

Phase 1

1. System Response of I & II order systems

Find time domain specifications of first order and second order system response to step, ramp and sinusoidal inputs, manual calculation, and plotting system response using Matlab program.

PROBLEM: A system has a transfer function, $G(s) = \frac{50}{s + 50}$. Find the time constant, T_c , settling time, T_s , and rise time, T_r .

ANSWER: $T_c = 0.02$ s, $T_s = 0.08$ s, and $T_r = 0.044$ s.

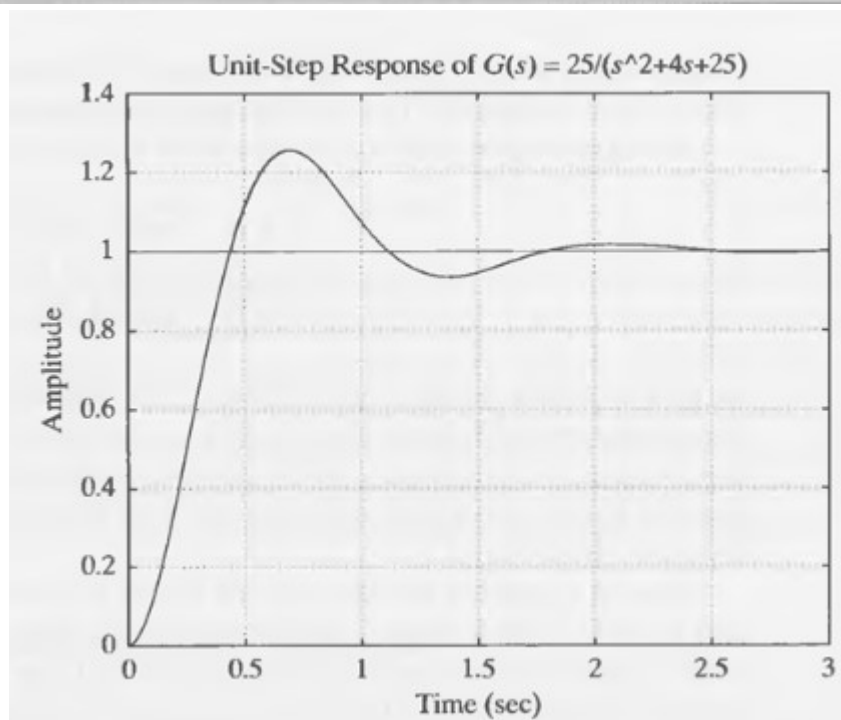
System	Pole-zero plot	Response
<p>(a) $R(s) = \frac{1}{s}$ $\xrightarrow{G(s)}$ $C(s)$</p> <p style="text-align: center;"> $G(s) = \frac{b}{s^2 + as + b}$ General </p>		
<p>(b) $R(s) = \frac{1}{s}$ $\xrightarrow{G(s)}$ $C(s)$</p> <p style="text-align: center;"> $G(s) = \frac{9}{s^2 + 9s + 9}$ Overdamped </p>	<p>s-plane</p>	<p>c(t) $c(t) = 1 + 0.171e^{-7.854t} - 1.171e^{-1.146t}$</p>
<p>(c) $R(s) = \frac{1}{s}$ $\xrightarrow{G(s)}$ $C(s)$</p> <p style="text-align: center;"> $G(s) = \frac{9}{s^2 + 2s + 9}$ Underdamped </p>	<p>s-plane</p>	<p>c(t) $c(t) = 1 - e^{-t}(\cos\sqrt{8}t + \frac{\sqrt{8}}{8}\sin\sqrt{8}t)$ $= 1 - 1.06e^{-t}\cos(\sqrt{8}t - 19.47^\circ)$</p>
<p>(d) $R(s) = \frac{1}{s}$ $\xrightarrow{G(s)}$ $C(s)$</p> <p style="text-align: center;"> $G(s) = \frac{9}{s^2 + 9}$ Undamped </p>	<p>s-plane</p>	<p>c(t) $c(t) = 1 - \cos 3t$</p>
<p>(e) $R(s) = \frac{1}{s}$ $\xrightarrow{G(s)}$ $C(s)$</p> <p style="text-align: center;"> $G(s) = \frac{9}{s^2 + 6s + 9}$ Critically damped </p>	<p>s-plane</p>	<p>c(t) $c(t) = 1 - 3te^{-3t} - e^{-3t}$</p>

MATLAB representation of linear systems. The transfer function of a system is represented by two arrays of numbers. Consider the system

$$\frac{C(s)}{R(s)} = \frac{25}{s^2 + 4s + 25} \quad (4-38)$$

MATLAB Program 4-1

```
% -----Unit-step response-----  
  
% ***** Enter the numerator and denominator of the transfer  
% function *****  
  
num = [0 0 25];  
den = [1 4 25];  
  
% ***** Enter the following step-response command *****  
  
step(num,den)  
  
% ***** Enter grid and title of the plot *****  
  
grid  
title ('Unit-Step Response of  $G(s) = 25/(s^2 + 4s + 25)$ ')
```



Obtain the unit-impulse response of the following system:

$$\frac{C(s)}{R(s)} = G(s) = \frac{1}{s^2 + 0.2s + 1}$$

MATLAB Program 4-5

```
num = [0 0 1];  
den = [1 0.2 1];  
impz(num,den);  
grid  
title('Unit-Impulse Response of  $G(s) = 1/(s^2 + 0.2s + 1)$ ')
```

