

TEAM #1

ISEN 614:700

SPRING 2020

SEMESTER PROJECT

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BACKGROUND

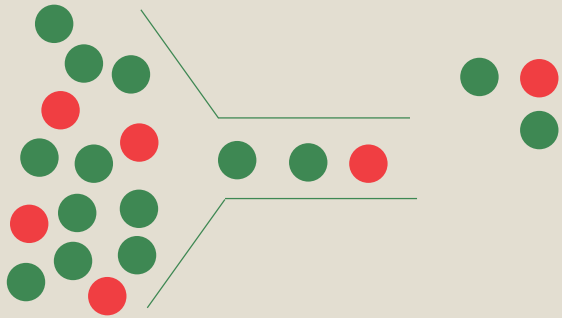
1

- Setting:
 - Manufacturing plant
 - 552 records
 - p 209
 - $n = 1$
 - Actual meaning of data points is omitted
- Audience
 - Manufacturing Manager
- Objective:
 - Classify data into two sets
 - In-control
 - Out-of-control
 - Determine in control population parameters

APPROACH

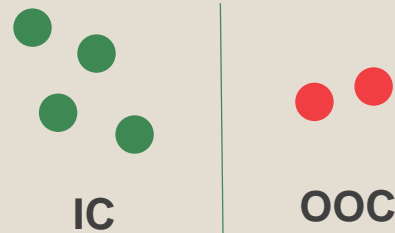
2

REFINE



- Refine the data to reduce the data set while retaining most of variation reflected in the original data set by using:
 - Principle component analysis

DISCOVER



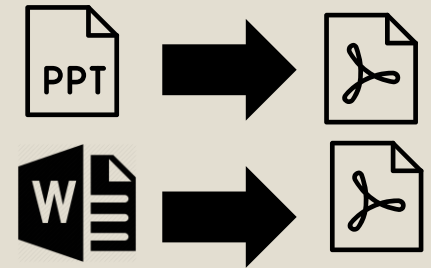
- Finding best method to determine the in-control and out-of-control subset by using and combining the following techniques:
 - Multivariate cumulative sum (m-CUSUM)
 - Multivariate exponentially weighted moving average (m-EWMA)
 - Hotelling T^2

DEFINE



- Determine the in-control dataset's parameters to describe the distribution by using:
 - Distribution tests

