import pandas as pd
from openpyxl.workbook import Workbook

#reading excel file

In [2]:

#Top 5 rows of the Excel file
df.head()

Out[2]

t[2]:		Date	Ottawa	Toronto West/Ouest	Toronto East/Est	Windsor	London	Peterborough	St. Catharine's	Sudbury	Sault Saint Marie	Thunder Bay	N
	0	1990- 01-03	55.9	49.1	48.7	45.2	50.1	0.0	0.0	56.4	54.8	56.6	
	1	1990- 01-10	55.9	47.7	46.8	49.7	47.6	0.0	0.0	56.4	54.9	56.8	
	2	1990- 01-17	55.9	53.2	53.2	49.6	53.7	0.0	0.0	55.8	54.9	56.8	
	3	1990- 01-24	55.9	53.2	53.5	49.0	52.1	0.0	0.0	55.7	54.9	56.8	
	4	1990- 01-31	55.9	51.9	52.6	48.6	49.1	0.0	0.0	55.6	54.8	56.8	

In [3]:

 $\# Datatype \ and \ Null \ Information \ about \ the \ columns \ in \ the \ Excel \ file \ df.info()$

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 9962 entries, 0 to 9961
Data columns (total 20 columns):

Data	columns (total 20 columns):		
#	Column	Non-Null Count	Dtype
0	Date	9962 non-null	datetime64[ns]
1	Ottawa	9962 non-null	float64
2	Toronto West/Ouest	9962 non-null	float64
3	Toronto East/Est	9962 non-null	float64
4	Windsor	9962 non-null	float64
5	London	9962 non-null	float64
6	Peterborough	9962 non-null	float64
7	St. Catharine's	9962 non-null	float64
8	Sudbury	9962 non-null	float64
9	Sault Saint Marie	9962 non-null	float64
10	Thunder Bay	9962 non-null	float64
11	North Bay	9962 non-null	float64
12	Timmins	9962 non-null	float64
13	Kenora	9962 non-null	float64
14	Parry Sound	9962 non-null	float64
15	Ontario Average/Moyenne provinciale	9962 non-null	float64
16	Southern Average/Moyenne du sud de l'Ontario	9962 non-null	float64
17	Northern Average/Moyenne du nord de l'Ontario	9962 non-null	float64

```
memory usage: 1.5+ MB
In [4]:
        #Creating a new dataframe
        df2 = pd.DataFrame()
In [5]:
        #Choosing rows from the original dataframe with Fuel Type "Mid-Grade gasoline" and pasting
        df2 = df.loc[df['Fuel Type'] == 'Mid-Grade Gasoline']
In [6]:
        #Datatype and Null Information about the columns in the new dataframe
        df2.info()
       <class 'pandas.core.frame.DataFrame'>
       Int64Index: 1675 entries, 4937 to 6611
       Data columns (total 20 columns):
          Column
                                                         Non-Null Count Dtype
       --- ----
                                                         _____
                                                         1675 non-null datetime64[ns]
           Date
        1
           Ottawa
                                                         1675 non-null float64
        2 Toronto West/Ouest
                                                         1675 non-null float64
        3 Toronto East/Est
                                                         1675 non-null float64
           Windsor
                                                         1675 non-null float64
        4
        5 London
                                                         1675 non-null float64
        6 Peterborough
                                                         1675 non-null float64
        7
          St. Catharine's
                                                         1675 non-null float64
        8 Sudbury
                                                         1675 non-null float64
        9 Sault Saint Marie
                                                         1675 non-null float64
        10 Thunder Bay
                                                         1675 non-null float64
        11 North Bay
                                                         1675 non-null float64
        12 Timmins
                                                         1675 non-null float64
        13 Kenora
                                                         1675 non-null float64
        14 Parry Sound
                                                         1675 non-null float64
        15 Ontario Average/Moyenne provinciale
                                                         1675 non-null float64
        16 Southern Average/Moyenne du sud de l'Ontario 1675 non-null float64
        17 Northern Average/Moyenne du nord de l'Ontario 1675 non-null float64
                                                         1675 non-null object
        18 Fuel Type
        19 Type de carburant
                                                         1675 non-null object
       dtypes: datetime64[ns](1), float64(17), object(2)
       memory usage: 274.8+ KB
In [7]:
        df2.head()
Out[7]
```

