

Resampling in Sequential Monte Carlo

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Residual Resampling^{1,2}

Definition

1. Deterministically assign $\lfloor Nw_i \rfloor$ offspring to particle i
2. There are $R := N - \sum_{i=1}^N \lfloor Nw_i \rfloor$ offspring still to be assigned
3. Assign these randomly according to the residual weights $r_i := w_i - \lfloor Nw_i \rfloor$


¹Liu & Chen (1998) 'Sequential Monte Carlo Methods for Dynamic Systems'

²Whitley (1994) 'A Genetic Algorithm Tutorial'


Residual Resampling

Illustration

$w_1 = 0.28$ 

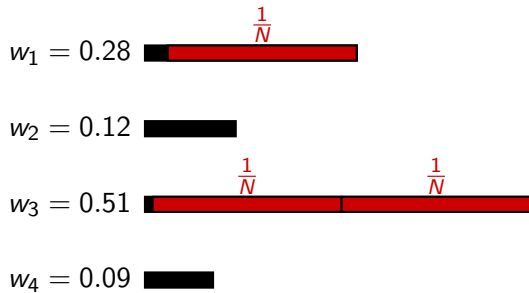
$w_2 = 0.12$ 

$w_3 = 0.51$ 

$w_4 = 0.09$ 

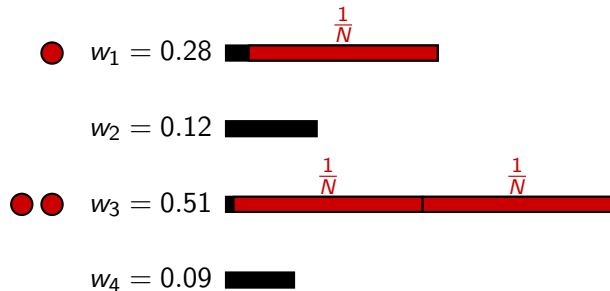
Residual Resampling

Illustration



Residual Resampling

Illustration



Residual Resampling

Illustration

● $r_1 \propto 0.03$ ■


$r_2 \propto 0.12$ ■■■■

●● $r_3 \propto 0.01$ ■


$r_4 \propto 0.09$ ■■■■

Residual Resampling

Illustration

● $r_1 = 0.12$ 

$r_2 = 0.48$ 

● ● $r_3 = 0.04$ 

$r_4 = 0.36$ 

References I

- [1] Jun S Liu and Rong Chen. Sequential Monte Carlo methods for dynamic systems. *Journal of the American Statistical Association*, 93(443):1032–1044, 1998.
- [2] Darrell Whitley. A genetic algorithm tutorial. *Statistics and Computing*, 4(2):65–85, 1994.