

1.1)

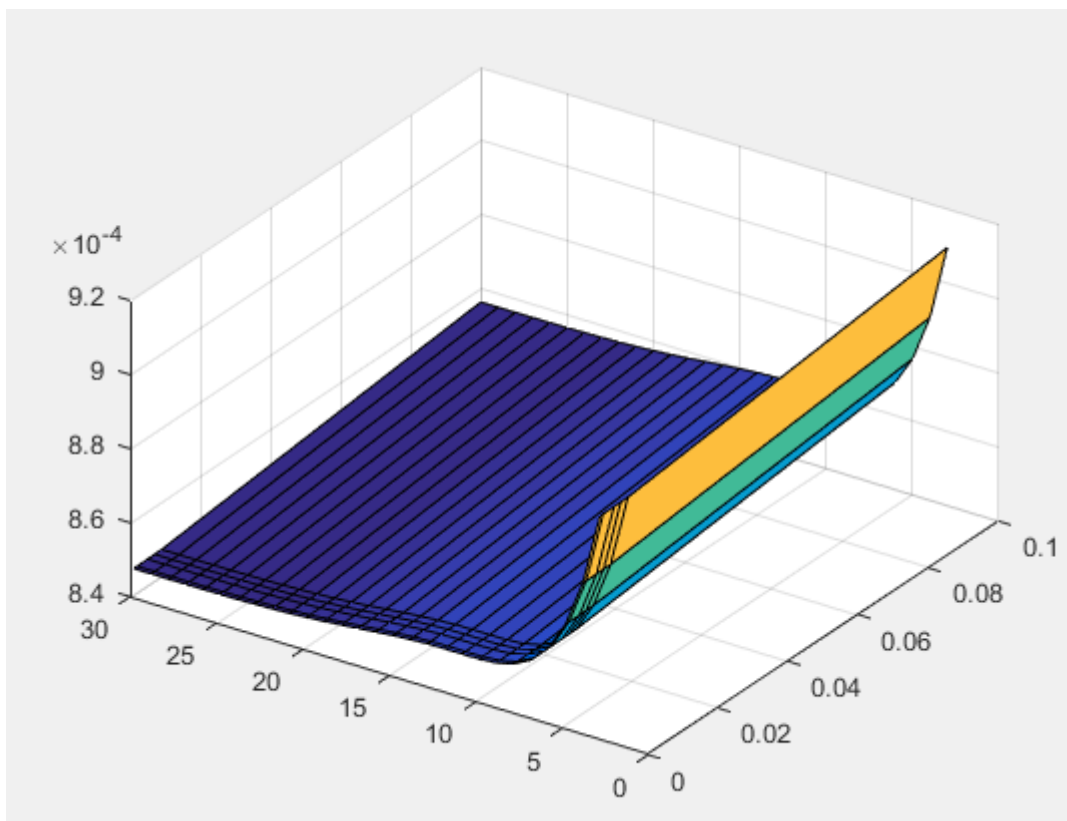
- For selecting the hyper parameters, we need to train data on training.mat. Also as per the hint given , I selected 5 values from the range 3 to 30 for filter order and took lambda as a set of following values:

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14 - lambda = [0.01,0.05,0.1,0.5,1];
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- Calculation of W^* for $m=3:30$ using training or validation data.
- W^* was calculated as product of autocorrelation matrix and correlation matrix.
- Desired signal is train/validate (Y).
- Calculation of \hat{Y} :