DESCRIBE



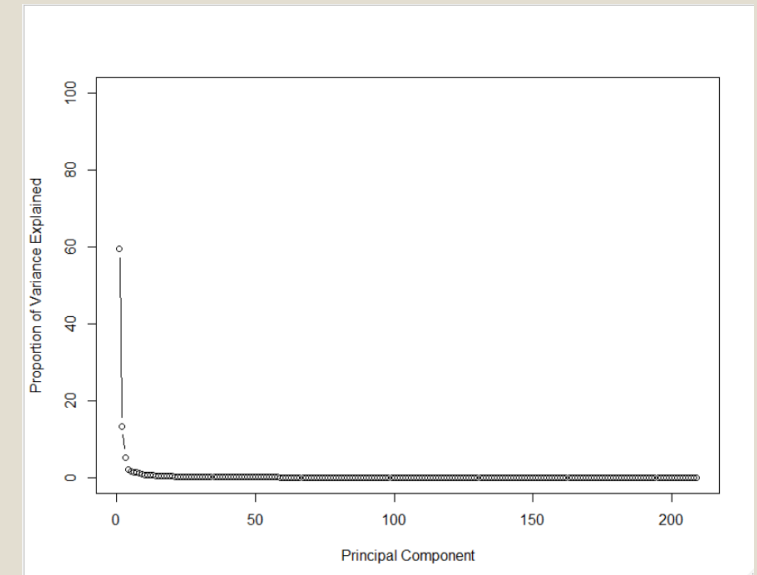
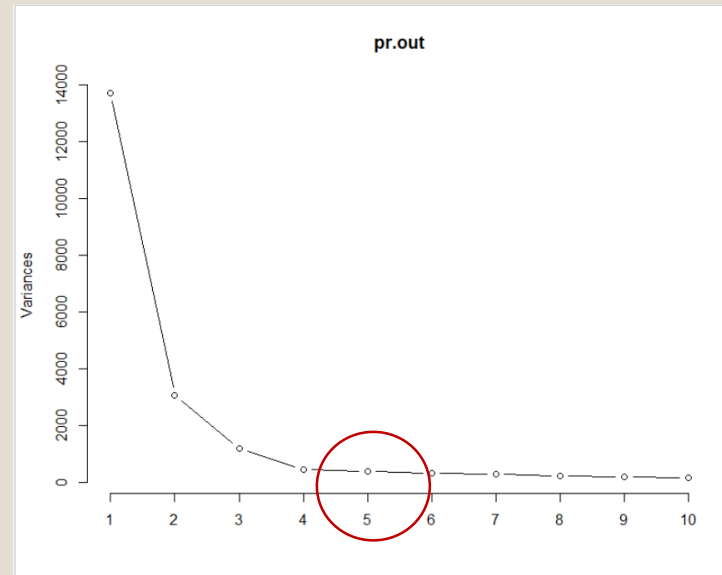
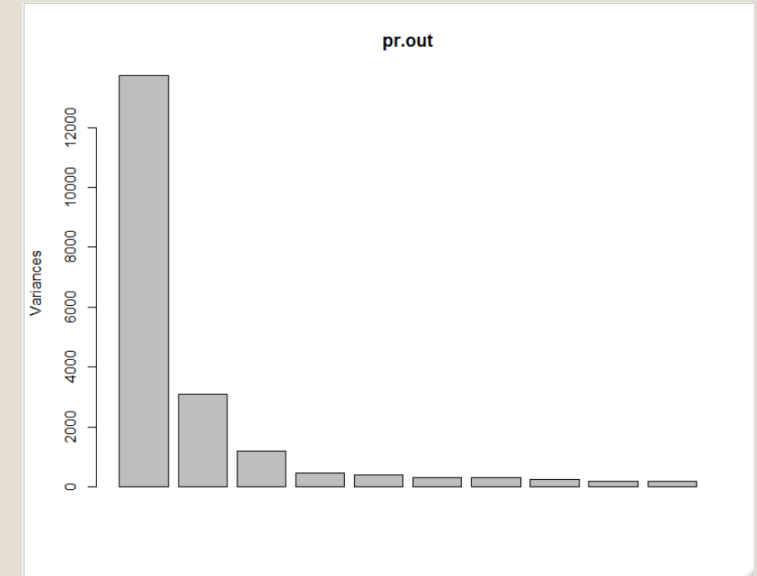
- Summarize approach and findings into deliverables
 - Microsoft Word report saved as a PDF
 - Microsoft PowerPoint presentation saved as a PDF

PRINCIPAL COMPONENT ANALYSIS (PCA) RESULTS

3

- Vital Few effects to be monitored
- Eigenvalues ordered from largest to smallest
 - PVE = Proportion of Variance Explained
 - CVE = Cumulative Variance Explained
- 5 Principal Components Selected because it explains 81.79% of the data's variance

