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Assignment-04

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Download all python codes from

https://github.com/suyogtangade/Assignment4.git

and latex-tikz codes from

https://github.com/suyogtangade/Assignment4.git

Question taken from

https://github.com/gadepall/ncert/blob/main/linalg/ linear_forms/gvv_ncert_linear_forms.pdf

1 Linear Forms Exercise 2.5(c)

Find out whether the following pair of linear equations are consistent, or inconsistent.

$$\left(\frac{3}{2} \quad \frac{5}{3}\right)\mathbf{x} = 7 \tag{1.0.1}$$

$$(9 -10) \mathbf{x} = 14 \tag{1.0.2}$$

2 Solution

$$\left(\frac{3}{2} \quad \frac{5}{3}\right)\mathbf{x} = 7 \tag{2.0.1}$$

$$(9 -10)$$
x = 14 (2.0.2)

The above equations can be expressed as the matrix equation

$$\begin{pmatrix} \frac{3}{2} & \frac{5}{3} \\ 9 & -10 \end{pmatrix} \mathbf{x} = \begin{pmatrix} 7 \\ 14 \end{pmatrix} \tag{2.0.3}$$

The augmented matrix for the above equation is row reduced as follows:

$$\begin{pmatrix} \frac{3}{2} & \frac{5}{3} & 7\\ 9 & -10 & 14 \end{pmatrix} \xrightarrow{R_1 \leftarrow \frac{2}{3}R_1} \begin{pmatrix} 1 & \frac{10}{9} & \frac{14}{3}\\ 9 & -10 & 14 \end{pmatrix} \tag{2.0.4}$$

$$\stackrel{R_2 \leftarrow R_2 - 9R_1}{\longleftrightarrow} \begin{pmatrix} 1 & \frac{10}{9} & \frac{14}{3} \\ 0 & -20 & -28 \end{pmatrix} \qquad (2.0.5)$$

$$\stackrel{R_2 \leftarrow \frac{-1}{20}R_2}{\longleftrightarrow} \begin{pmatrix} 1 & \frac{10}{9} & \frac{14}{3} \\ 0 & 1 & \frac{7}{5} \end{pmatrix} \qquad (2.0.6)$$

$$\stackrel{R_1 \leftarrow \frac{-10}{9}R_2 + R_1}{\longleftrightarrow} \begin{pmatrix} 1 & 0 & \frac{28}{9} \\ 0 & 1 & \frac{7}{5} \end{pmatrix} \qquad (2.0.7)$$

So by reduction of the (2×3) matrix

$$\begin{pmatrix} \frac{3}{2} & \frac{5}{3} & 7\\ 9 & -10 & 14 \end{pmatrix} \tag{2.0.8}$$

gives matrix with 2 non zero row, so i'ts rank is 2.

$$\begin{pmatrix} \frac{3}{2} & \frac{5}{3} \\ 9 & -10 \end{pmatrix} \tag{2.0.9}$$

The rank of the above matrix is also 2.

: lines are Consistent and gives unique solution.

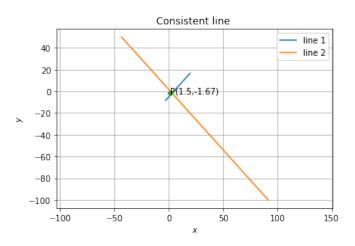


Fig. 2.1: Graphical solution

... This figure verifies that two lines are intersecting at point $P = \begin{pmatrix} 1.5 \\ -1.67 \end{pmatrix}$.