9962 non-null object 9962 non-null object

18 Fuel Type

19 Type de carburant

dtypes: datetime64[ns](1), float64(17), object(2)

ut[7]:		Date	Ottawa	Toronto West/Ouest	Toronto East/Est	Windsor	London	Peterborough	St. Catharine's	Sudbury	Sault Saint Marie	Thunder Bay
	4937	1990- 01-03	58.3	51.1	51.0	47.4	52.3	0.0	0.0	58.6	57.6	58.7
	4938	1990- 01-10	58.3	50.1	49.6	51.8	50.0	0.0	0.0	58.6	57.6	58.8
	4939	1990- 01-17	58.3	55.5	55.5	51.8	56.0	0.0	0.0	57.9	57.6	58.9

		Date	Ottawa	Toronto West/Ouest		Windsor	London	Peterborough	St. Catharine's	Sudbury	Sault Saint Marie	Thunder Bay
	4940	1990- 01-24	58.3	55.6	55.8	51.2	54.4	0.0	0.0	57.9	57.6	58.8
	4941	1990- 01-31	58.2	54.3	55.0	50.8	51.4	0.0	0.0	57.8	57.7	58.9
In [8]:		_	<i>a new</i> DataFra	dataframe								
In [9]:	df3.	inser	t(0,"Da	-Grade Gasc ate",df2['D mmins",df2	oate'], T :	rue)		s Region onl	y and pas	ting it	into n	ew data
In [10]:	df3.	.head()									
Out[10]:			Date Tir	mmins								
	4937	1990-0)1-03	0.0								
	4938	1990-0)1-10	60.3								
	4939	1990-0)1-17	60.5								
	4940	1990-0)1-24	60.5								
	4941	1990-0)1-31	60.5								
In [11]:	#thi #dai df3.	is inc ily va .set_i	onisten lues. ndex('D		cting the	e date c e)	column i	he week star nto daily va				
Tn [12]·												

Out[12]: Date Timmins **11707** 2022-01-22 164.8 **11708** 2022-01-23 164.8 **11709** 2022-01-24 171.5 **11710** 2022-01-25 171.5 **11711** 2022-01-26 171.5 **11712** 2022-01-27 171.5 **11713** 2022-01-28 171.5 **11714** 2022-01-29 171.5

```
In [13]:
          #Checking for null values
          df3.isnull().values.any()
         False
Out[13]:
In [14]:
          #Splitting the "Date" column into year, month and week to explore trends
          df3['Year']=df3['Date'].dt.year
          df3['Month'] = df3['Date'].dt.month
          df3['Week'] = df3['Date'].dt.isocalendar().week
In [15]:
          df3.head(10)
                Date Timmins Year Month Week
Out[15]:
         0 1990-01-03
                           0.0 1990
         1 1990-01-04
                           0.0 1990
         2 1990-01-05
                           0.0 1990
         3 1990-01-06
                           0.0 1990
                                              1
         4 1990-01-07
                           0.0 1990
                                              1
         5 1990-01-08
                           0.0 1990
         6 1990-01-09
                           0.0 1990
                                              2
         7 1990-01-10
                          60.3 1990
                                              2
         8 1990-01-11
                          60.3 1990
                                              2
         9 1990-01-12
                          60.3 1990
                                              2
                                        1
In [16]:
          #Splitting the dataset in Train and Test
          #Train from Year 1990 to Year 2019
          #Test from Year 2020
          train = df3[(df3['Date'] > '1990-01-01') & (df3['Date'] <= '2019-12-31')]
          test = df3[df3['Date'] >= '2020-01-01']
```