$$\hat{y}(n) = \sum_{k=0}^{M-1} w(k)x(n-k)$$

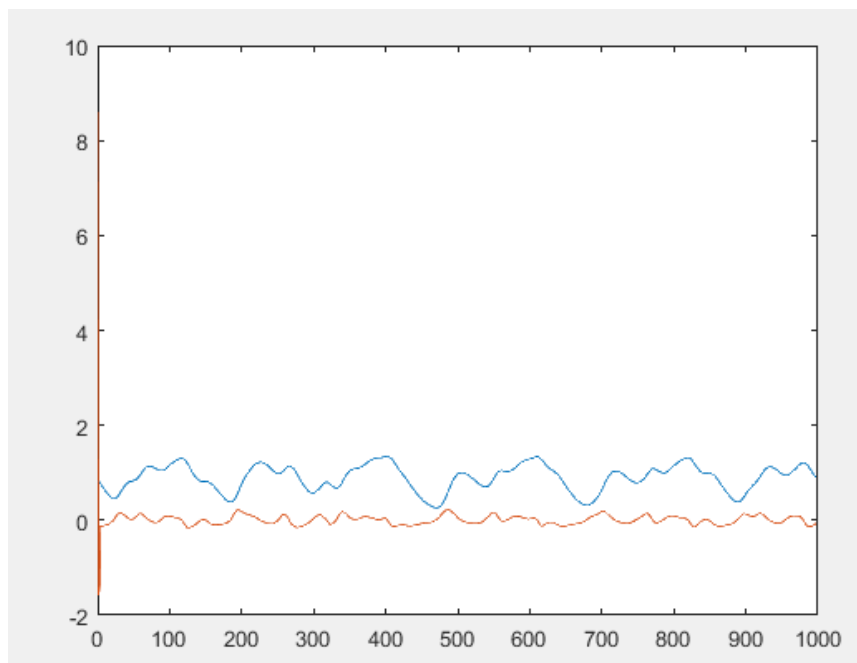
- Calculation of mean square error , using Y , \hat{Y} .
- With this idea , I approximately understood that value of m lies in range of 20:30 . Then plotting error (J) with respect to all values in range of 3:30 and all possible value of Lambda, we get following plot on validate set:



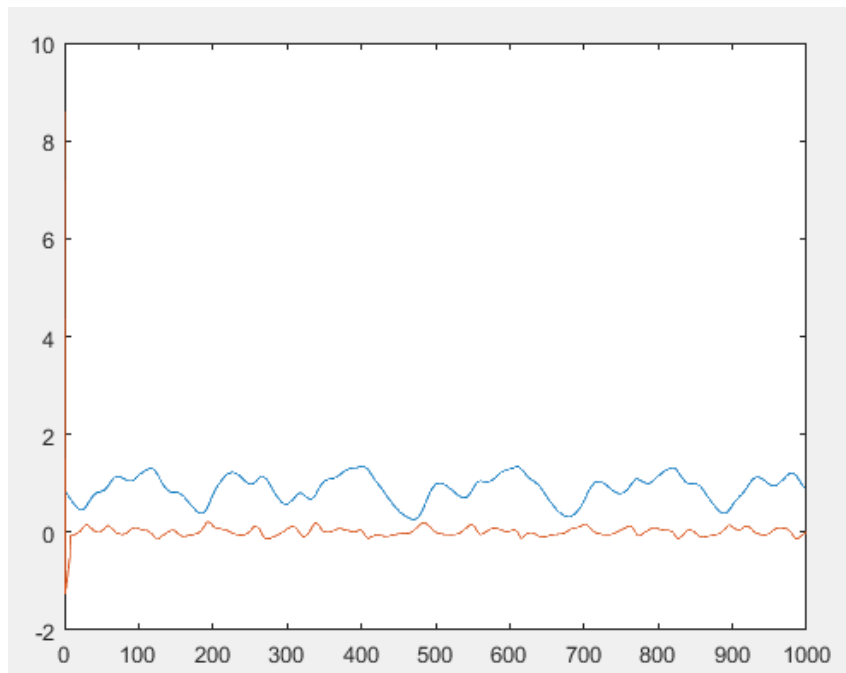
This shows that $m=30$ and $\lambda = 0.001$ gives us a best mean square error. Also the same, was confirmed with training data, which also gave minimum value for error for $m= 30$ and $\lambda= 0.001$

1.2) Plot of Test vs error over time.