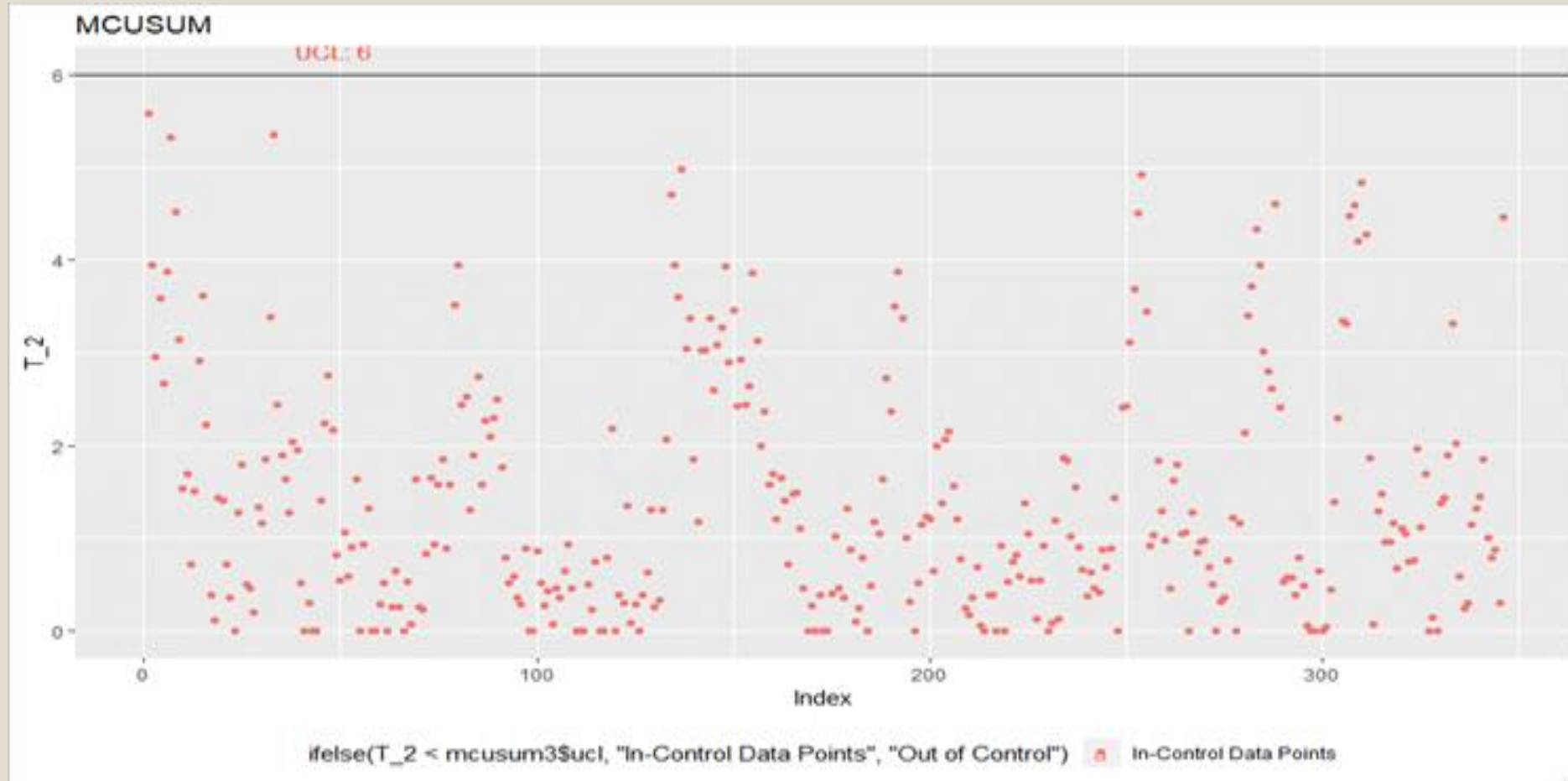
E.V.	PVE	CVE
1	59.52	59.52
2	13.35	72.87
3	5.23	78.1
4	2.00	80.1
5	1.69	81.79



