

Lecture 02

Digital Image Basics

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MÉXICO

1. Motivation

1. Why Computer Vision for Geosciences?
2. Computer Vision processing levels
2. What is a digital image?
3. Point operations
4. Image manipulation with Python

Computer Vision for Geosciences (CV4GS)

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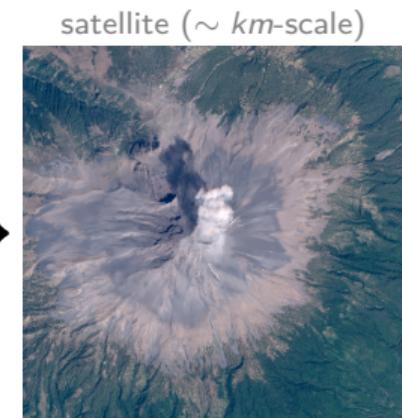
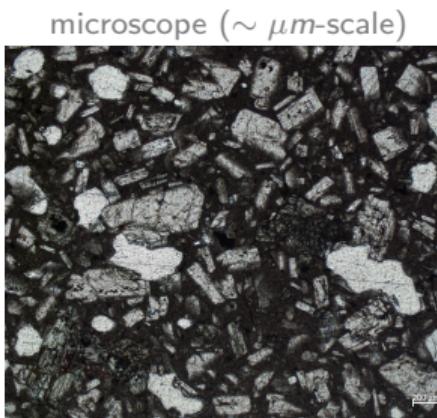
- **What is Computer Vision?**

⇒ discipline focused on enabling computers to acquire, process, and interpret visual data, primarily from digital images or video

Computer Vision for Geosciences (CV4GS)

- Sources of images for **geosciences** applications?

⇒ images can be derived from different imaging techniques at different scales

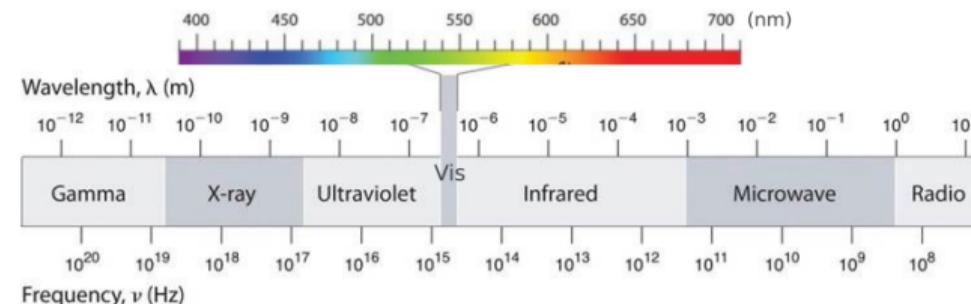


1.1. Why Computer Vision for Geosciences?

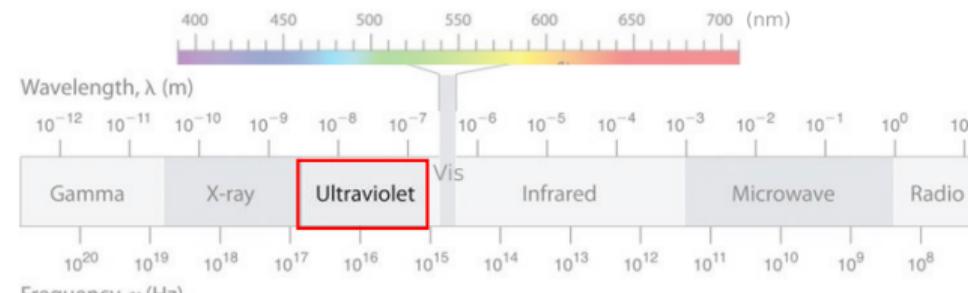
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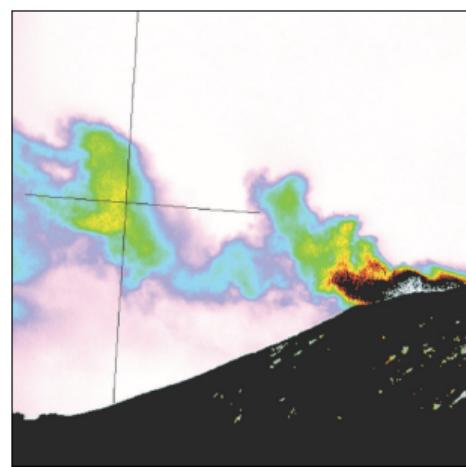
⇒ images can be constructed using different wavelengths spanning the entire electromagnetic spectra



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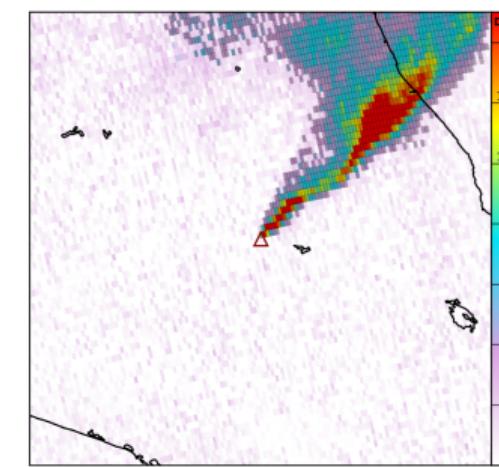


UV camera



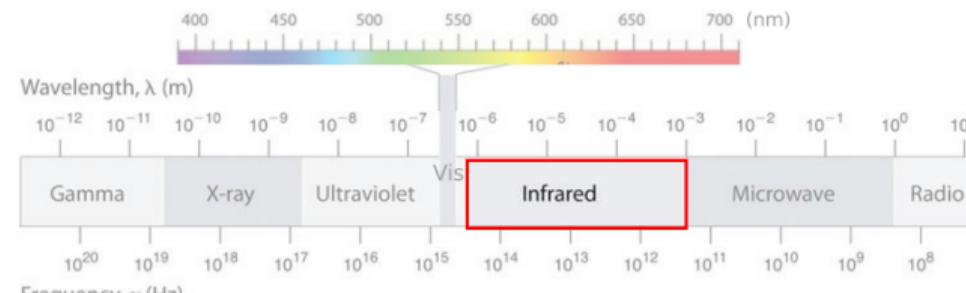
Popocatépetl 2013-01-29 (UV camera, [Campion et al. 2018](#))

UV satellite

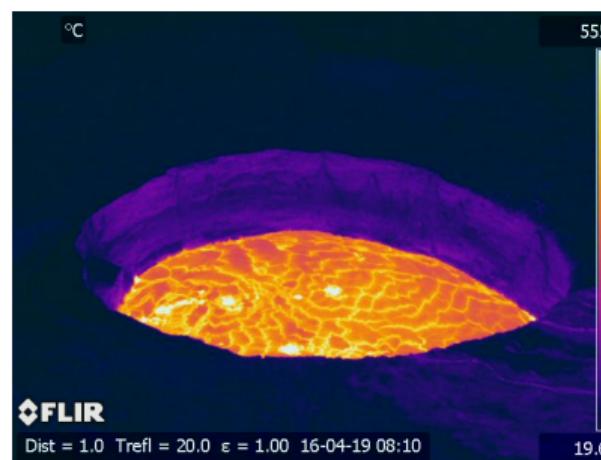


Popocatépetl 2019-02-17 (Sentinel-5P, [MOUNTS](#))

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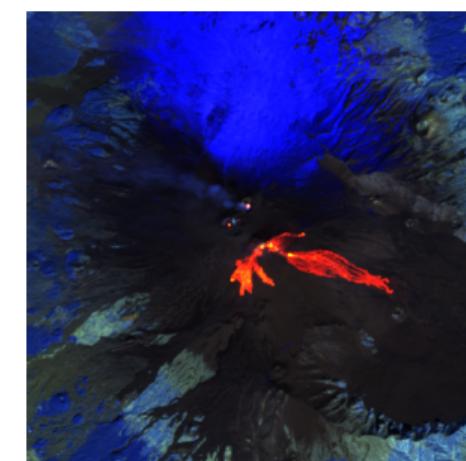


IR camera



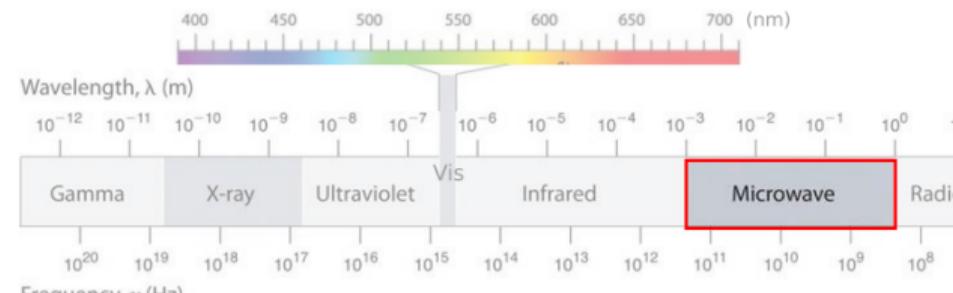
Nyiragongo 2016-04-16 (FLIR image, [Valade et al. 2018](#))

IR satellite

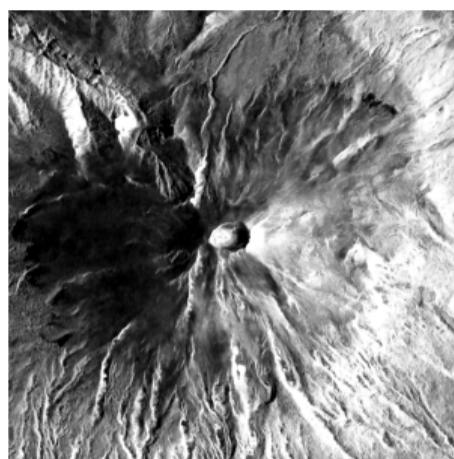


Etna 2021-02-23 (Sentinel-2 image, [MOUNTS](#))