Yearly Price Visualization on Train and Test Dataset

Date Timmins

171.5

171.7

11715 2022-01-30

11716 2022-01-31

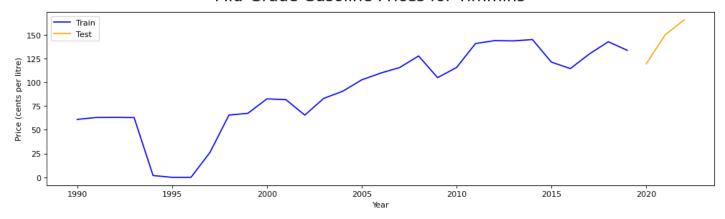
```
import matplotlib.pyplot as plt
from matplotlib.pyplot import figure

yearly_train_Price = train.groupby(['Year'])['Timmins'].mean()
yearly_test_Price = test.groupby(['Year'])['Timmins'].mean()

figure(figsize=(15, 4), dpi=80)
plt.plot(yearly_train_Price, label='Train',c='blue')
plt.plot(yearly_test_Price, label='Test',c='orange')
plt.legend(loc='best')
```

```
plt.suptitle('Mid-Grade Gasoline Prices for Timmins', fontsize=20)
plt.xlabel('Year')
plt.ylabel('Price (cents per litre)')
plt.show()
```

Mid-Grade Gasoline Prices for Timmins



DataPrep for Time Series

```
In [18]:
    train.index = pd.DatetimeIndex(train['Date'])
    #Changing the frequency of the index to Daily
    train.index = train.asfreq('d').index

    test.index = pd.DatetimeIndex(test['Date'])
    #Changing the frequency of the index to Daily
    test.index = test.asfreq('d').index
```

Train and Time Series Dataset

```
In [19]:
    train_time_series = pd.DataFrame()
    train_time_series.index = train.index
    train_time_series.insert(0, "Timmins Gas Price Train", train['Timmins'], True)

    test_time_series = pd.DataFrame()
    test_time_series.index = test.index
    test_time_series.insert(0, "Timmins Gas Price Test", test['Timmins'], True)

    print(train_time_series.tail())
    print(test_time_series.tail())
```

```
Timmins Gas Price Train
Date
2019-12-27
                               134.3
2019-12-28
                               134.3
2019-12-29
                               134.3
2019-12-30
                               133.8
2019-12-31
                               133.8
            Timmins Gas Price Test
Date
2022-01-27
                              171.5
2022-01-28
                              171.5
2022-01-29
                              171.5
2022-01-30
                              171.5
2022-01-31
                              171.7
```

ARIMA Model

To predict time series with ARIMA, we need to set the values of three parameters (p,d,q):

- p: The order of the auto-regressive (AR) model (i.e., the number of lag observations)
- d: The degree of differencing.
- q: The order of the moving average (MA) model.

Checking if data is stationary - We can see that it is not based on the P-value - Augmented Dickey Fuller Test

Taking First difference - P value is < 0.05. We can stop at the First Difference; d = 1

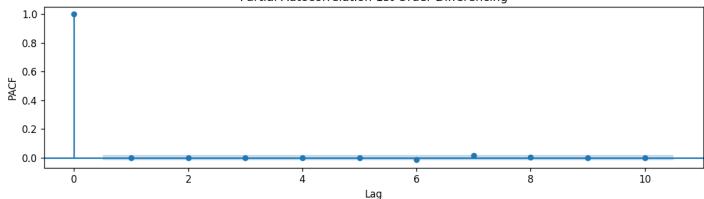
```
In [21]:
    train_time_series_stationary1 = train_time_series.diff().dropna()
    results1 = adfuller(train_time_series_stationary1['Timmins Gas Price Train'])
    print('ADF Statistic: ',results1[0])
    print('p-value: ',results1[1])
    print('Critical Values', results1[4])

ADF Statistic: -104.65223257600798
    p-value: 0.0
    Critical Values {'1%': -3.4309471727572607, '5%': -2.861803917364605, '10%': -2.5669104780 8449}
```

The Order of Autoregressive Term p; p = 0

```
In [22]:
    plt.rcParams.update({'figure.figsize':(12,3), 'figure.dpi':120})
    from statsmodels.graphics.tsaplots import plot_pacf
    plot_pacf(train_time_series_stationary1, lags=10, title="Partial Autocorrelation 1st Orde
    plt.xlabel('Lag')
    plt.ylabel('PACF')
    plt.show()
```

