

~~Ans~~ 26-11
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Course :- B. Tech CSE

Subject :- Theory Of
Computation

CAPSTONE
ASSIGNMENT

Unit -1 Finite Automata and Regular Expression

Regular Expression for valid Identifiers

Let ΣA be the set of alphabets and Σd be the set of digits
 The regular expression R for all valid identifiers (alphabet followed by any sequence of alphabets or digits) is

$$R = (\Sigma A) (\Sigma A \cup \Sigma d)^*$$

The keywords (for, while, if) are excluded in the lexical analysis phase following token recognition

2. Design a DFA equivalent to R

The DFA $M = \{Q, \Sigma, \delta, q_0, F\}$

$$Q = \{q_0, q_1, q_f\}$$

q_0 = start state

q_1 = accepting state (valid identifier started)

q_f = dead state (invalid start)

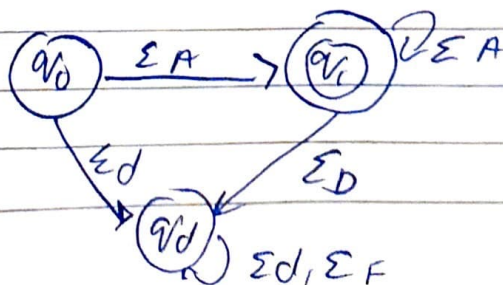
$$\Sigma = \Sigma A \cup \Sigma d$$

$$F = \{q_1, \text{is final state}\}$$

Transition Table

State	Input ΣA	Input Σd	Input (other)
q_0	q_1	q_f	q_f
q_1	q_1	q_1	q_1 (loop)
q_f	q_f	q_f	q_f

DFA Diagram



3 Embedding the DFA in a lexical analyzer The DFA acts as the state machine for recognizing the patterns of an Identifier

Q 1 DFA Recognition: The lexer consume input character receiving DFA's state & when the input stream ~~passes~~ forces the DFA out of q_i (encountering a space or operator) the operator reader to that point is identified as a potential token

2 Keyword check: The recognized string is then checked against a small, finite list of reserved keywords (for while, if) This is typically done via a fast hash table lookup

3 Token generation

• If the string is found in the keyword list, a keyword token is generated

• otherwise a Identifier token is generated and its entry (lemma and type) is stored in the Symbol Table

Q 2 Unit 2 DDA and Context free language

Formulate a CFG for well formed queries

let $O = \langle \text{open} \rangle$ and $C = \langle \text{/close} \rangle$, The grammar and include balanced nesting

$S \rightarrow OSC/SS/E$

$S \rightarrow OSC$ handles nested structure (eg $\langle \text{open} \rangle \dots \langle \text{/close} \rangle$)

$S \rightarrow SS$ handles concatenated structures (eg $\langle \text{open} \rangle \langle \text{/close} \rangle \langle \text{open} \rangle$)

$S \rightarrow \epsilon$ handles empty query

- 2 Construct a PDA that accept such queries
The PDA accept the language by empty stack. It uses the stack to track unmatched <open> tags

$M = (Q, \Sigma, \Gamma, \delta, q_0, \epsilon, \{ \})$

State	Input	Top of Stack	New State	Stack operation
q_0	O	z_0	q_0	Push x for first O
q_0	O	x	q_0	Push x for nested O
q_0	C	x	q_0	Pop x for matching C
q_0	ϵ	z_0	q_0	Accept by empty stack

- 3 ~~Demonstrate~~ Demonstrate the parse tree
Query: $\langle open \rangle \langle open \rangle \langle /close \rangle \langle /close \rangle$

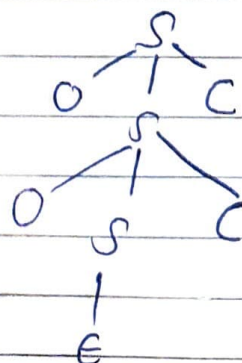
Derivation

$$S \Rightarrow OSC$$

$$S \Rightarrow O(OSC)C \quad (S \rightarrow OSC)$$

$$S \Rightarrow OCOEC)C \quad (S \rightarrow \epsilon)$$

parse tree:



Q3 Unit 3 Turing machine and Chomsky Hierarchy

① Justify why $L = \{a^n b^n c^n / n \geq 1\}$ is not context free using pumping lemma for CFL