1.1. Why Computer Vision for Geosciences?

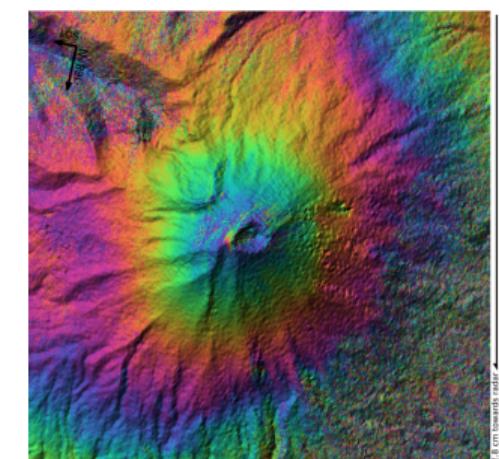


SAR satellite



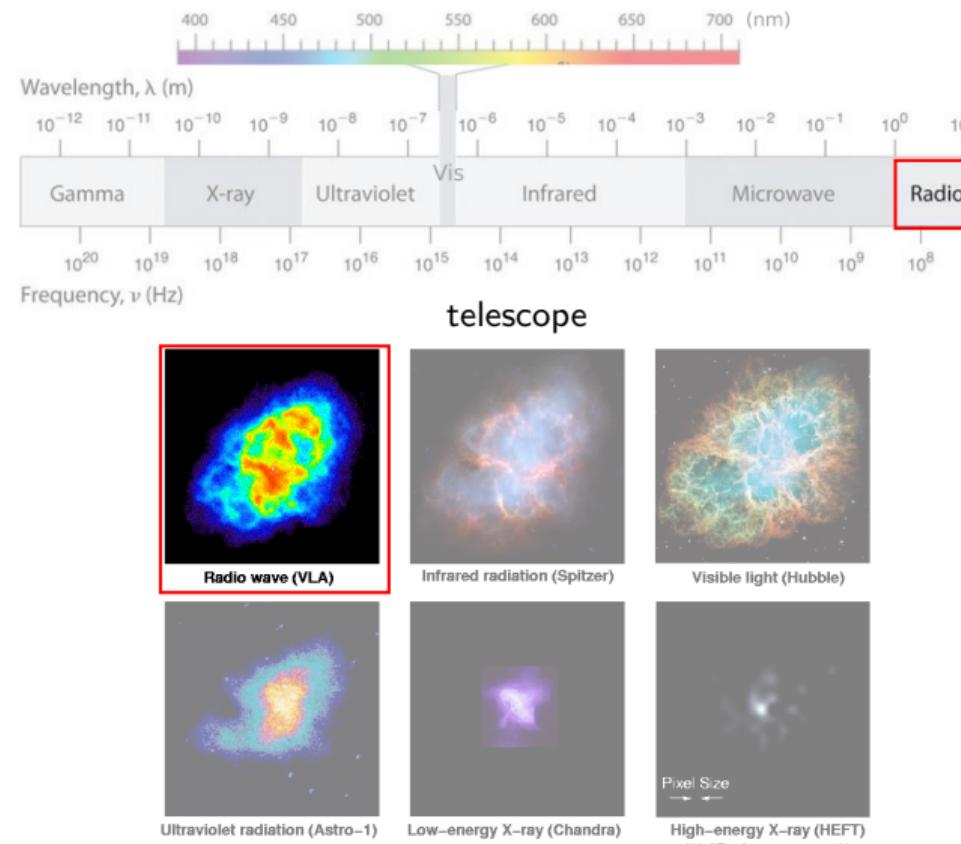
Popocatépetl SAR 2021-12-25 (Sentinel-1, [MOUNTS](#))

InSAR satellite

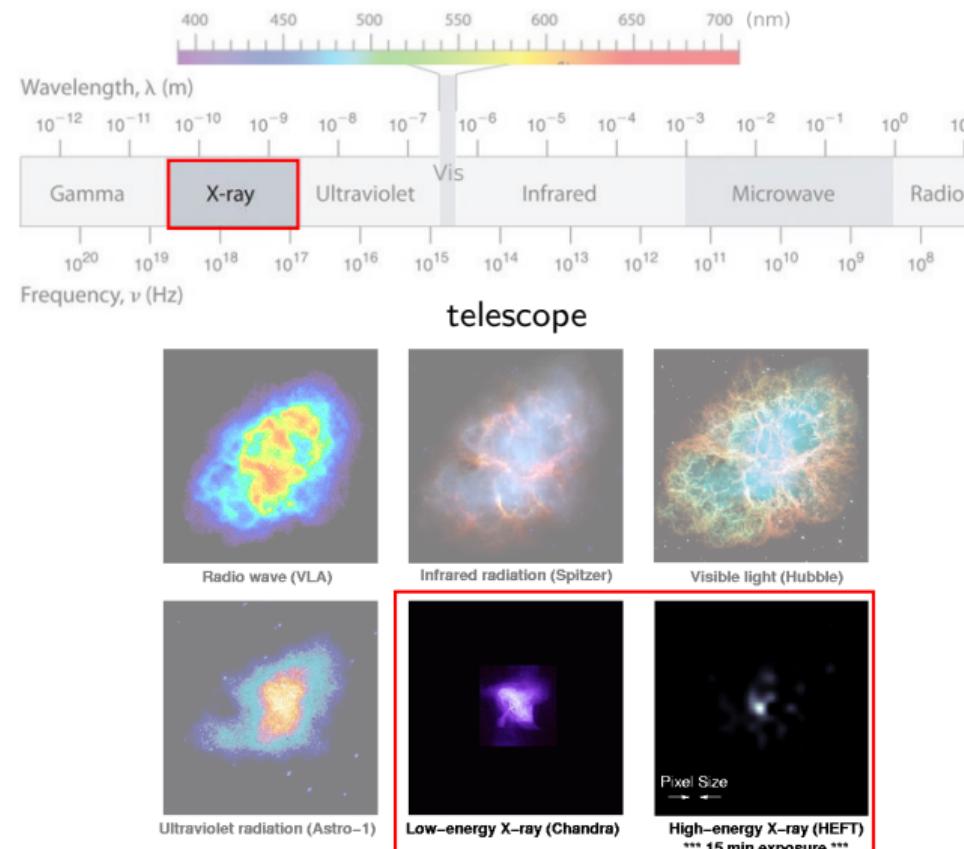


Popocatépetl InSAR interferogram 2021-12-25 dt=6 days ([MOUNTS](#))

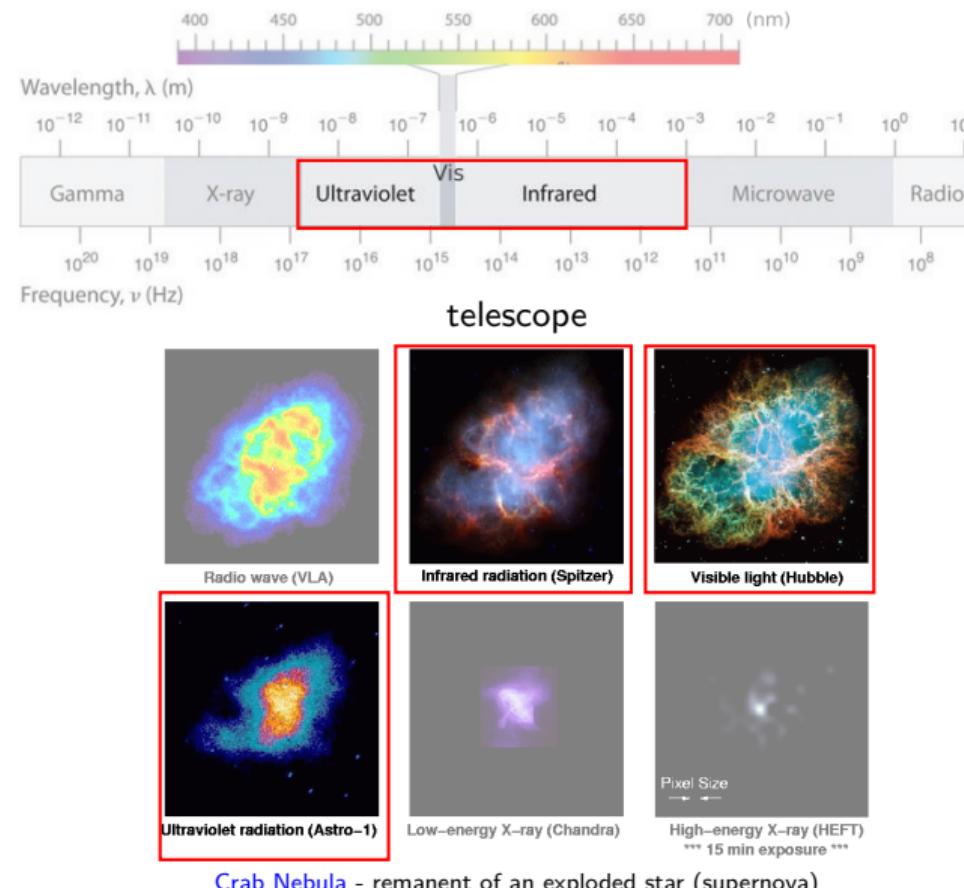
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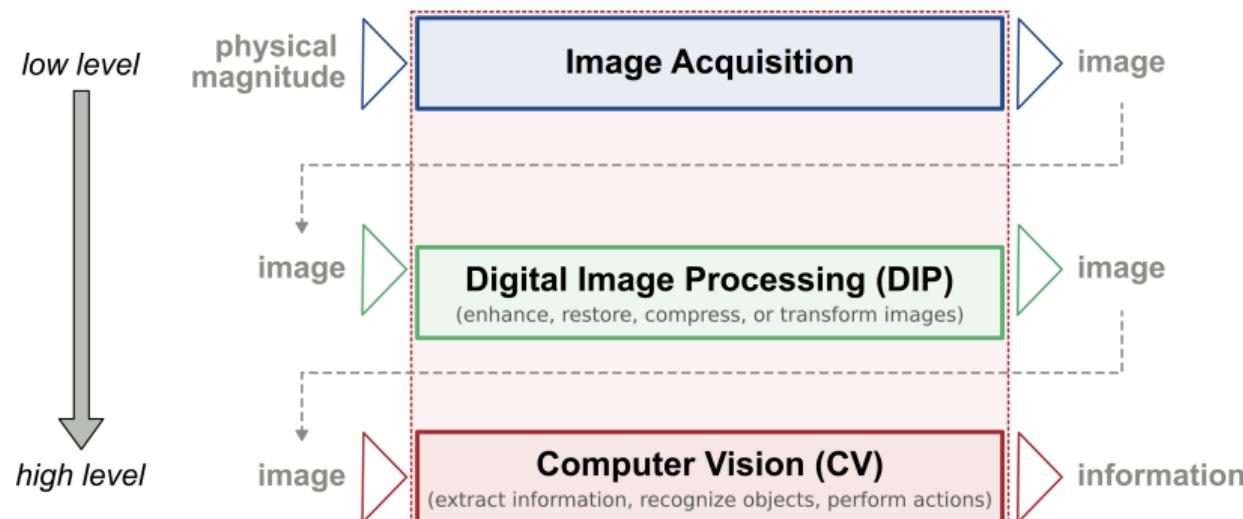
1.1. Why Computer Vision for Geosciences?



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From image acquisition to image processing:



“Computer Vision tasks include methods for **acquiring, processing, analyzing** and **understanding digital images**, and extraction of high-dimensional data from the real world in order to produce numerical or symbolic information, e.g., in the forms of decisions”.