Partial Autocorrelation 1st Order Differencing

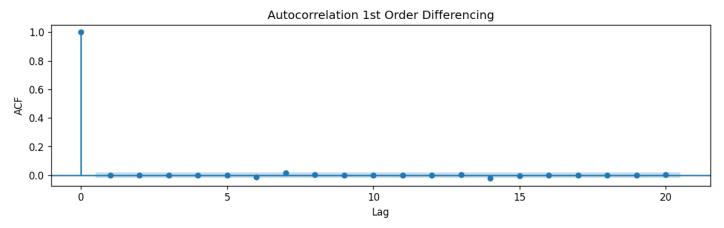


The order of the Moving Average term q; q = 0

Best model: ARIMA(0,1,0)(0,0,0)[0]

Total fit time: 4.449 seconds

```
In [23]:
    plt.rcParams.update({'figure.figsize':(12,3), 'figure.dpi':120})
    from statsmodels.graphics.tsaplots import plot_acf
    plot_acf(train_time_series_stationary1, lags=20, title="Autocorrelation 1st Order Different plt.xlabel('Lag')
    plt.ylabel('ACF')
    plt.show()
```



Check the above p,d,q parameters with Auto Arima - Best Model ARIMA (0,1,0)

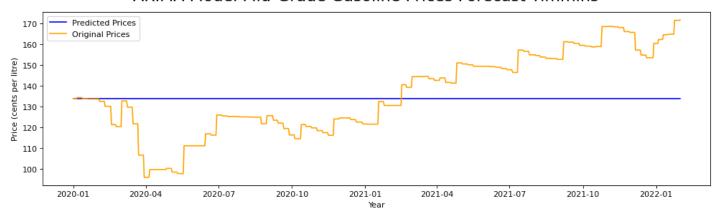
```
In [24]:
         import pmdarima as pm
         from pmdarima.model selection import train test split
         import numpy as np
         model1 = pm.auto arima(train time series, trace=True, error action='ignore', suppress warn
         model1.fit(train time series)
         forecast1 = model1.predict(n periods=len(test time series))
         forecast1 = pd.DataFrame(forecast1,index = test time series.index,columns=['Prediction'])
        Performing stepwise search to minimize aic
                                            : AIC=43128.532, Time=1.94 sec
         ARIMA(2,1,2)(0,0,0)[0] intercept
         ARIMA(0,1,0)(0,0,0)[0] intercept
                                            : AIC=43120.532, Time=0.27 sec
         ARIMA(1,1,0)(0,0,0)[0] intercept
                                           : AIC=43122.532, Time=0.53 sec
         ARIMA(0,1,1)(0,0,0)[0] intercept
                                            : AIC=43122.532, Time=0.75 sec
                                            : AIC=43119.077, Time=0.12 sec
         ARIMA(0,1,0)(0,0,0)[0]
                                            : AIC=43124.532, Time=0.82 sec
         ARIMA(1,1,1)(0,0,0)[0] intercept
```

Model Summary

plt.show()

```
In [25]:
       import statsmodels.api as sm
       model = sm.tsa.arima.ARIMA(train time series, order=(0,1,0))
       model result = model.fit()
       print(model result.summary())
                               SARIMAX Results
      ______
      Dep. Variable: Timmins Gas Price Train No. Observations: 10955
                                                            -21558.539
                           ARIMA(0, 1, 0) Log Likelihood
                         Sun, 06 Mar 2022 AIC
      Date:
                                                             43119.077
      Time:
                               12:04:27 BIC
                                                              43126.379
                             01-03-1990 HQIC
      Sample:
                                                              43121.538
                             - 12-31-2019
      Covariance Type:
                               opg
      ______
                  coef std err z P>|z| [0.025 0.975]
      ______
                2.9992
                         0.002 1816.150 0.000
                                                   2.996
      ______
      Ljung-Box (L1) (Q):
                                  0.00 Jarque-Bera (JB): 659991307.77
      Prob(Q):
                                  1.00 Prob(JB):
                                                                 0.00
      Heteroskedasticity (H):
                                  0.34 Skew:
                                                                 8.97
                                  0.00 Kurtosis:
                                                               1205.38
      Prob(H) (two-sided):
      _______
      Warnings:
      [1] Covariance matrix calculated using the outer product of gradients (complex-step).
      Model Prediction
In [26]:
       import warnings
       warnings.filterwarnings('ignore')
       ARIMA Predict = model result.predict(start='1/1/2020', end='1/31/2022')
       ARIMA Predict df = pd.DataFrame(ARIMA Predict)
In [27]:
       ARIMA Predict df.tail()
Out[27]:
              predicted_mean
      2022-01-27
                  133.8
      2022-01-28
                   133.8
      2022-01-29
                  133.8
      2022-01-30
                  133.8
      2022-01-31
                  133.8
In [28]:
       figure (figsize=(15, 4), dpi=80)
       plt.plot(ARIMA Predict df, label='Predicted Prices',c='blue')
       plt.plot(test time series, label='Original Prices',c='orange')
       plt.legend(loc='best')
       plt.suptitle('ARIMA Model Mid-Grade Gasoline Prices Forecast Timmins', fontsize=20)
       plt.xlabel('Year')
       plt.ylabel('Price (cents per litre)')
```

