

# PUNE INSTITUTE OF COMPUTER TECHNOLOGY

## IT Department

### CGL Assignment 3

**Name:** Suyash More

**Class:**SE9

**Roll No:** 23148

**Batch:** G9

---

#### **Title:**

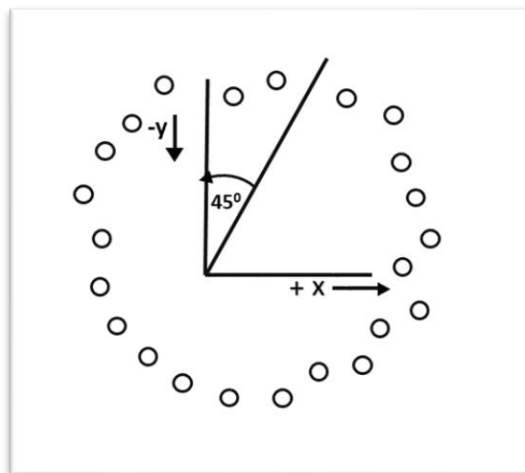
Implement Bresenham circle drawing algorithm to draw any object. The object should be displayed in all the quadrants with respect to center and radius

#### **Problem Statement:**

Implement Bresenham circle drawing algorithm to draw any object. The object should be displayed in all the quadrants with respect to center and radius

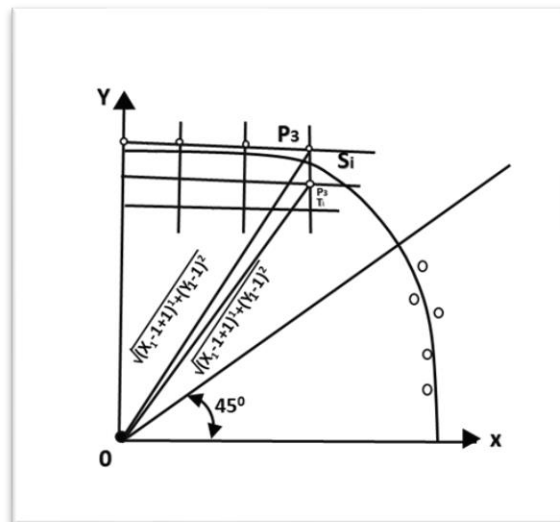
#### **Theory:**

Scan-Converting a circle using Bresenham's algorithm works as follows: Points are generated from  $90^\circ$  to  $45^\circ$ , moves will be made only in the  $+x$  &  $-y$  directions as shown in fig:



The best approximation of the true circle will be described by those pixels in the raster that falls the least distance from the true circle. We want to generate the points from  $90^\circ$  to  $45^\circ$ . Assume that the last scan-converted pixel is  $P_1$  as shown in fig.

Each new point closest to the true circle can be found by taking either of two actions.



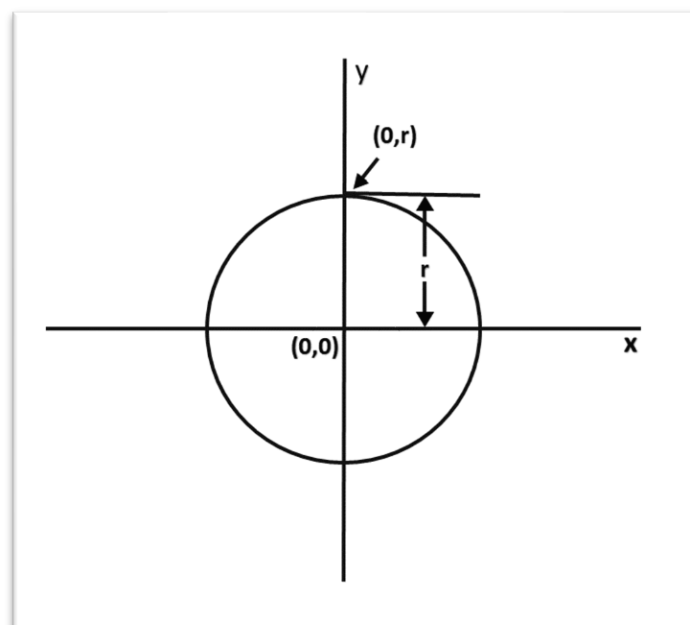
1. Move in the x-direction one unit or
2. Move in the x- direction one unit & move in the negative y-direction one unit.

