

# Time Series

## Midterm project

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### Part 1

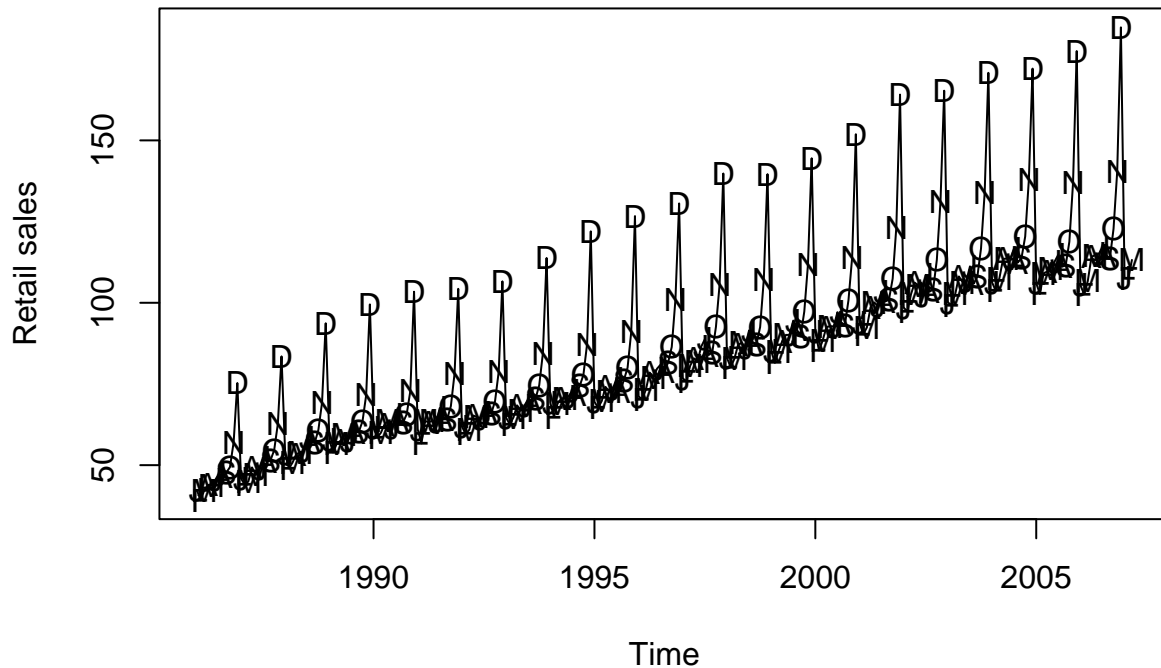
#### 1.

I am expecting a somewhat clear upward trend due to the increase in the population. Also, there could be a seasonal trend, such that the retail sales are higher on special holidays. Since the Brexit was later than 2007, I am not expecting a big sink somewhere in the graph.

```
library(TSA)
```

```
data(retail)
plot(retail, xlab = expression("Time"), ylab = expression("Retail sales"),
     main = expression("Time Series Plot of Retail sales"))
points(retail, pch = as.vector(season(retail)))
```

# Time Series Plot of Retail sales



Seeing the actual graph, I can confirm the upward trend and also a very strong seasonal behaviour. I clearly expected more holidays to be that present as christmas. There surely is a really strong seasonal behaviour due to christmas. This means that the sales are going up starting November each year and reach the peak in December before dropping again.

## 2.

I would try a seasonal ARIMA model, given the upward trend and the potential seasonality.

```
model <- forecast::auto.arima(retail, seasonal = TRUE)
summary(model)
```

```
## Series: retail
## ARIMA(1,0,4)(0,1,1)[12] with drift
##
## Coefficients:
##      ar1      ma1      ma2      ma3      ma4      sma1      drift
##      0.8469 -0.5939  0.0504  0.0878  0.1742 -0.0966  0.3083
## s.e.  0.0533  0.0788  0.0740  0.0772  0.0756  0.0631  0.0405
##
## sigma^2 = 3.413: log likelihood = -491.04
## AIC=998.07  AICc=998.69  BIC=1026.02
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE
```

```
## Training set -0.0003999956 1.777353 1.287341 -0.1007814 1.485438 0.3327206
##               ACF1
## Training set 0.00339952
```

### Model type and coefficients

Looking at the summary, we are given an ARIMA model with  $p = 1$ ,  $d = 0$ ,  $q = 4$ , where  $q$  is the autoregressive order with the coefficient  $ar_1 = 0.8469$ , also known as the lag order.  $d$  is the number of differences we take, which is 0, so that indicates that the data is already stationary. And  $q$  is the order of the moving average process, where the coefficients are  $ma_1 = -0.5939$ ,  $ma_2 = 0.0504$ ,  $ma_3 = 0.0878$ ,  $ma_4 = 0.1742$ . Speaking in a sentence, we have a first order degree autoregressive model with zero order of differencing and a fourth order moving average model. That was for the non-seasonal part. For the seasonal part, we have  $p = 0$ ,  $d = 1$ ,  $q = 1$ , where  $p$ ,  $d$  and  $q$  are exactly as above. The number 12 in brackets just states the number of seasons (here: months).

