MATCHING IS: (Format: (woman,man)):
(w1,m1)
(w2,m2)
ubuntu@suyash-18-04:~/Desktop/Sem 5/IT300/Assignment2$
```

Fig 2: Output of Question 1

Q2. Given a set of preferences among hospitals and medical students, implement a stable matching admissions process.

SOLUTION:

```
1) This program performs stable matching for admission in hospitals in given loactions
2) Hospitals will send proposals to students in this program
3) There can be multiple perfect matches, one of them is computed
unordered_map<string, int> id;
//Function to perform stable matching void matching(int n,vector<string> shlist,vector<vector<int>>> preference)
        \begin{array}{l} \textbf{vector} < \textbf{int} > \textbf{matching(n,-1);} / \textbf{stores matched ids of students with hospitals} \\ \textbf{vector} < \textbf{stigned(n,false);} / / \textbf{stores whether a student has been assigned or not } \\ \textbf{int free=n;} / \textbf{number of free hospitals left} \\ \textbf{while(free>0)} / \textbf{until all hospitals have been paired} \\ \end{array} 
                     if(!assigned[i])
                     if(assigned[student]) break;// if he's already assigned
                     //if the student in the hospital's pref list is not assigned if(matching[preference[student][i]-n]==-1)
                            //match both of them
                            matching[preference[student][i]-n] = student;
                            assigned[student]=true;
                            int prev_student = matching[preference[student][i]-n]; //the student shes assigned with
                            int temp:
                                   if(preference[preference[student][i]][j]==prev_student or preference[preference[student][i]][j]==student)
                                          temp = preference[preference[student][i]][j];
```

```
temp = preference[preference[student][i]][j];
break;
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                                                                                                                                              matching[preference[student][i]·n] = student;
assigned[prev_student] = false;
assigned[student] = true;
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                                                       cin>=n;
vector<string> shlist(2*n);
cout<="Enter names of hospitals ("<<n<<" space seperated strings):\n";
for(int i=0;i<n;i++) cin>>shlist[i];
cout<="Enter names of students ("<<n<<" space seperated strings):\n";
for(int i=0;i<n;i++) cin>>shlist[i+n];
                                                      //assign ids to hospitals and students in order for(int i=0;i<2*n;i++) {
                                                      //Stores preferences of hospitals and students in order vector<vector=int>> preference(2*n,vector=int>> (n,-1)); cout<<**\liminstance* (n,-1): cout<**\liminstance* (n,-1): cout<*\liminstance* (n,-1):
                                                                             string sender=shlist[i];
cout<<"Preference list of "<<sender<<":\n";
for(int j=0;j<n;j++)</pre>
                                                                                                   string pref;
cin>>pref;
                                                                                string receiver=shlist[i];
cout<<"Preference list of "<<receiver<<":\n";
for(int j=0;j<n;j++)</pre>
```

Fig 3. Code for Question 2 (above 3 images combined)

```
ubuntu@suyash-18-04:~/Desktop/Sem 5/IT300/Assignment2$ g++ stablematching.cpp
ubuntu@suyash-18-04:~/Desktop/Sem 5/IT300/Assignment2$ ./a.out
Number of hospitals/students: 3
Enter names of hospitals (3 space seperated strings):
Delhi Mumbai Banglore
Enter names of students (3 space seperated strings):
Deepak Manoj Pankaj
Enter preference list of hospitals...
NOTE:(3 Space seperated strings of students from highest to lowest preference)
Preference list of Delhi:
Deepak Manoj Pankaj
Preference list of Mumbai:
Manoj Deepak Pankaj
Preference list of Banglore:
Deepak Manoj Pankaj
Enter preference list of students...
NOTE:(3 Space seperated strings of hospitals from highest to lowest preference)
Preference list of Deepak:
Mumbai Delhi Banglore
Preference list of Manoj:
Delhi Mumbai Banglore
Preference list of Pankaj:
Delhi Mumbai Banglore
FINAL MATCHING IS: (Format: (student,hospitals)):
(Deepak, Delhi)
(Manoj, Mumbai)
(Pankaj,Banglore)
ubuntu@suyash-18-04:~/Desktop/Sem 5/IT300/Assignment2$
```

Fig 4: Output of Question 2

Q3. Implementation of propose and reject algorithm using Gale-shapley approach.

SOLUTION:

The sample output given in the problem statement is a stable matching algorithm. Hence the code will remain the same in that case.

Output:

```
ubuntu@suyash-18-04:~/Desktop/Sem 5/IT300/Assignment2$ g++ stablemarriage.cpp
ubuntu@suyash-18-04:~/Desktop/Sem 5/IT300/Assignment2$ ./a.out
Number of men/women:
Enter names of men (5 space seperated strings):
Enter names of women (5 space seperated strings):
ABCDE
Enter preference list of MEN..
NOTE:(5 Space seperated strings of women from highest to lowest preference)
Preference list of V:
ABCDE
Preference list of W:
BCDAE
Preference list of X:
CDABE
Preference list of Y:
DABCE
Preference list of Z:
ABCDE
Enter preference list of WOMEN..
NOTE:(5 Space seperated strings of men from highest to lowest preference)
Preference list of A:
WXYZV
Preference list of B:
XYZVW
Preference list of C:
YZVWX
Preference list of D:
ZVWXY
Preference list of E:
VWXYZ
FINAL MATCHING IS: (Format: (woman, man)):
(A,W)
(B,X)
(C,Y)
(D,Z)
(E,V)
ubuntu@suyash-18-04:~/Desktop/Sem 5/IT300/Assignment2$
```

Fig 5. Output for Question 3

Q4. You have a shopping list, and your friend is telling you to grab them in 20 minutes. He also gives you priorities, so you need to grab them first **SOLUTION:**

```
//function to partition the array into two parts and finding correct position of pivot
int partition(vector<pair<string,int>> &list,int low,int high)
    int x=list[high].second,j=low-1;
for(int i=low;i<high;i++)</pre>
        if(list[i].second<x)
            pair<string,int> temp=list[j];
list[j]=list[i];
list[i]=temp;
    pair<string, int> temp=list[j];
    list[j]=list[high];
    list[high]=temp;
//Function to perform quicksort on the list from index low to high
void quicksort(vector<pair<string,int>> &list,int low,int high)
     if(low<high)
         int q=partition(list,low,high);
        quicksort(list,low,q-1);
        quicksort(list,q+1,high);
     int n;
     vector<pair<string, int>> list;
        string item;
         cin>>item>>priority;
         list.push back({item,priority});
         list.push back({item,priority});
      //Display results
cout<<"\nFINAL SORTED SHOPPING LIST:\n(NOTE: Format: item_name priority_value)\n";</pre>
      for(auto x:list)
```

Fig 6. Code for Question 4 (above 2 images combined)

```
ubuntu@suyash-18-04:~/Desktop/Sem 5/IT300/Assignment2$ g++ dncq1.cpp
ubuntu@suyash-18-04:~/Desktop/Sem 5/IT300/Assignment2$ ./a.out
Number of items: 6
Enter 6 items, i.e. shopping list contents:
(NOTE: Format: item name priority value)
Eggs 4
Bread 2
Milk 6
Water 3
Meat 1
Detergent 5
FINAL SORTED SHOPPING LIST:
(NOTE: Format: item name priority value)
Meat : 1
Bread : 2
Water : 3
Eggs: 4
Detergent : 5
Milk : 6
ubuntu@suyash-18-04:~/Desktop/Sem 5/IT300/Assignment2$
```

Fig 7: Output for Question 4

Q5. Suppose you had 20 years of stock market data in 300 files. you wanted to combine the files and remove duplicate data. Some of the files were not properly sorted by time. Each file was about 150MB, so you could not load all of the data into RAM at once. you only have 32GB of ram. you could use virtual memory, but it would cause lots of swapping and bring the system to its knees. How are you going to implement it?

SOLUTION:

Code:

(continued...)