Examples of processing levels:

- Low-level processing
 - image manipulation ⇒ *resizing, color adjustments, filtering, etc.*
 - feature extraction ⇒ *edges, gradients, etc.*
- Mid-level processing
 - panorama stitching
 - Structure from Motion (SfM) ⇒ 2D to 3D
 - Optical Flow ⇒ velocities
- High-level processing
 - classification ⇒ *what is in the image?*
 - detection ⇒ *where are they?*
 - segmentation (semantic or instance) ⇒ *segment image and give names*

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hue x5



filter (high pass)



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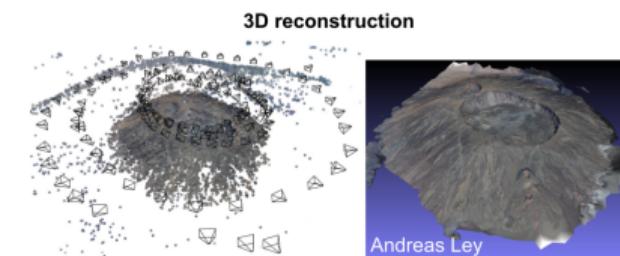
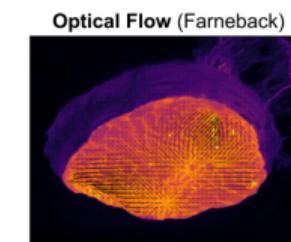
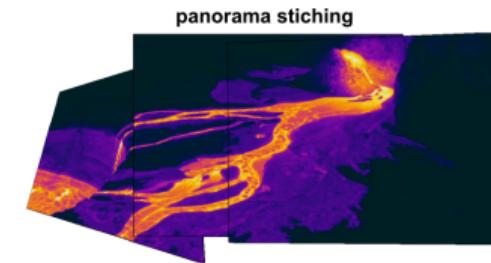
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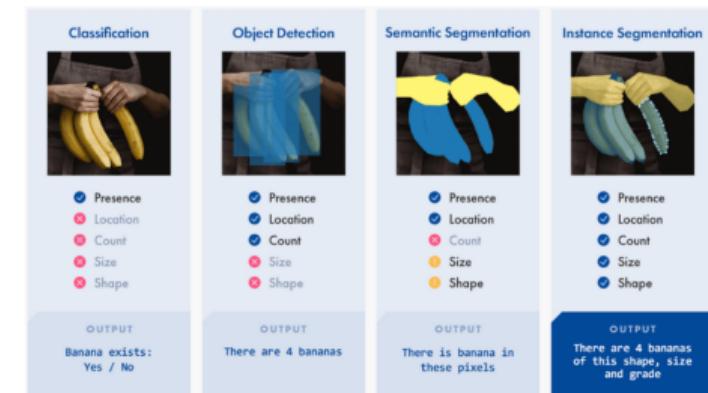
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Credit: cloudfactory

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1. Motivation

2. What is a digital image?

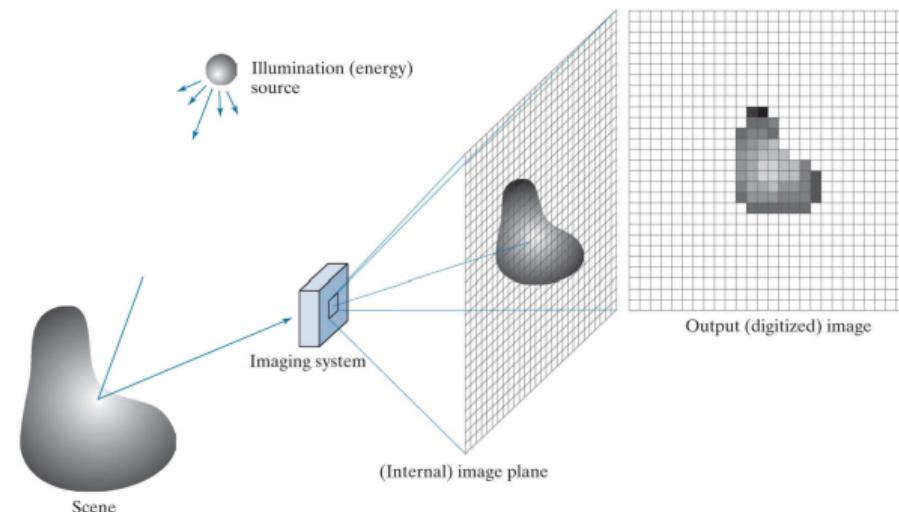
1. image acquisition
2. sampling and quantization
3. 3D projection on 2D plane
4. color image
5. color spaces
6. image histogram

3. Point operations

4. Image manipulation with Python

2.1. image acquisition

1. energy from an **illumination source** is reflected from a **scene**
2. the **imaging system** collects the incoming energy and focuses it onto an **image plane**
NB: light-sensing instruments typically use 2-D arrays of photosensors to record incoming light intensity
I(x): the CCD (Charge-Coupled Device)
3. the image plane is sampled and quantized to produce a **digital image**



Credit: Gonzalez & Woods 2018

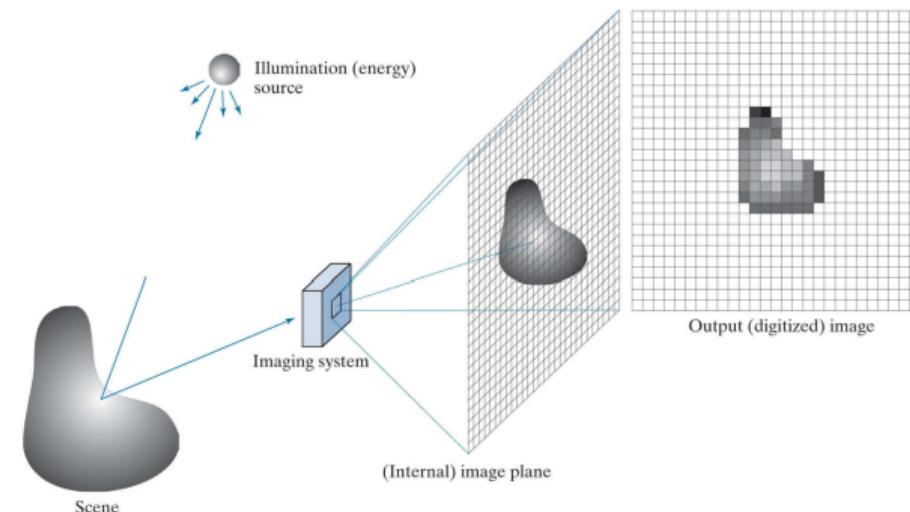
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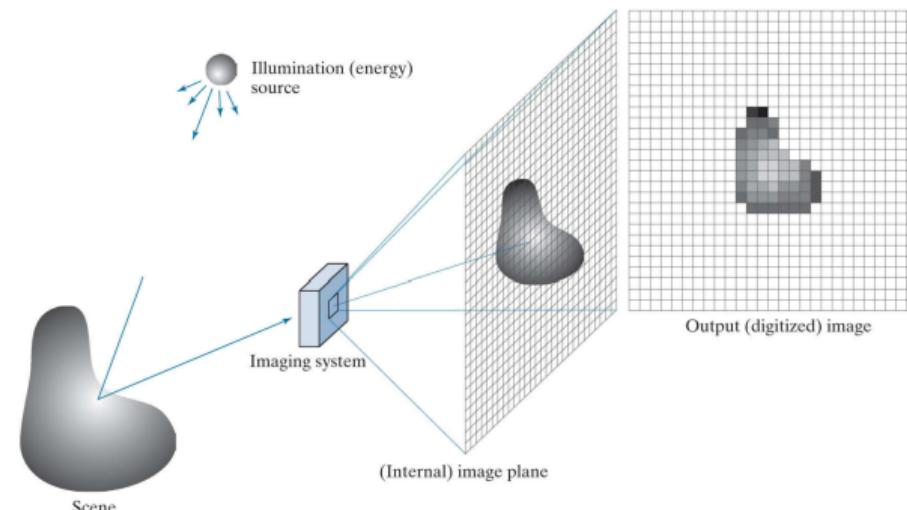
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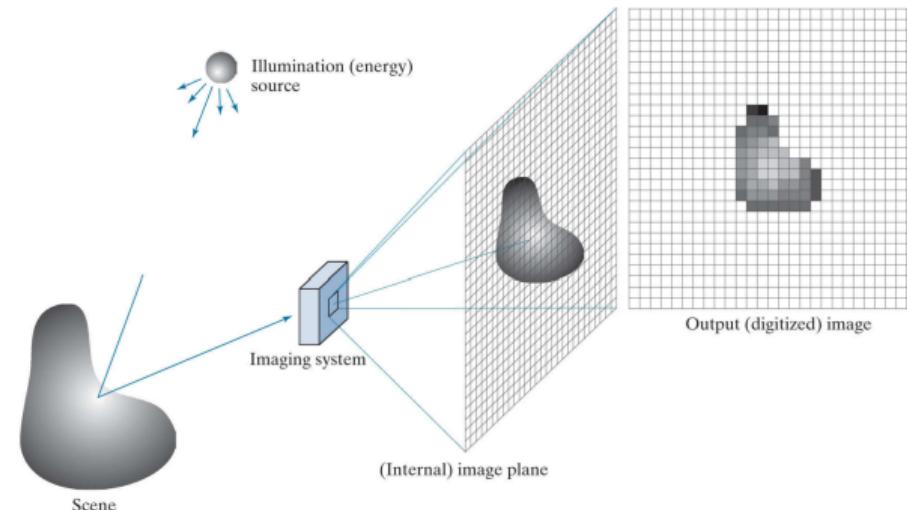
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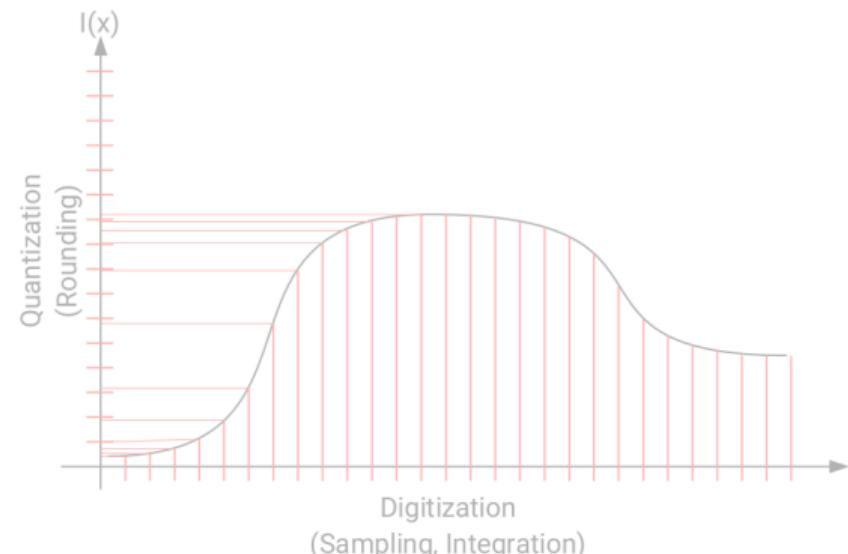
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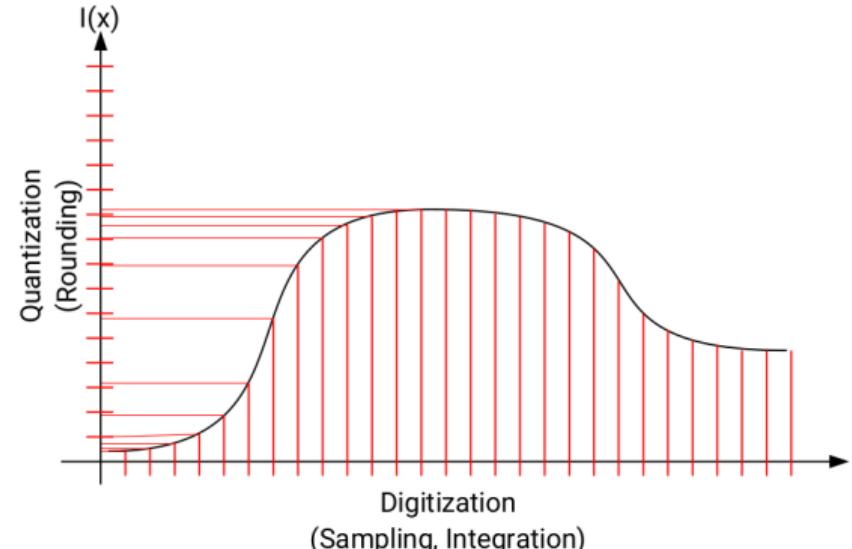
2.2. sampling and quantization