MULTIVARIATE CUMULATIVE SUM (M-CUSUM) RESULTS

4

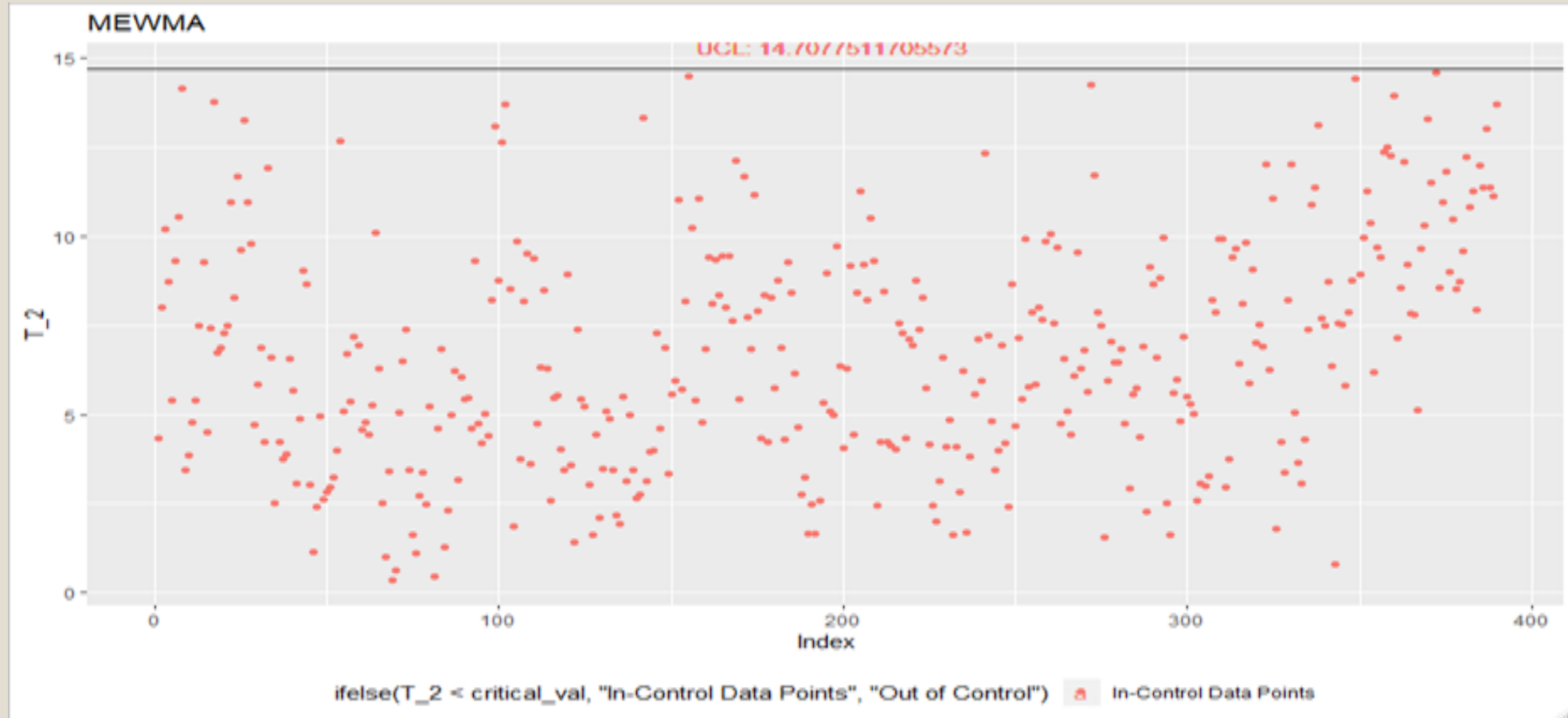
- Iterations: 6
- In-Control Points: 346