### Fit

We have some values to rate the model fit, which are

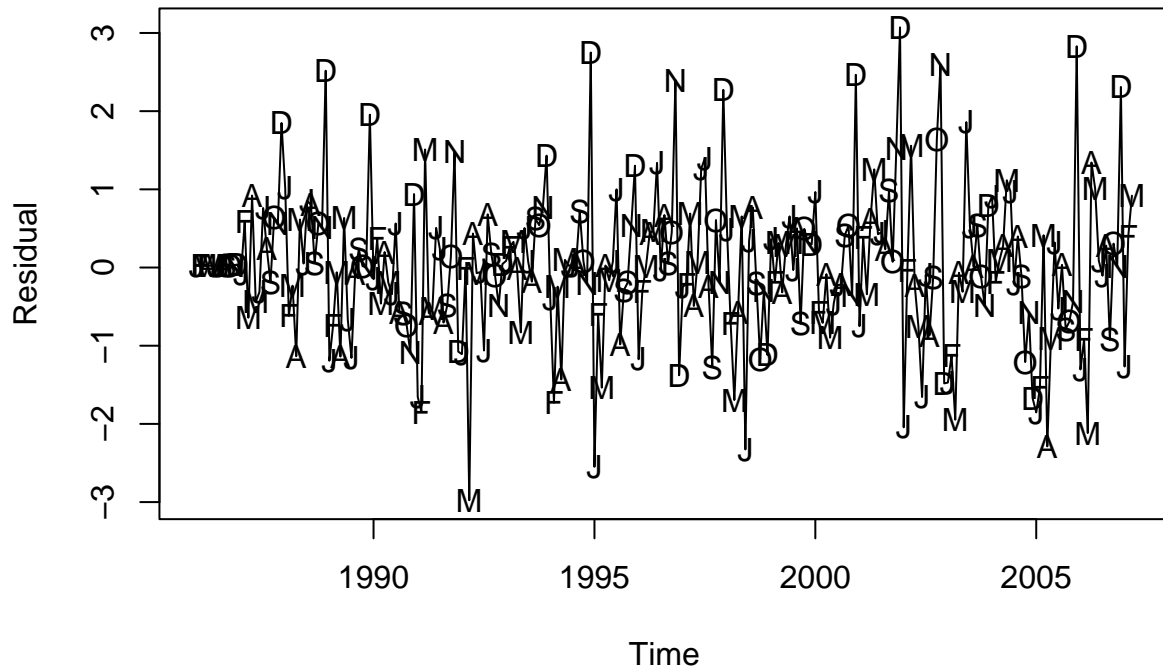
$$\begin{aligned}\sigma^2 &= 3.413, \\ \log \text{likelihood} &= -491.04, \\ AIC &= 998.07, \\ AICc &= 998.69, \\ BIC &= 1026.02.\end{aligned}$$

Here, we can just look at AIC and BIC which suggest a reasonable choice based on model complexity vs fit. The other values are basically for forecasting reasons.

### 3.

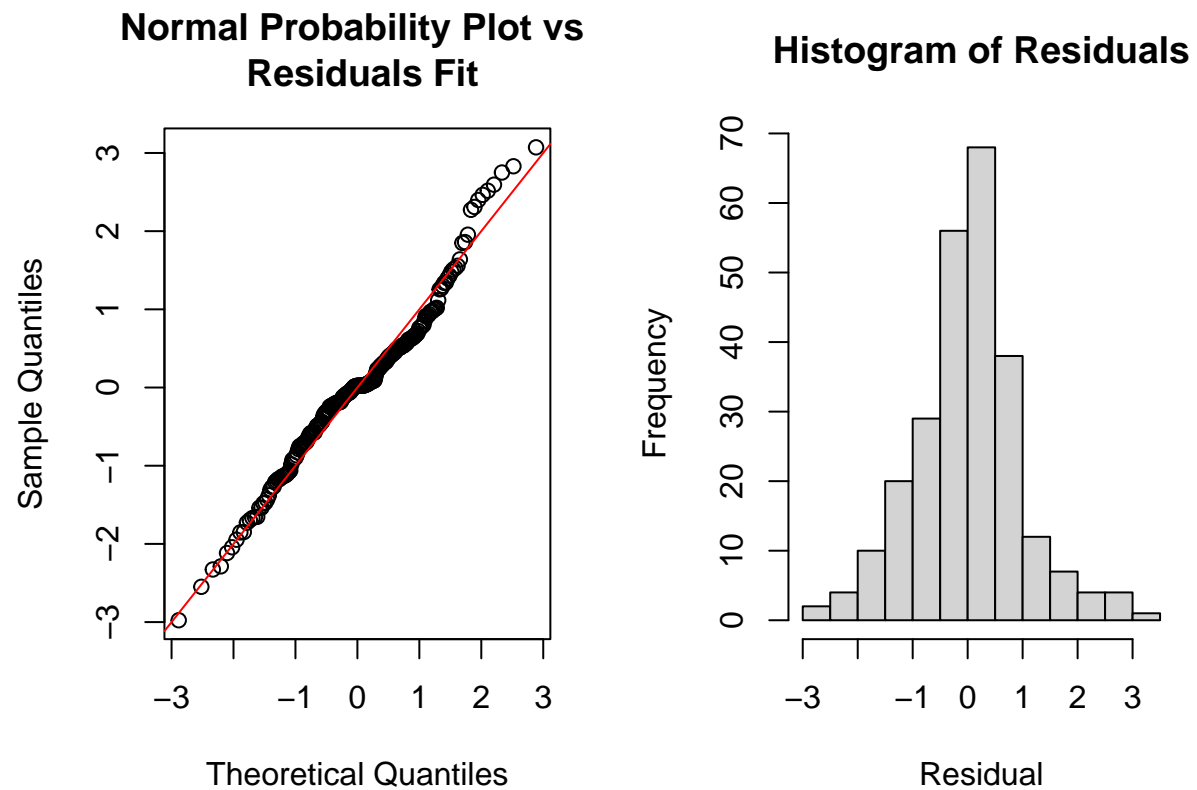
```
res <- ts(rstandard(model), start = c(1986, 1), end = c(2007,
3), frequency = 12)
plot(res, xlab = "Time", ylab = "Residual", main = "Time Series Plot of Residuals")
points(y = res, x = time(res), pch = as.vector(season(res)))
```