- each photosensor records incident light
- digitalization of an analog signal involves two operations
 - spatial sampling (= discretization of space domain)
 - intensity quantization (= discretization of incoming light signal)



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2.2. sampling and quantization

spatial sampling (= discretization of space domain)

⇒ smallest element resulting from the discretization of the space is called a pixel (=picture element)

(512, 512)

(128, 128)

(64, 64)

(32, 32)

**intensity quantization** (= discretization of light intensity signal)

⇒ typically, 256 levels (8 bits/pixel = 2^8 values) suffices to represent the intensity

8-bit resolution
 $2^8 = 256$ gray levels3-bit resolution
 $2^3 = 8$ gray levels2-bit resolution
 $2^2 = 4$ gray levels1-bit resolution
 $2^1 = 2$ gray levels

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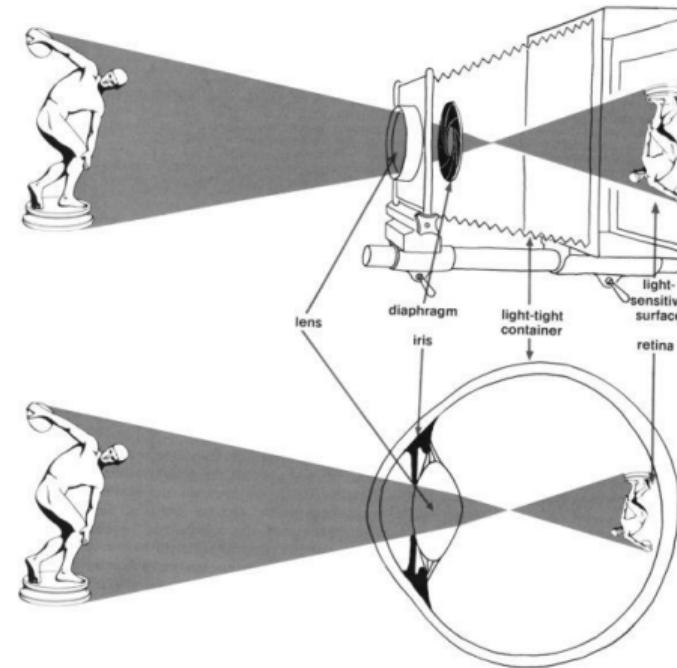
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2.3. 3D projection on 2D plane

But how is the 3D world projected on a 2D plane?

⇒ comparison between human eye and pinhole camera:

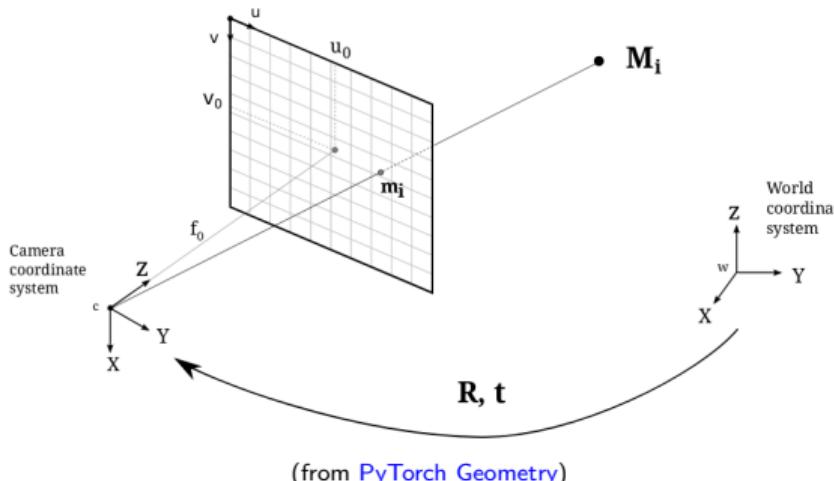


In 1514, Leonardo da Vinci explained: "By letting the images of illuminated objects penetrate through a small hole into a very dark room, you will then intercept these images on a white sheet of paper placed in this room. [...] but they will be smaller and reversed".

2.3. 3D projection on 2D plane

Image = 3D world projection on 2D

⇒ projection using the **pinhole camera** model:



Perspective transformation:

$$s m' = K[R|t]M' \quad (1)$$

$$s \begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = \begin{bmatrix} f_x & 0 & u_0 \\ 0 & f_y & v_0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} r_{11} & r_{12} & r_{13} & t_1 \\ r_{21} & r_{22} & r_{23} & t_2 \\ r_{31} & r_{32} & r_{33} & t_3 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix} \quad (2)$$

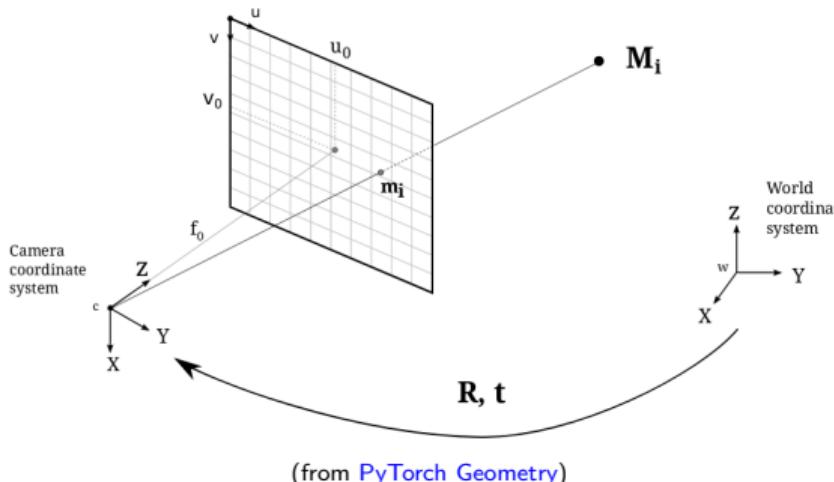
where:

- M' = 3D point in space with coordinates $[X, Y, Z]^T$ expressed in Euclidean coordinates
- m' = projection of the 3D point M' onto the image plane with coordinates $[u, v]^T$ expressed in pixel units
- K = camera calibration matrix (a.k.a. intrinsics parameters matrix)
 - f_x, f_y = focal lengths expressed in pixel units
 - u_0, v_0 = coordinates of the optical center (aka principal point), origin in the image plane
- $[R|t]$ = joint rotation-translation matrix (a.k.a. extrinsics parameters matrix), describing the camera pose, and translating from world coordinates to camera coordinates

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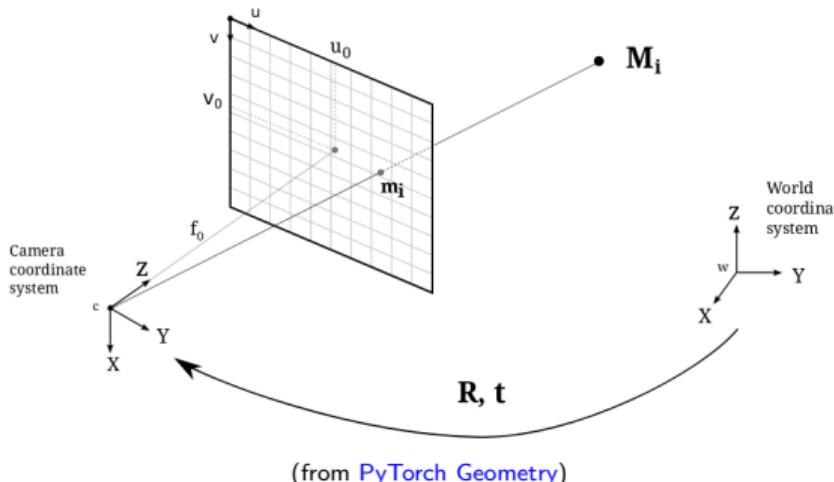
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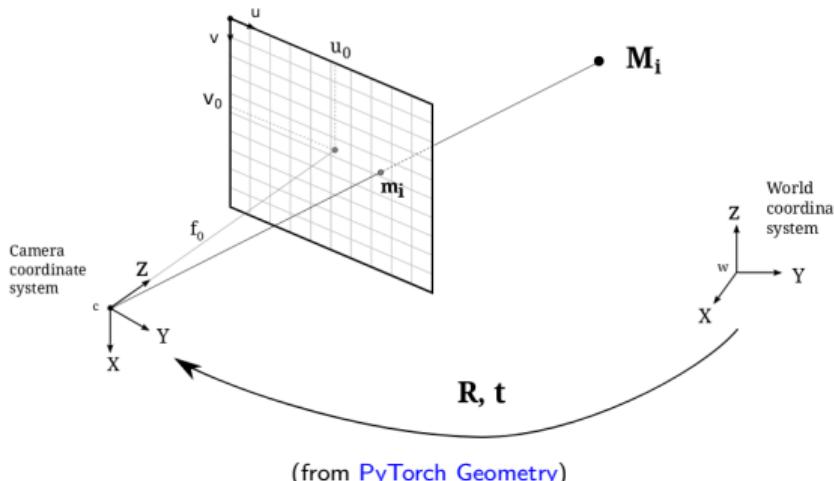
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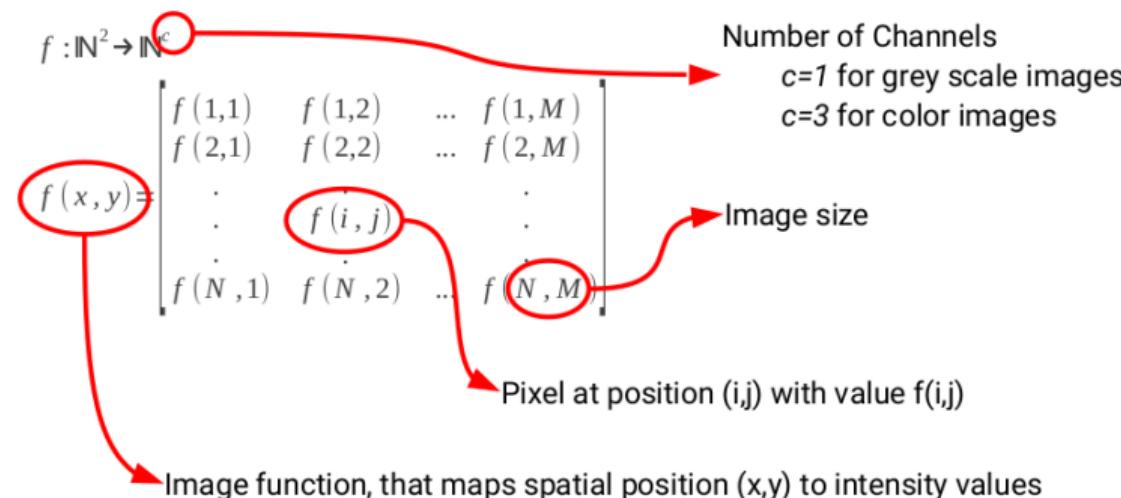
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⇒ digital image function $f(x, y)$