Let  $D(S_i)$  is the distance from the origin to the true circle squared minus the distance to point  $P_3$  squared.  $D(T_i)$  is the distance from the origin to the true circle squared minus the distance to point  $P_2$  squared. Therefore, the following expressions arise.

$$D(S_i) = (x_{i-1} + 1)^2 + y_{i-1}^2 - r^2$$

$$D(T_i) = (x_{i-1} + 1)^2 + (y_{i-1} - 1)^2 - r^2$$

Since  $D(S_i)$  will always be +ve &  $D(T_i)$  will always be -ve, a decision variable  $d$  may be defined as follows:



$$d_i = D(S_i) + D(T_i)$$

Therefore,

$$d_i = (x_{i-1} + 1)^2 + y_{i-1}^2 - r^2 + (x_{i-1} + 1)^2 + (y_{i-1} - 1)^2 - r^2$$

From this equation, we can drive initial values of  $d_i$  as

If it is assumed that the circle is centered at the origin, then at the first step  $x = 0$  &  $y = r$ .

Therefore,

$$\begin{aligned} d_i &= (0+1)^2 + r^2 - r^2 + (0+1)^2 + (r-1)^2 - r^2 \\ &= 1+1+r^2-2r+1-r^2 \\ &= 3 - 2r \end{aligned}$$

Thereafter, if  $d_i < 0$ , then only  $x$  is incremented.

$$x_{i+1} = x_i + 1 \quad d_{i+1} = d_i + 4x_i + 6$$

& if  $d_i \geq 0$ , then  $x$  &  $y$  are incremented

$$\begin{aligned} x_{i+1} &= x_i + 1 & y_{i+1} &= y_i - 1 \\ d_{i+1} &= d_i + 4(x_i - y_i) + 10 \end{aligned}$$

### Algorithm:

**Step1:** Start Algorithm

**Step2:** Declare  $p, q, x, y, r, d$  variables

$p, q$  are coordinates of the center of the circle  
 $r$  is the radius of the circle

**Step3:** Enter the value of  $r$

**Step4:** Calculate  $d = 3 - 2r$

**Step5:** Initialize  $x=0$   
 $y=r$

**Step6:** Check if the whole circle is scan converted  
 If  $x \geq y$   
 Stop

**Step7:** Plot eight points by using concepts of eight-way symmetry.

The center is at  $(p, q)$ . Current active pixel is  $(x, y)$ .

putpixel  $(x+p, y+q)$   
 putpixel  $(y+p, x+q)$   
 putpixel  $(-y+p, x+q)$   
 putpixel  $(-x+p, y+q)$

```
putpixel (-x+p, -y+q)
putpixel (-y+p, -x+q)
putpixel (y+p, -x+q)
putpixel (x+p, -y-q)
```

**Step8:** Find location of next pixels to be scanned

If  $d < 0$

then  $d = d + 4x + 6$

increment  $x = x + 1$

If  $d \geq 0$

then  $d = d + 4(x - y) + 10$

increment  $x = x + 1$

decrement  $y = y - 1$

**Step9:** Go to step 6

**Step10:** Stop Algorithm

## **Conclusion:**

Learned to implement Bresenham's circle drawing algorithm

### **Advantages**

- It is a simple algorithm.
- It can be implemented easily
- It is totally based on the equation of circle i.e.  $x^2 + y^2 = r^2$

### **Disadvantages**

- There is a problem of accuracy while generating points.
- This algorithm is not suitable for complex and high graphic images.