## Time Series Plot of Residuals



The plot of the residuals is kind of displaying the seasonal/periodic behaviour.

```
par(mfrow = c(1, 2))
qqnorm(res, main = "Normal Probability Plot vs \n Residuals Fit")
abline(a = 0, b = 1, col = "red")
hist(res, xlab = "Residual", main = "Histogram of Residuals")
```



The residuals look like they are normally distributed, indicating a good model fit.

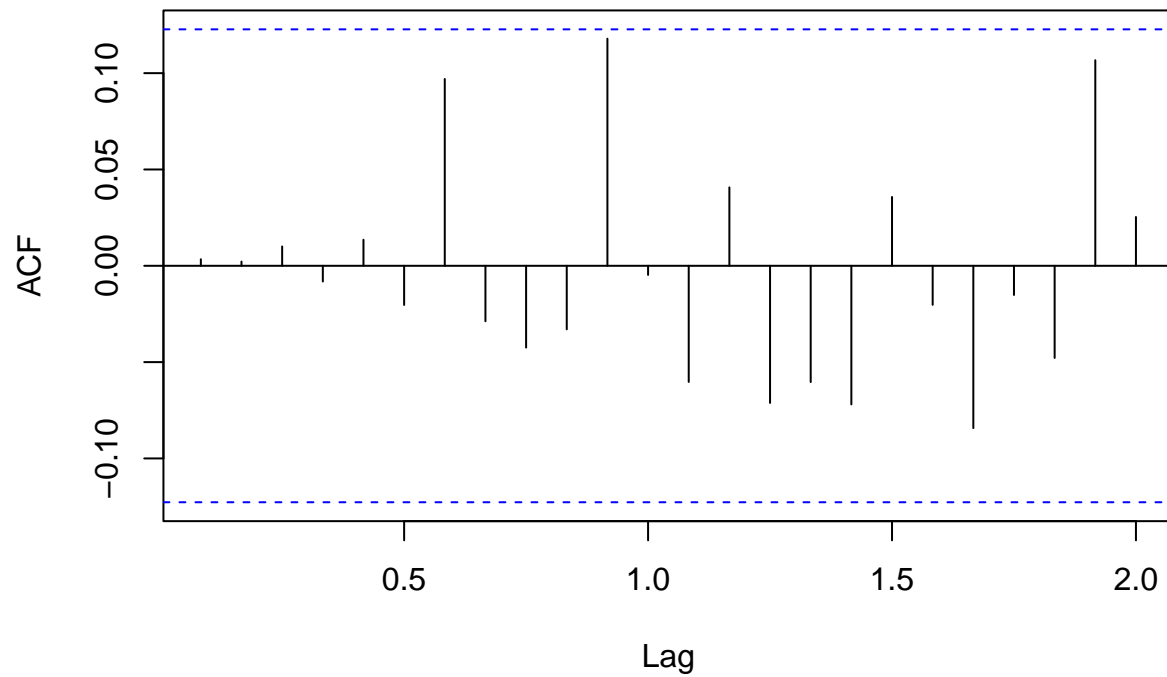
```
shapiro.test(res)
```

```
##  
##  Shapiro-Wilk normality test  
##  
## data:  res  
## W = 0.97597, p-value = 0.0002613
```

Since the p-value of the Shapiro-Wilk test is also really low, we can say that they are normally distributed.

```
acf(res, main = "Autocorrelation Plot of Residuals")
```

## Autocorrelation Plot of Residuals



Since there are just some “spikes” which are not at all big, the chosen model seems to capture the time-series pretty well. Also, no value is outside of the confidence interval.

## Part 2

```
data <- as.ts(read.delim(file = "../homework/MidtermPt2.txt",
  header = TRUE, sep = " "))
plot(data, main = "Original Series")
```

**Original Series**