```
This program takes in multiple arrays, sorts them individually,
and merges all of them together into a single array removing the duplicates
#include<bits/stdc++.h>
using namespace std;
int partition(vector<int> &a,int low,int high)
    int x=a[high],j=low-1;
for(int i=low;i<high;i++)</pre>
       if(a[i] < x)
            int temp=a[j];
           a[j]=a[i];
a[i]=temp;
    int temp=a[j];
    a[j]=a[high];
    a[high]=temp;
}
void quicksort(vector<int> &a,int low,int high)
    if(low<high)
         int q=partition(a,low,high);
        quicksort(a,low,q-1);
        quicksort(a,q+1,high);
//Function to merge to sorted arrays
vector<int> merge(vector<int> a, vector<int> b)
    int i=0,j=0;//pointers to each array
    vector<int> result;
    //merge the arrays into result
    while(i<a.size() and j<b.size())</pre>
         if(a[i]<b[j])
             if(result.size()==0) result.push_back(a[i]);
             else if(result[result.size()-1]!=a[i]) result.push back(a[i]);
```

```
i++;
              }
              else if(a[i]>b[j])
                   if(result.size()==0) result.push back(b[j]);
                   else if(result[result.size()-1]!=b[j]) result.push back(b[j]);
              }
              else
                   if(result.size()==0) result.push back(a[i]);
                   else if(result[result.size()-1]!=b[j]) result.push back(b[j]);
                   j++;
              }
          }
          //If any of the arrays is still not covered
          if(i!=a.size())
          {
              while(i<a.size())</pre>
              {
                   if(result.size()==0) result.push back(a[i]);
                   else if(result[result.size()-1]!=a[i]) result.push back(a[i]);
          else if(j!=b.size())
              while(j<b.size())
              {
                   if(result.size()==0) result.push back(b[j]);
                   else if(result[result.size()-1]!=b[j]) result.push back(b[j]);
                   j++;
              }
          return result:
      int main()
          //Take input
          cout<<"Enter number of arrays: ";</pre>
          cin>>n;
          vector<vector<int>> list;
102
          for(int i=0;i<n;i++)
103
               int size,x;
105
              vector<int> v;
106
              cout<<"Enter size of array "<<i+1<<": ";</pre>
              cin>>size;
108
               cout<<"Enter elements of the array "<<i+1<<": ";</pre>
```

```
cout<<"Enter elements of the array "<<i+1<<": ";</pre>
    for(int j=0;j<size;j++)</pre>
        cin>>x;
        v.push back(x);
    list.push back(v);
//quick sort each array
for(int i=0;i<n;i++)
    quicksort(list[i],0,list[i].size()-1);
//merge arrays pairwise
vector<int> result;
result = list[0];
for(int i=1;i<n;i++)
    result=merge(result, list[i]);
//Diplay resulting array
cout<<"FINAL SORTED AND MERGED ARRAY IS: ";</pre>
for(auto x:result) cout<<x<<" ";</pre>
cout<<endl;
```

Fig 8. Code for Question 5 (above 3 images combined)

```
ubuntu@suyash-18-04:~/Desktop/Sem 5/IT300/Assignment2$ g++ dncq2.cpp
ubuntu@suyash-18-04:~/Desktop/Sem 5/IT300/Assignment2$ ./a.out
Enter number of arrays: 3
Enter size of array 1: 4
Enter elements of the array 1: 1 9 2 5
Enter size of array 2: 3
Enter elements of the array 2: 1 1 1
Enter size of array 3: 5
Enter elements of the array 3: 7 2 5 1 3
FINAL SORTED AND MERGED ARRAY IS: 1 2 3 5 7 9
ubuntu@suyash-18-04:~/Desktop/Sem 5/IT300/Assignment2$
```

Fig 9: Output of Question 5

Q6. If you want to divide a long loaf of bread into 8 or 16 equal pieces, generally people cut it into two equal halves first and then cut each half into two equal halves again, repeating the process until you get as many pieces as you want -

8, 16, 32, or whatever. Almost nobody tries to divide the loaf into 8 pieces all at once - people can guess halves much better than eighths. Implement this.

SOLUTION:

```
This program is a divide and conquer technique to
divide a loaf of bread into a number of divisons which is user input
NOTE: Number of divisions must be a power of 2
#include<bits/stdc++.h>
using namespace std;
//Functio nto divide a partition of loaf into two parts
void divide(int div,float low, float high)
    //least possible divison reached
    if(div==1) cout<<"("<<low<<" , "<<high<<")"<<endl;
    if(div>1)
        //find middle
        float mid=(low+high)/2;
        // num divisons gets halved
        div/=2:
        //call divide on both halves
        divide(div.low.mid);
        divide(div,mid,high);
    }
int main()
    int bread len,divisions;
    cout<<"Enter the length of bread: ";
    cin>>bread len;
    cout<<"Enter the number of divisons to make: ";</pre>
    cin>>divisions;
    if(ceil(log2(divisions))!=floor(log2(divisions)))
        cout<<"Number of divisions must be power of 2!!";</pre>
        return 0;
    cout<<"\nDivisions are as follows:\n";</pre>
    divide(divisions, 0, bread len);
```

```
ubuntu@suyash-18-04:~/Desktop/Sem 5/IT300/Assignment2$ g++ dncq3.cpp
ubuntu@suyash-18-04:~/Desktop/Sem 5/IT300/Assignment2$ ./a.out
Enter the length of bread: 10
Enter the number of divisons to make: 4

Divisions are as follows:
(0 , 2.5)
(2.5 , 5)
(5 , 7.5)
(7.5 , 10)
ubuntu@suyash-18-04:~/Desktop/Sem 5/IT300/Assignment2$ ./a.out
Enter the length of bread: 10
Enter the number of divisons to make: 5
Number of divisions must be power of 2!!
ubuntu@suyash-18-04:~/Desktop/Sem 5/IT300/Assignment2$
```

Q7. Use the divide-and-conquer integer multiplication algorithm to multiply the two binary integers 10011011 and 10111010

SOLUTION:

Code:

(continued...)

```
This program performs binary multiplication of two binary numbers using divide and conquer techinque % \left( 1\right) =\left( 1\right) +\left( 1\right
using namespace std;
#define mod 100000007
typedef long long int ll;
  //Compute power a^b efficiently
ll pow(ll a,ll b)
                                          ll res=1;
while(b>0)
                                                                                     if(b%2==1) res=(res*a)%mod;
a=(a*a)%mod;
  //Function to make the two strings of equal length (append zeros at start if not) int same_lengths(string &s1, string &s2) {
                                          //append zeros to smaller string
if (n1<n2)</pre>
                                              }
else if(n1>n2)
                                                                                       for(int i=0;i<n1-n2;i++) s2='0'+s2;
  //Function to perform addition of two binary numbers string binary_addition(string s1,string s2) \,
                                              string result; //stores final added result
                                                                                     int a=s1[i]-'0';
int b=s2[i]-'0';
int s=(a^b^c)+'0'; //sum of three bits
result = (char)s + result;
```

```
int s=(a^b^c)+'0'; //sum of three bits
result = (char)s + result;
    if(n==0) return 0;
else if(n==1) //single digit binary numbers
    //calculating number of digits in two halves int num_left = n/2; int num_right = n - num_left;
   //dividing binary numbers in two halves
string s1_left = s1.substr(0, num_left);
string s1_right = s1.substr(num_left, num_right);
    string s2_left = s2.substr(0, num_left);
string s2_right = s2.substr(num_left, num_right);
    //perform multiplication of the halves
ll product_left = binary_multiplication(s1_left, s2_left);
ll product_right = binary_multiplication(s1_right, s2_right);
    //addition of left and right halves
string sllr = binary_addition(s1_left, s1_right);
string s2lr = binary_addition(s2_left, s2_right);
    //calculate final result 
 ll result = product_left *(pow(2,2*num\_right)) + (product_mid - product_left - product_right)*(pow(2,num\_right)) + product_right;
int main()
     //Take input
string num1,num2;
cout<<"Enter binary number 1: ";</pre>
     cin>>num1;
cout<<"Enter binary number 2: ";</pre>
     //Display final result
ll res = binary_multiplication(num1,num2);
cout<<"\nFINAL RESULT AFTER MULTIPLICATION: "<<res<<endl;</pre>
```

```
ubuntu@suyash-18-04:~/Desktop/Sem 5/IT300/Assignment2$ g++ dncq4.cpp
ubuntu@suyash-18-04:~/Desktop/Sem 5/IT300/Assignment2$ ./a.out
Enter binary number 1: 10011011
Enter binary number 2: 10111010

FINAL RESULT AFTER MULTIPLICATION: 28830
ubuntu@suyash-18-04:~/Desktop/Sem 5/IT300/Assignment2$
```