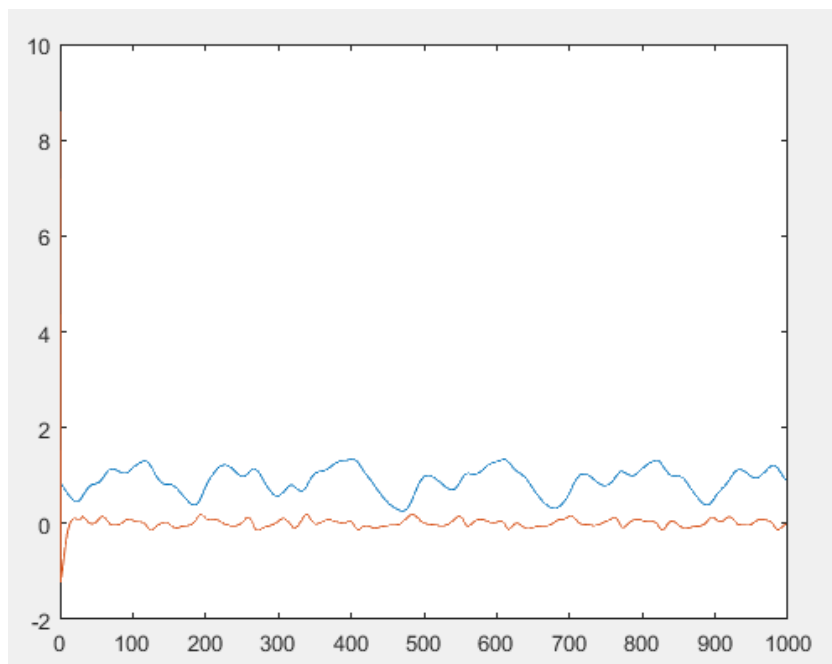
- Blue line is the signal and orange line is error (**error is scaled 10 times that means error for plotting is 10 times the original error**).
- Following steps were used to deduce this:
- Calculation of W^* for $m=4,8$ and 30 using training /validation data.
- Then respective X matrix's were calculated from test.mat
- Desired signal is test (Y).
- Calculation of \hat{Y} = which is $X * W$ obtained from 1 and 2 respectively for filter order 4,8 and 30.
- Calculation of mean square error, using Y , \hat{Y} .
- For $m=4$, and $\lambda = 0.001$



For $m=8$, and $\lambda = 0.001$



For $m= 30$ and $\lambda = 0.001$



This plots approximately looks the same, as the value of error is extremely small . Difference between error at $m=4, 8$ and $m= 30$ is very small. We are trying to fit a sinusoidal type wave, in an linear regression, that is the reason I think error is not constant across time. Though regular sinusoidal wave can be well approximated by linear regression, the test signal is not regular.

1.3) Quantifying results on testnoisy.mat:

- Following were the steps followed :
 - 1) Calculation of W^* for $m=4,8$ and 30 using training or validation data. We will use the values of W obtained from them for prediction.
 - 2) Then respective X matrix's were calculated from testnoisy.mat
 - 3) Desired signal is test (Y).
 - 4) Calculation of $Y(\text{hat}) =$ which is $X * W$ obtained from 1 and 2 respectively for filter order $4,8$ and 30 .
 - 5) Calculation of mean square error , using Y , $Y(\text{hat})$.
- After following the above procedure we get following values, min square error values for error for $m= 4, 8$ and 30 and $\lambda = 0.001$,

 Err1	1.5881
 Err2	1.4308
 Err3	1.4157

As we see, value for Err3 or when $m= 30$ and $\lambda = 0.001$ is minimum, we can say that filter order 30 works better for noisy data.

References :

- 1) Discussion with friends – Kunal Bajaj, Ruturaj Zadbukey, Devyash Sanghai ,Ning Wei, Mayank Kulkarni, Atharva.
- 2) Hw2 help documents.

Note :

- 1) No code file has been attached as per request. Code for the questions have been programmed by myself completely.