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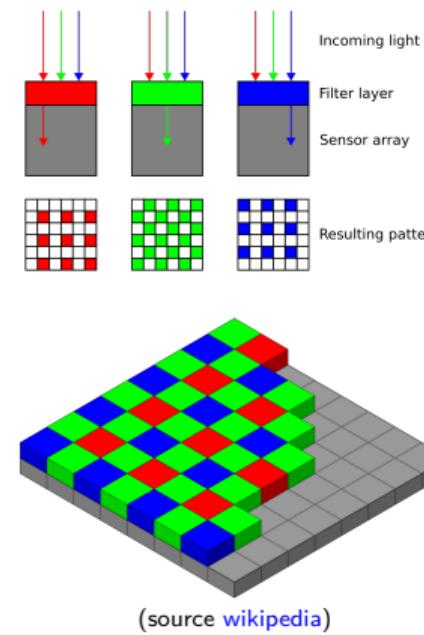
		columns									
		0	1	2	3	4	5	6	7	8	9
rows	0	8	24	67	103	87	79	176	138	94	180
	1	98	53	66	226	14	34	241	240	24	143
	2	228	107	60	58	144	251	137	93	86	130
	3	155	108	132	159	129	141	245	211	100	11
	4	91	187	67	135	49	175	193	61	14	183
	5	199	251	80	2	121	105	222	147	226	63
	6	181	27	56	238	113	158	176	47	167	109
	7	38	172	18	192	184	162	181	202	17	72
	8	13	106	30	17	53	68	178	232	91	219
	9	211	181	78	2	13	185	204	106	131	70

Typical ranges:

- $\text{uint8} = [0-255]$ (0=black, 255=white)
(8 bits = 1 byte = $2^8 = 256$ values per pixel)
- $\text{float32} = [0-1]$ (0=black, 1=white)
(32 bits = 4 bytes = 4.3×10^9 values per pixel)

How do we record colors?

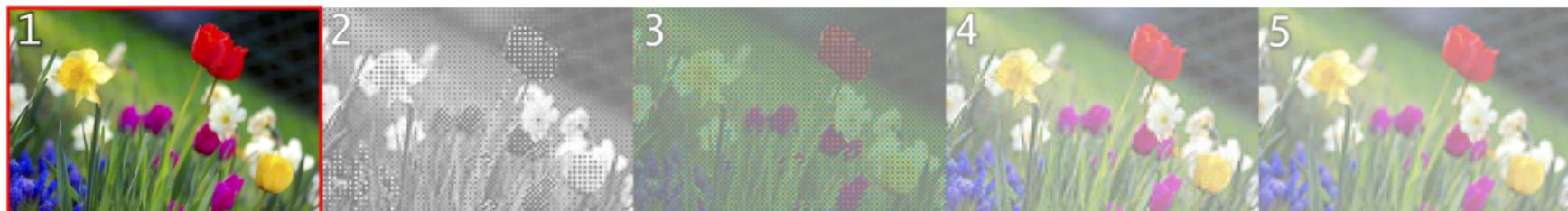
⇒ **Bayer Filter**: color filter array for arranging RGB color filters on a square grid of photosensors



NB: notice the filter pattern is 1/2 green, 1/4 red and 1/4 blue ⇒ more green photosensors are used in order to mimic the physiology of the human eye, which is more sensitive to green light.

How do we record colors?

⇒ **Bayer Filter**: color filter array for arranging RGB color filters on a square grid of photosensors



1. Original scene
2. Output of a 120×80 -pixel sensor with a Bayer filter
3. Output color-coded with Bayer filter colors
4. Reconstructed image after interpolating missing color information (a.k.a. demosaicing)
5. Full RGB version at 120×80 -pixels for comparison

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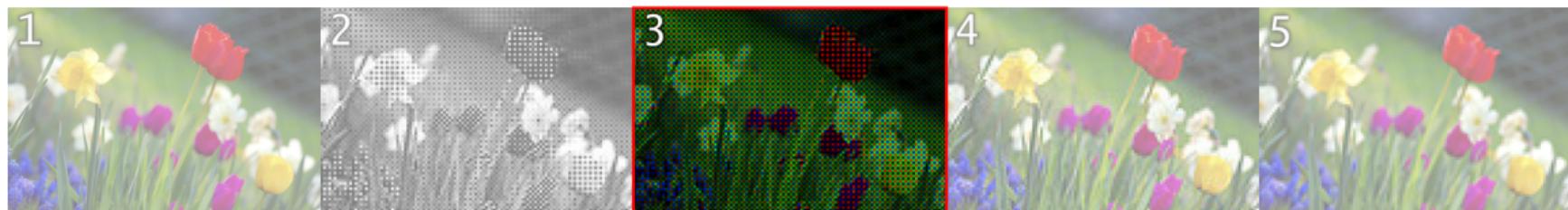


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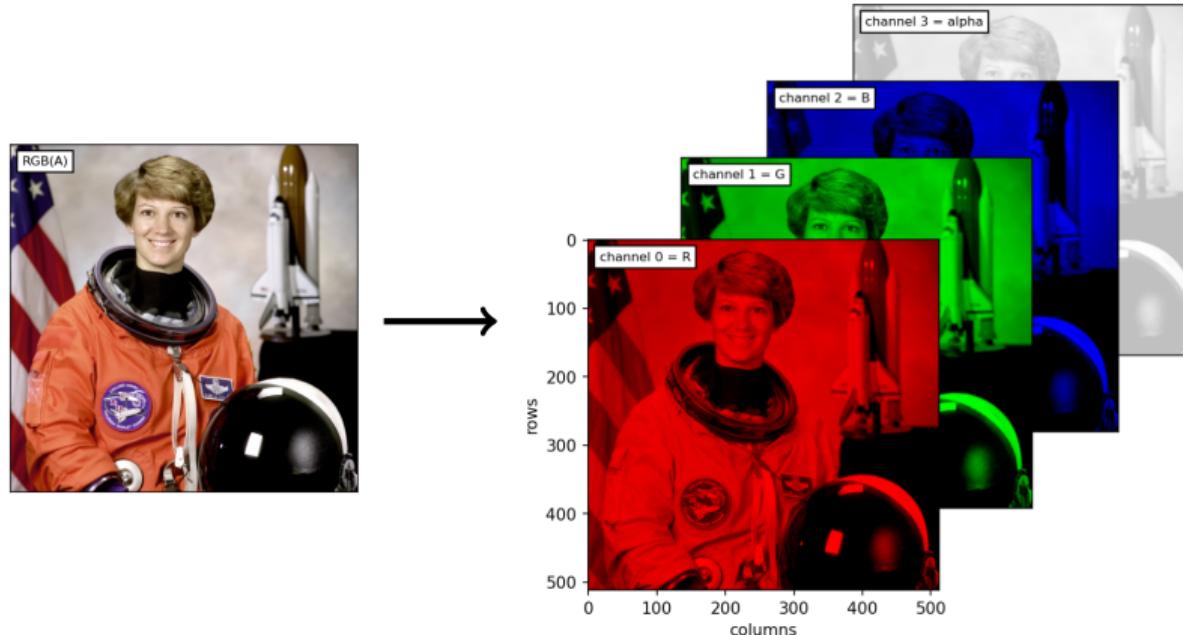


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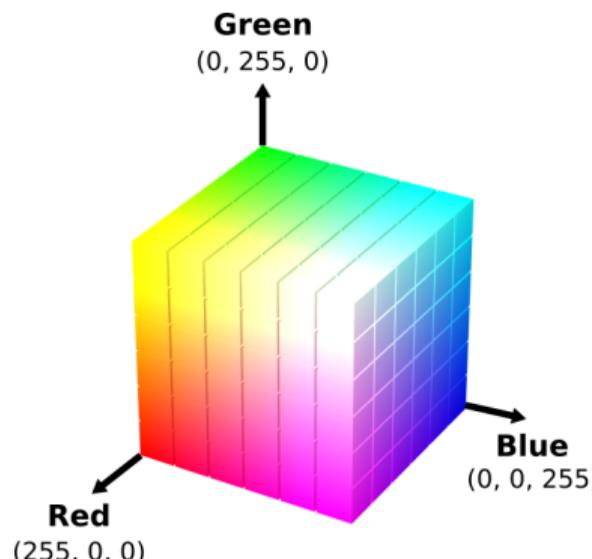
⇒ color image = 3D tensor in colorspace

- **RGB** = Red + Green + Blue bands (.JPEG)
- **RGBA** = Red + Green + Blue + Alpha bands (.PNG, .GIF, .BMP, TIFF, .JPEG 2000)

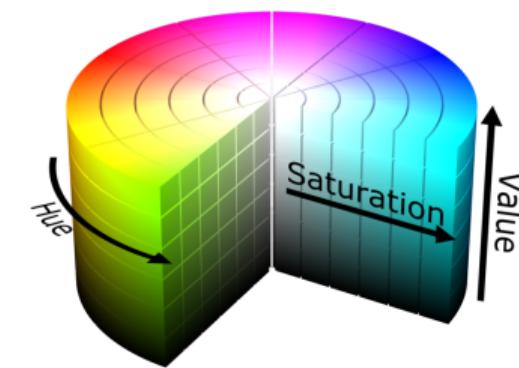


Other ways to represent the color information?

RGB colorspace



HSV colorspace

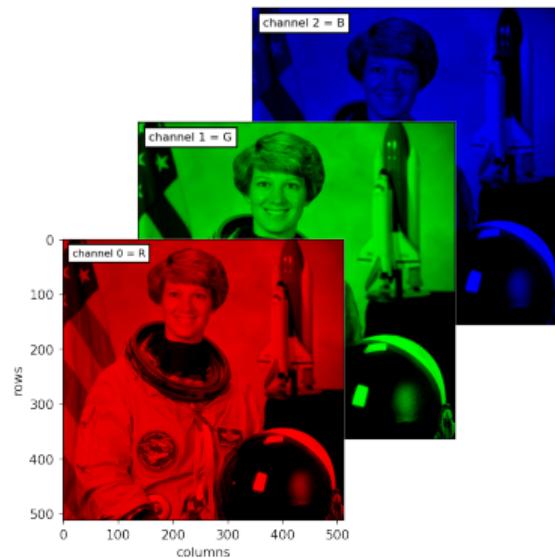


- Hue (H) = [0-360] ⇒ shift color
- Saturation (S) = [0-1] ⇒ shift intensity
- Value (V) = [0-1] ⇒ shift brightness

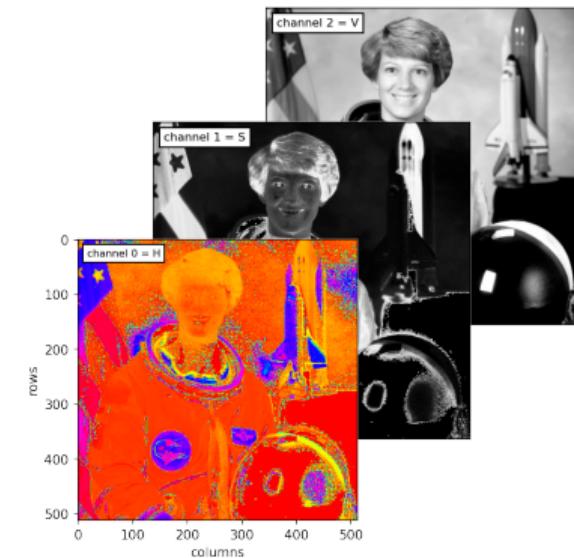
2.5. color spaces

3D tensor with different information:

RGB colorspace



HSV colorspace



2.5. color spaces

HSV allows for more intuitive color adjustments:

- more saturation S
⇒ more intense colors



- more value V
⇒ brighter colors

- shift hue H
⇒ shift color

2.5. color spaces

HSV allows for more intuitive color adjustments:

- more saturation S
⇒ more intense colors



- more value V
⇒ brighter colors



- shift hue H
⇒ shift color

2.5. color spaces

HSV allows for more intuitive color adjustments:

- more saturation S
⇒ more intense colors



- more value V
⇒ brighter colors



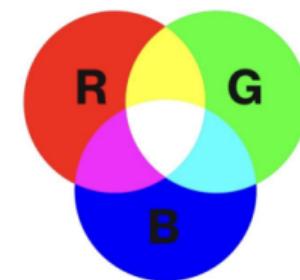
- shift hue H
⇒ shift color



Additive vs. Subtractive Color Models:

RGB (Additive Model)

- ⇒ used for devices that emit light (monitors, TVs, smartphones)
- ⇒ additive model: colors are created by combining different intensities of red, green, and blue light
 - combining all three colors at full intensity results in *white* light, absence of all results in *black*



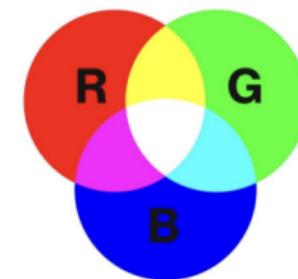
CMYK (Subtractive Model)

- ⇒ used for printing on paper and other physical media
- ⇒ subtractive color model: colors are created by subtracting light reflected off the paper
 - combining all three colors ideally absorb all light, resulting in *black* (NB: in printers black ink is added to achieve deeper blacks and reduce usage of the other inks)

Additive vs. Subtractive Color Models:

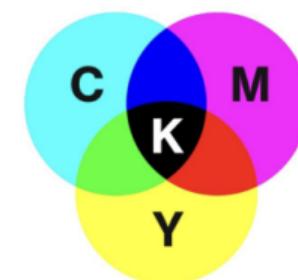
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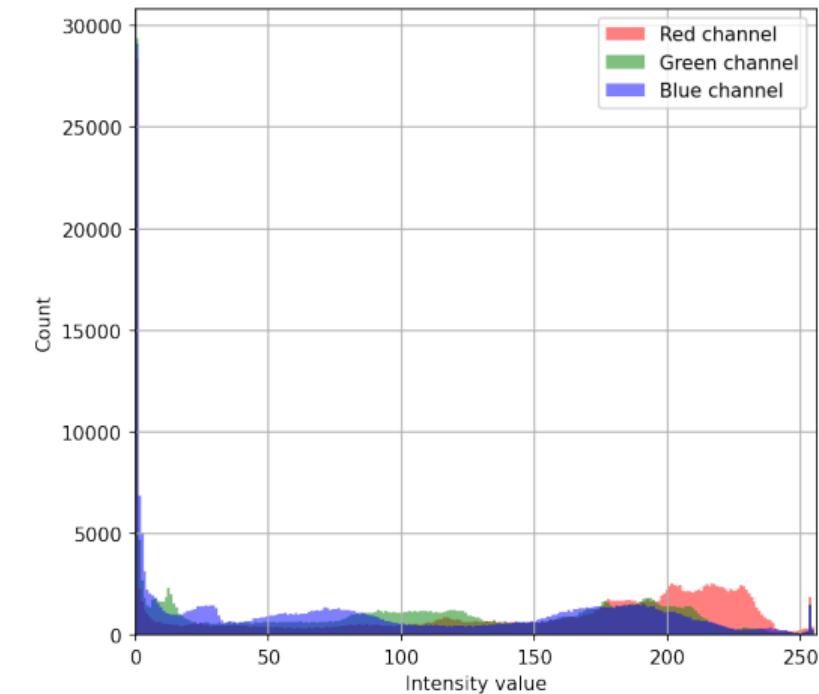
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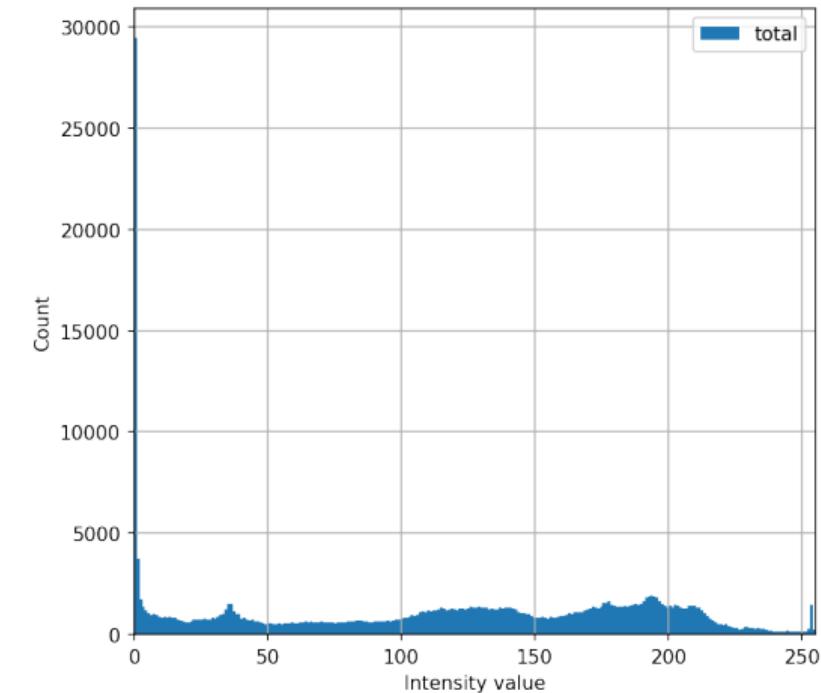
2.6. image histogram

Histogram of pixel values in each band:



2.6. image histogram

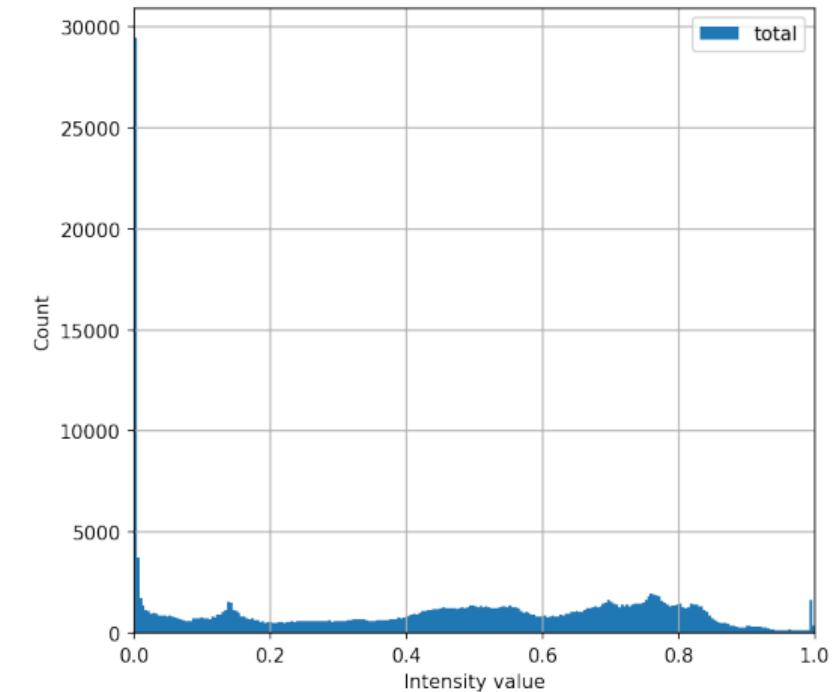
Histogram of pixel values after conversion from RGB (3-bands) to gray-scale (1-band):



NB: weights are chosen to mimic human perception of red, green and blue: the weight on the green band is larger because the human eye has greater sensitivity to green (the retina contains more photoreceptor cells (cones) that are tuned to detect green light)

2.6. image histogram

Histogram of pixel values after conversion to float values (range [0-1])



1. Motivation

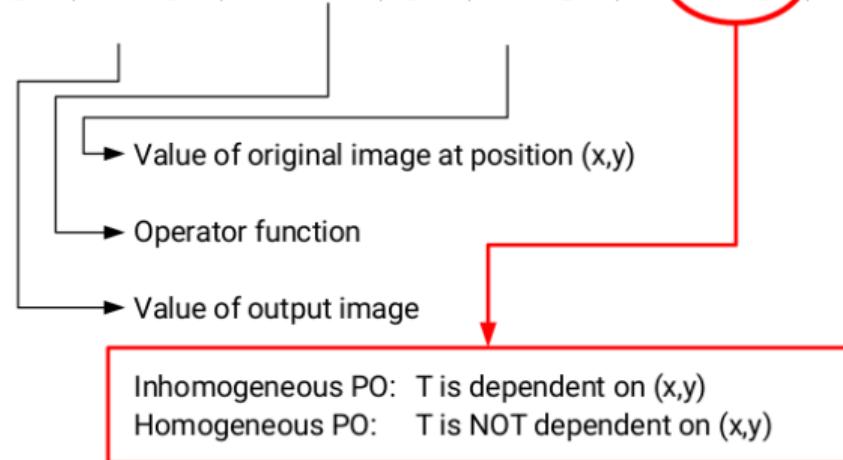
2. What is a digital image?

3. Point operations

1. homogeneous point operations
2. inhomogeneous Point Operations

4. Image manipulation with Python

$$g(x, y) = T(f(x, y), x, y)$$

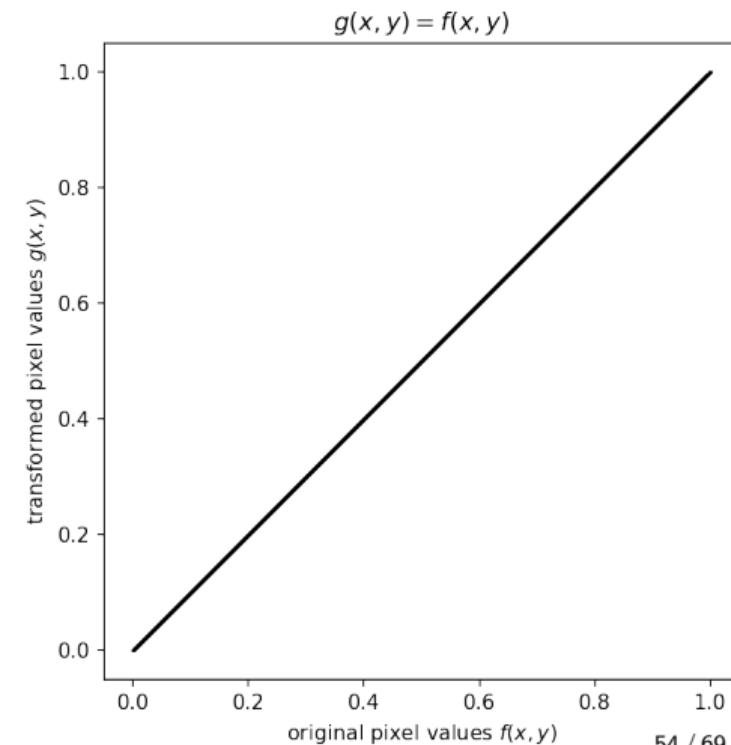


3.1. homogeneous point operations

Homogeneous Point Operations (does not depend on pixel position)