MULTIVARIATE EXPONENTIALLY WEIGHTED MOVING AVERAGE (M-EWMA) RESULTS

5

- Iterations: 11
- In-Control Points: 395

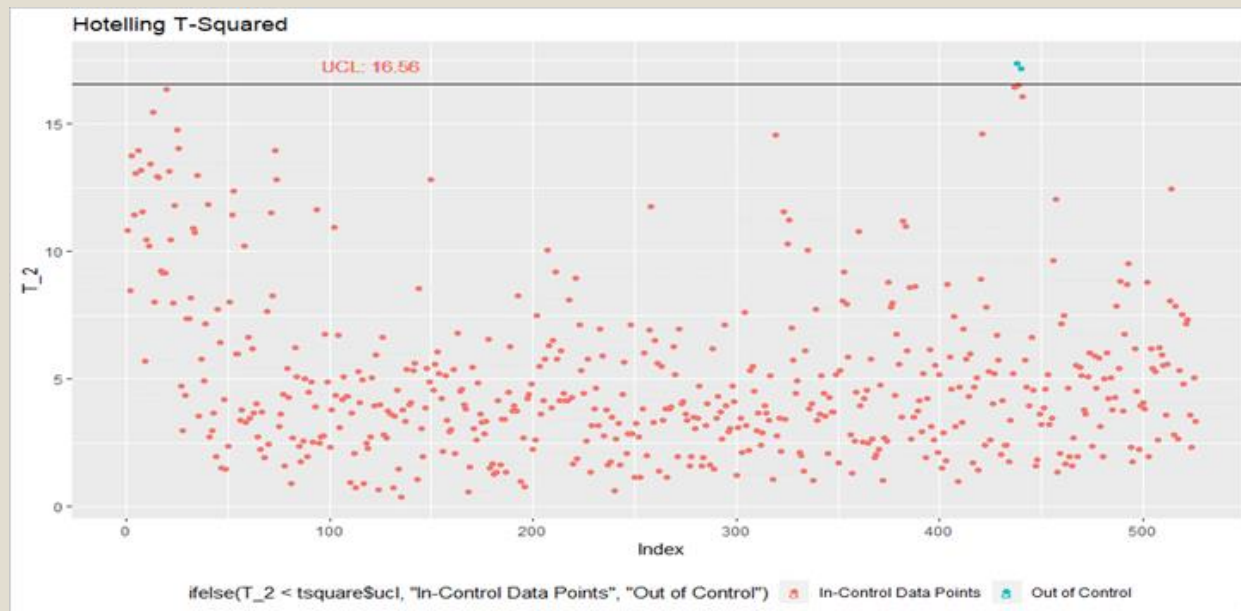


HOTELLING T^2 RESULTS (PART 1)