ARIMA Model Mid-Grade Gasoline Prices Forecast Timmins



Evaluation of the Model

Mean Absolute Error (MAE) ARIMA

```
In [29]:
    from sklearn.metrics import mean_absolute_error
    maeARIMA=mean_absolute_error(test_time_series['Timmins Gas Price Test'], ARIMA_Predict)
    print('Mean Absolute Error ARIMA = {}'.format(round(maeARIMA, 2)))

Mean Absolute Error ARIMA = 16.77
```

Mean squared error (MSE) ARIMA

```
from sklearn.metrics import mean_squared_error
mseARIMA=mean_squared_error(test_time_series['Timmins Gas Price Test'], ARIMA_Predict)
print('The Mean Squared Error ARIMA = {}'.format(round(mseARIMA, 2)))
```

Root mean squared error (RMSE) ARIMA

The Mean Squared Error ARIMA = 382.57

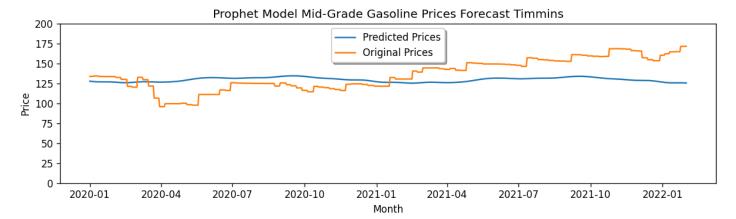
```
In [31]:
    from numpy import sqrt
    rmseARIMA = sqrt(mseARIMA)
    print('The Root Mean Squared Error ARIMA = {}'.format(round(rmseARIMA, 2)))
```

The Root Mean Squared Error ARIMA = 19.56

Prophet Model

```
In [33]: future = model_prophet.make_future_dataframe(periods=765)
    forecast = model_prophet.predict(future)
    forecast = forecast[(forecast['ds'] >= '2020-01-01') & (forecast['ds'] <= '2022-01-31')]</pre>
```

```
In [34]: fig, ax = plt.subplots()
    ax.plot(forecast['ds'], forecast['yhat'], label='Predicted Prices')
    ax.plot(test['Date'], test['Timmins'], label='Original Prices')
    plt.ylim([0,200])
    legend = ax.legend(loc='upper center', shadow=True)
    plt.title('Prophet Model Mid-Grade Gasoline Prices Forecast Timmins')
    plt.xlabel('Month')
    plt.ylabel('Price')
    plt.show()
```



Mean Absolute Error (MAE) Prophet

```
In [35]: maeProphet=mean_absolute_error(test['Timmins'],forecast['yhat'])
    print('Mean Absolute Error Prophet = {}'.format(round(maeProphet, 2)))
```

Mean Absolute Error Prophet = 17.76

Mean squared error (MSE) Prophet

```
In [36]: mseProphet = mean_squared_error(test['Timmins'], forecast['yhat'])
    print('The Mean Squared Error Prophet = {}'.format(round(mseProphet, 2)))
```

The Mean Squared Error Prophet = 425.86

Root mean squared error (RMSE) Prophet

```
In [37]:
    rmseProphet = sqrt(mseProphet)
    print('The Root Mean Squared Error Prophet = {}'.format(round(rmseProphet, 2)))
```

The Root Mean Squared Error Prophet = 20.64