1. image intensity transformation using standard mathematical operations (\Rightarrow adjust pixel color 0=black / 1=white)

identity



3.1. homogeneous point operations

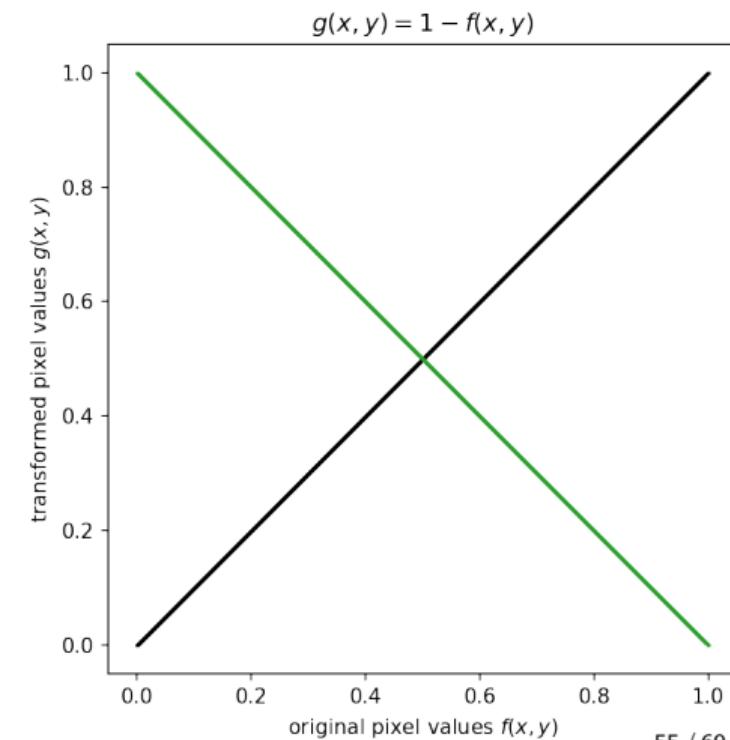
Homogeneous Point Operations (does not depend on pixel position)

1. image intensity transformation using standard mathematical operations (\Rightarrow adjust pixel color 0=black / 1=white)

identity



inverse



3.1. homogeneous point operations

Homogeneous Point Operations (does not depend on pixel position)

1. image intensity transformation using standard mathematical operations (\Rightarrow adjust pixel color 0=black / 1=white)

identity



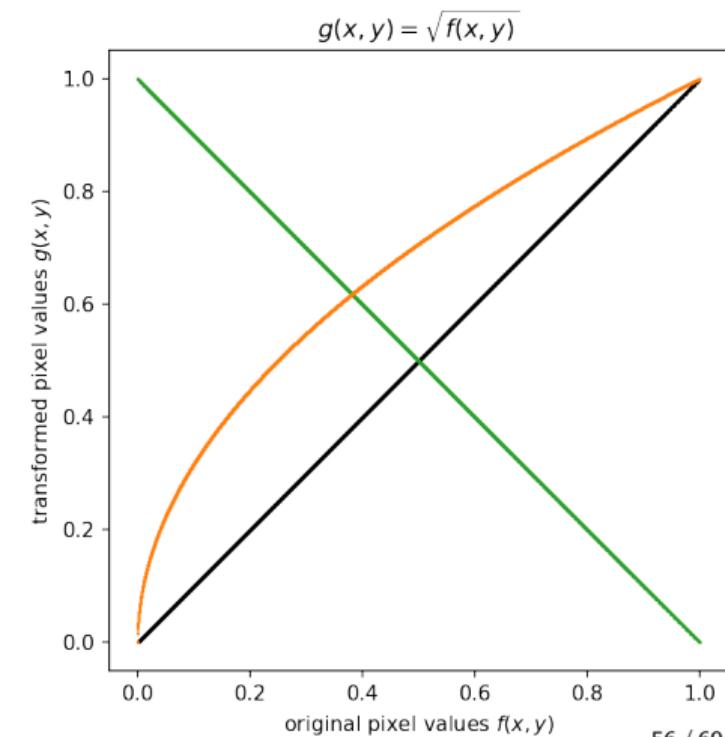
inverse



square root



$$g(x, y) = \sqrt{f(x, y)}$$



3.1. homogeneous point operations

Homogeneous Point Operations (does not depend on pixel position)

1. image intensity transformation using standard mathematical operations (\Rightarrow adjust pixel color 0=black / 1=white)

identity



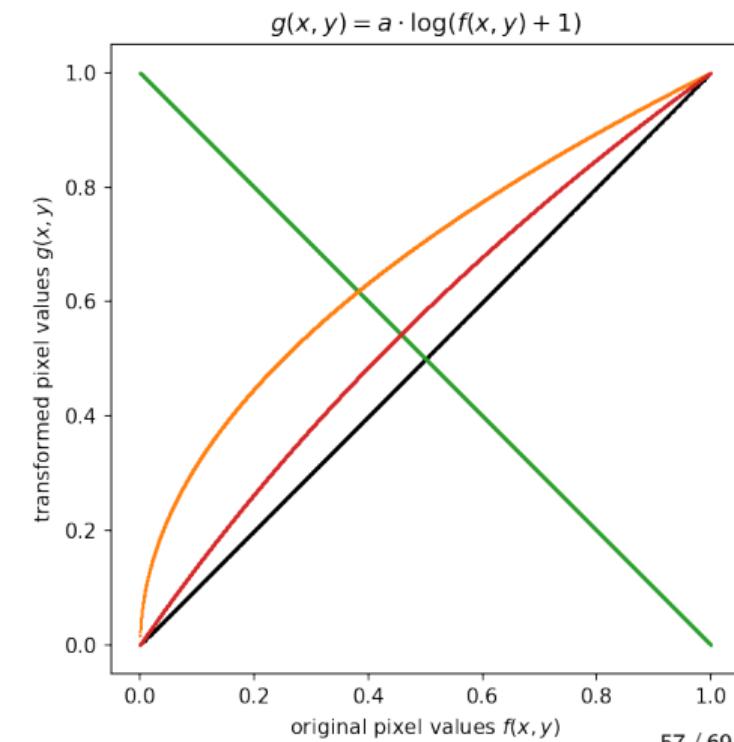
inverse



square root



logarithm



3.1. homogeneous point operations

Homogeneous Point Operations (does not depend on pixel position)

1. image intensity transformation using standard mathematical operations (\Rightarrow adjust pixel color 0=black / 1=white)

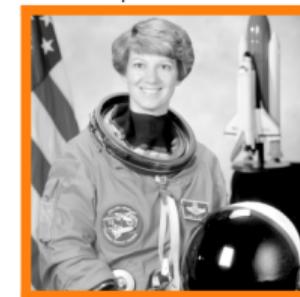
identity



inverse



square root



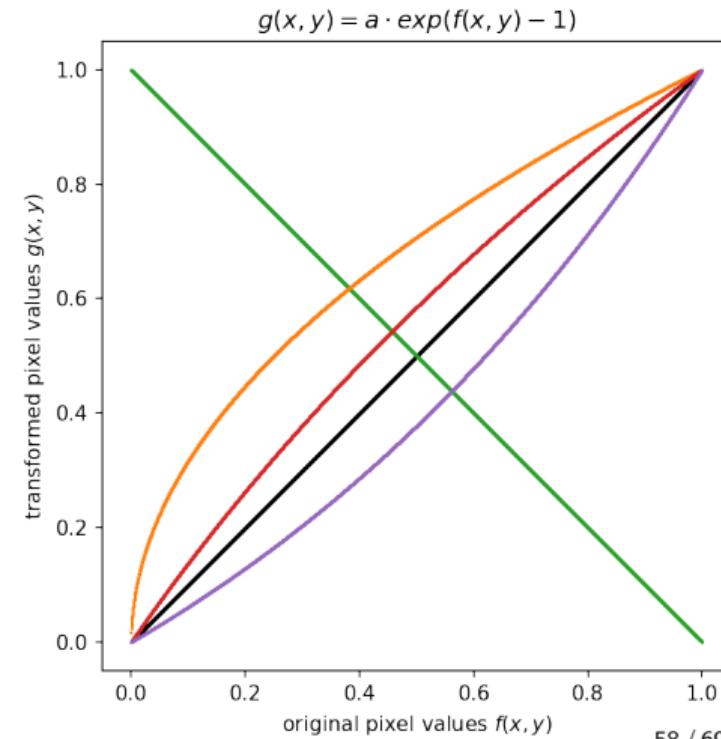
logarithm



exponential



$$g(x, y) = a \cdot \exp(f(x, y) - 1)$$



3.1. homogeneous point operations

Homogeneous Point Operations (does not depend on pixel position)

1. image intensity transformation using standard mathematical operations (\Rightarrow adjust pixel color 0=black / 1=white)

identity



inverse



square root



logarithm



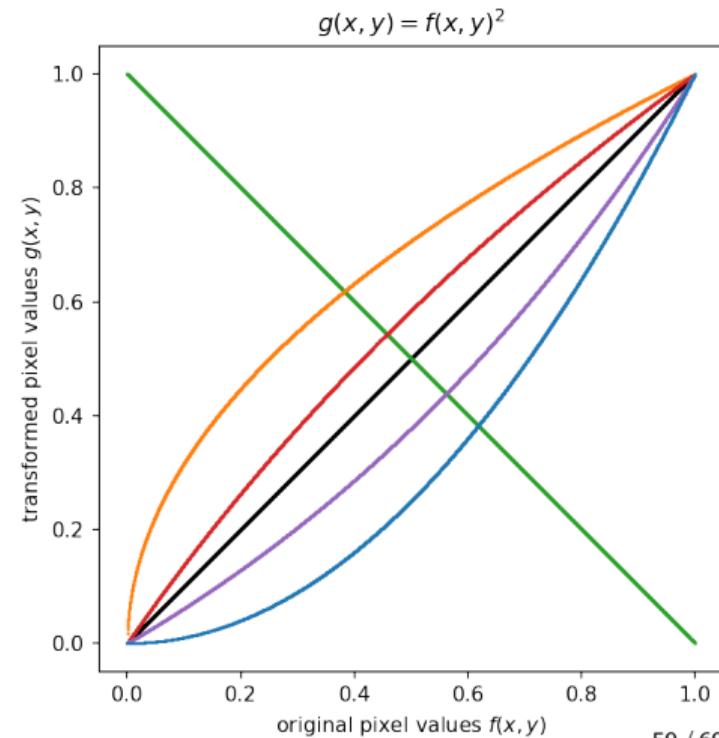
exponential



square



$$g(x, y) = f(x, y)^2$$

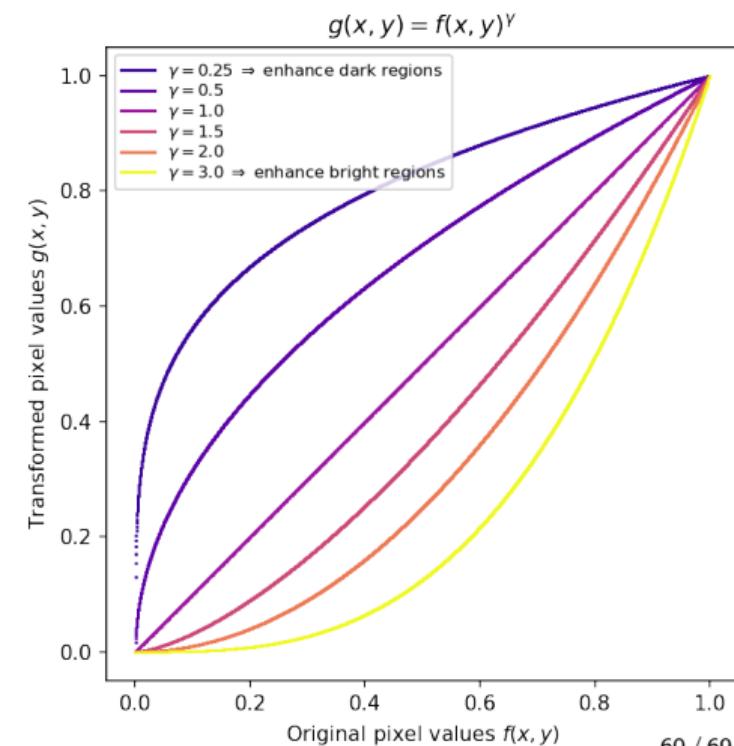
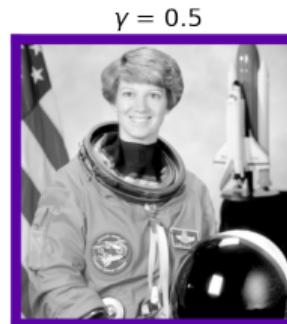