6

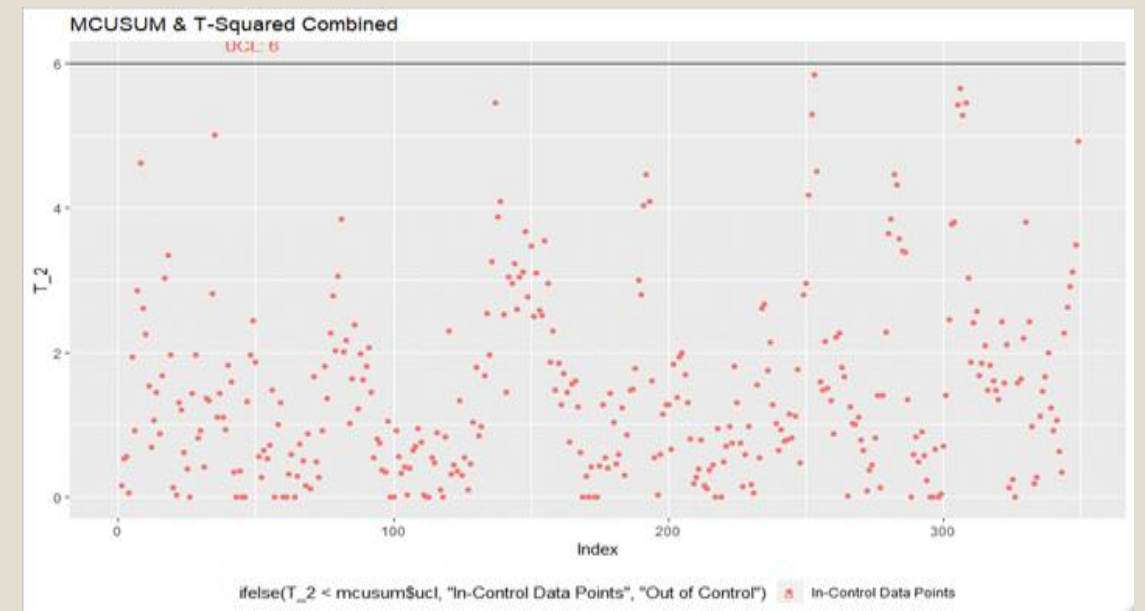
HOTELLING T^2 ONLY

- Iterations: 15
- In-Control Points: 482
- Out-of-Control Points: 2



HOTELLING T^2 + m-CUSUM

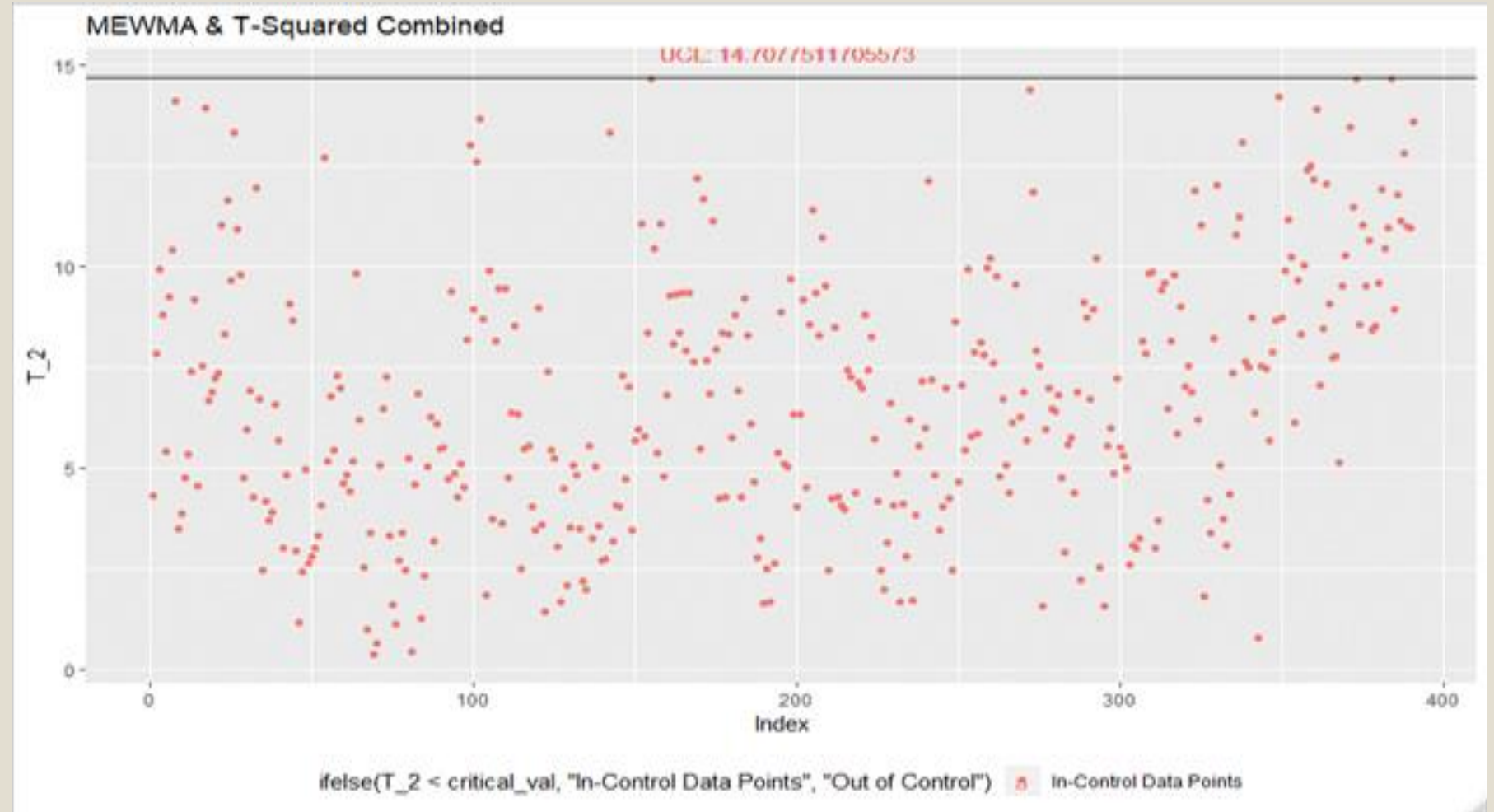
- Iterations: 5
- In-Control Points: 349



HOTELLING T^2 + m-EWMA RESULTS

7

- Iterations: 9
- In-Control Points: 491
- UCL = 14.71



DISTRIBUTION TESTS RESULTS

8

- Minitab Individual Distribution Identification indicated that a Johnson Transformation best fit the data
- Transformation
 - $x_{Transformed} = 1.11147 + 1.24842 * \ln\left(\frac{x+0.156411}{19.5056-x}\right)$
- Estimated Population Parameters on the Transformed Data $\sim N(\hat{\mu}, \hat{\sigma})$
 - $\hat{\mu} = -0.0058$
 - $\hat{\sigma} = 0.9975$
- Probability plot to the right confirms that a normal distribution on the transformed data fits the data with only a few outlying points