3.1. homogeneous point operations

Homogeneous Point Operations

 (does not depend on pixel position)

1. image intensity transformation using **Gamma correction** (\Rightarrow power-law transformation)



3.1. homogeneous point operations

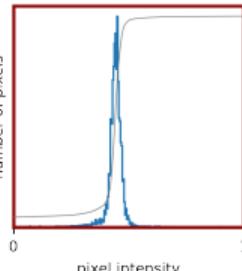
Homogeneous Point Operations (does not depend on pixel position)

2. image contrast adjustment (\Rightarrow adjust image histogram)

ORIGINAL image
low contrast



number of pixels



Original image (no stretch)

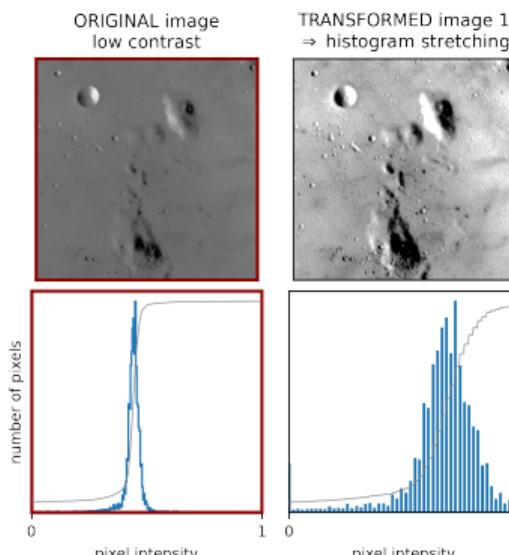
- \Rightarrow image pixel intensity values are limited to a narrow range
- \Rightarrow without stretch only a small portion of the full range of possible display levels is used
- \Rightarrow results in a low contrast image

Modified after: [skimage-tutorial](#)

3.1. homogeneous point operations

Homogeneous Point Operations (does not depend on pixel position)

2. image contrast adjustment (⇒ adjust image histogram)



Transformed image #1: linear histogram stretching

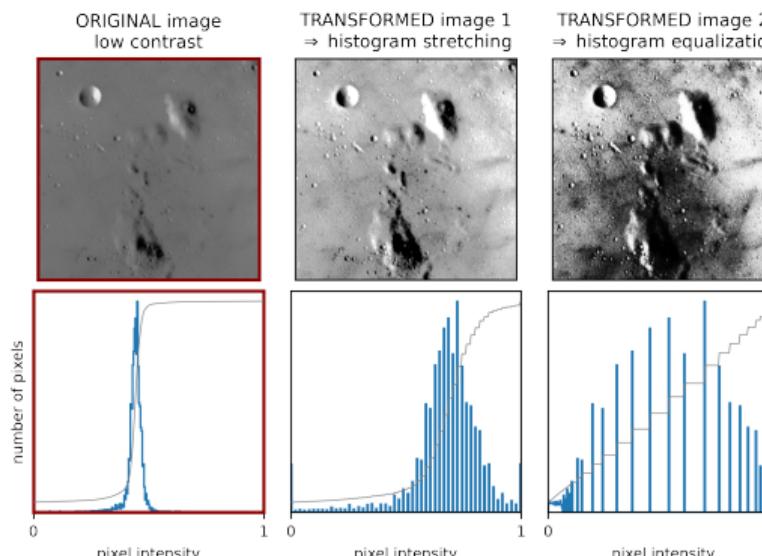
- ⇒ expand range of pixel intensities to stretch across full range of possible values
- ⇒ rescale pixel values to a specific range
EX: rescale pixel intensities between 2nd and 98th percentiles to occupy full 0-1 range

Modified after: [skimage-tutorial](#)

3.1. homogeneous point operations

Homogeneous Point Operations (does not depend on pixel position)

2. image contrast adjustment (⇒ adjust image histogram)



Transformed image #2: histogram equalization

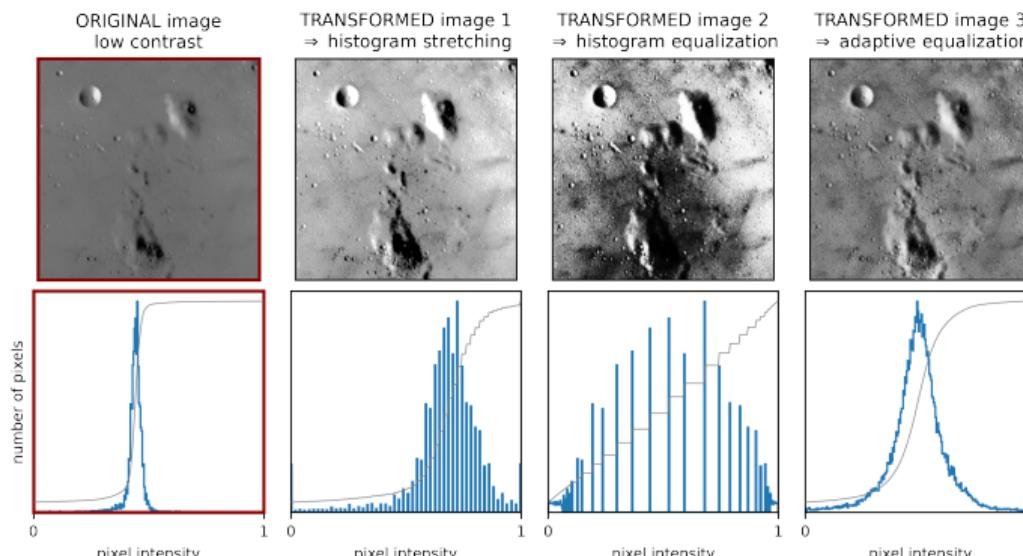
- ⇒ expand image pixel values on the basis of their frequency of occurrence (i.e. spreads out the most frequent intensity values)
- ⇒ equalized image has a roughly linear cumulative distribution function

Modified after: [skimage-tutorial](#)

3.1. homogeneous point operations

Homogeneous Point Operations (does not depend on pixel position)

2. image contrast adjustment (⇒ adjust image histogram)



Transformed image #3: adaptive histogram equalization

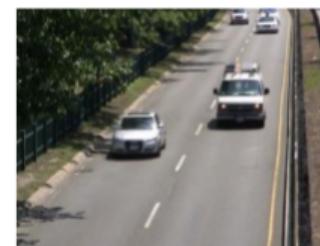
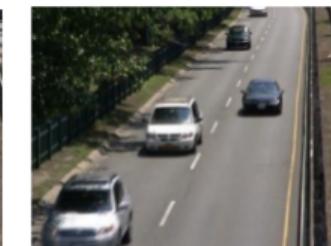
- ⇒ algorithm “Contrast Limited Adaptive Histogram Equalization” (CLAHE)
- ⇒ computes histograms over different regions of the image for local contrast enhancement
- ⇒ local details can be enhanced even in regions that are darker or lighter than most of the image

Modified after: [skimage-tutorial](#)

3.2. inhomogeneous Point Operations

Inhomogeneous Point Operations (depends on pixel position)

EX: background detection / change detection

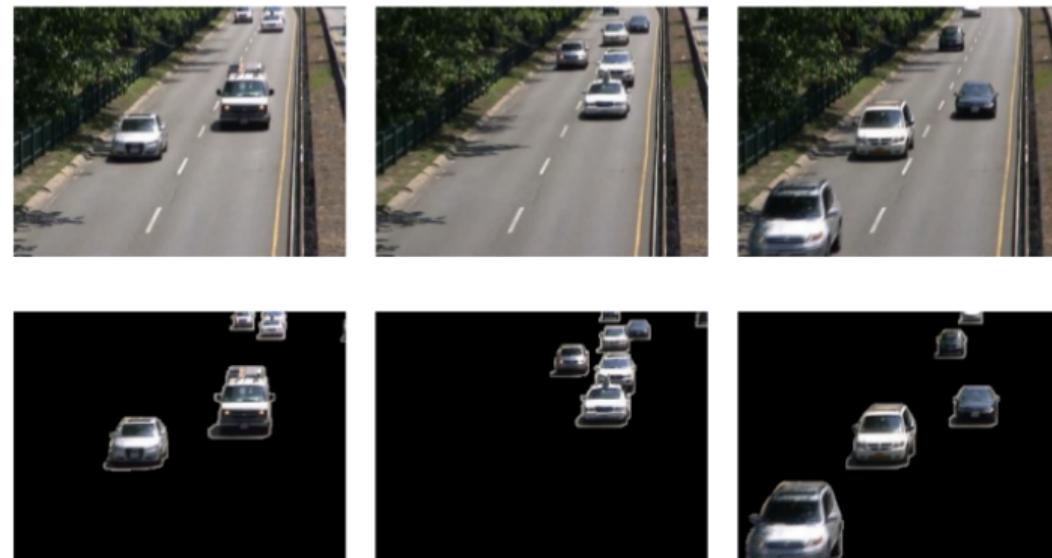
 f_1  f_i  f_N

$$a(x, y) = \frac{1}{N} \sum_{i=0}^N f_i(x, y)$$

$$\begin{aligned} g_i(x, y) &= T(f(x, y), x, y) \\ &= f_i(x, y) - a(x, y) \end{aligned}$$



3.2. inhomogeneous Point Operations

Inhomogeneous Point Operations (depends on pixel position)

1. Motivation
2. What is a digital image?
3. Point operations
4. Image manipulation with Python
 1. numpy tutorial
 2. exercises

4.1. numpy tutorial

Numpy tutorial:

⇒ Open CV4GS_02_image-basics/**CV4GS_02_numpy-tutorial.ipynb**

4.2. exercises

Exercices:

⇒ Open CV4GS_02_image-basics/**CV4GS_02_exercices.ipynb**