Choose string S : let P be the pumping length choose $S \in L$
 $S = a^P b^P c^P \in L$

Decompose S : $S = uvwxy$ where $|vwx| \leq P$ and $|vx| \geq 1$

Pumping argument. Since $|vwx| \leq P$ the pumpable segment vwx can only contain symbol from at most two blocks (only a 's and b 's, or only b 's and c 's)

Case 1 vwx is in a 's and b 's) pumping up $i=2$) ↑ The no. of a 's and/or b 's but leaves the number of c 's fixed at P

Resulting string $S' = uv^2wx^2y$ has unequal counts of a 's, b 's and c 's (specifically, $\text{count}(a) + \text{count}(b) > \text{count}(c)$)

Conclusion $S' \notin L$, since the condition of the pumping lemma are violated, L can't be a CFL

2 Design a Turing machine (TM) that accepts Th TM mark one a , one b , one c in the cycle until all symbols are marked

Tape alphabet $F = \{a, b, c, x, y, z, \square\}$ (x, y, z are markers)

q_0 : mark the left most a as x and transition to find b

q_2 : Find the left most ~~un~~ unmarked b and mark it as y then transition to find c

q_0 : Find the left most unmarked c and mark it as z. Then transition to return

q_{ret} : soon left the starting point (x)

q_{check} : After all are marked, scan right to ensure the rest of the tape is just y's z's and finally \square (CB)

Step by Step configuration for 'aaabbbccc'

The TM cycles three times to mark the three points

Cycle 1 (mark a_1, b_1, c_1): q_0 aaabbbccc \rightarrow q_0 xaabbbccc
(mark a) \rightarrow q_1/b , xaaybbcc (mark b) \rightarrow q_{ret} xaaybbccc
(mark c), return left) \rightarrow q_0 , xaaybbzcc (Restart)

Cycle 2 (mark a_2, b_2, c_2) and q_0 xaabbbccc \rightarrow q_{ret} xaayybzz
(Tape becomes ~~xxaayybzzc~~)

Cycle 3 (mark a_3, b_3, c_3): q_0 xxaayybzzc \rightarrow q_{ret} xxxxyyzzz

Final check (q_{check}): q_0 read the marked a's (x's)
Transition to q_{check} , q_{check} scans y's and z's
until it hits \square check xxxxyyzzz

Unit-4 code generation and optimization

Explain

Expression $(A+B) * (C-D) + E$

Syntax - Directed translation scheme (Sathiraj) using a simple ~~free~~ procedure-based grammar

Production Semantic Rules

$E_1 + T$ $E.addT = \text{new temp}(C); T.addcode || T.code ||$
 $E.addT = E.addT + T.addT$

$T_1 * F$ $T.addT = \text{new temp}(C); T.code = T_1.code || F.code ||$
 $T.addT = T_1.addT * F.addT$

$\rightarrow (E_1)$ $E.add = E_1.addT; F.code = E_1.code$

$\rightarrow Id$ $F.add = id.lexeme, F.code = \epsilon$

2. Operate Three address code (TAC)

The TAC is generated based on expression's evaluation order procedure: Parenthesis - multiplication \rightarrow addition

1. $T_1 = A + B$

$T_2 = C - D$

$T_3 = T_1 * T_2$

$T_4 = T_3 + E$

3. Optimize & Generate TAC

There is no duplicate expression (common sub-expression) in ~~first~~ lines 1 and 2. The code is already optimal w.r.t. TACSE

Assume the final result T_4 is used, all intermediate variables (T_1, T_2, T_3) are necessary inputs for sub-sequent lines. No dead code can be removed

Optimized TAC (unchanged)

$$T_1 = A + B$$

$$T_2 = C - D$$

$$T_3 = T_1 * T_2$$

$$T_4 = T_3 + E$$

Q5 Cumulative - Advanced Reasoning and Application
Language $L = \{ \text{Equal no. of 0's and 1's no prefix has more 1's than 0's Dyck Paths} \}$

Prove that L is context free but not regular

Not regular: Use the Pumping lemma for regular language
Choose $S = 0^b 1^b$. Pumping down ($i=0$) gives $0^{b-1} 1^b$ ($b \geq 1$) which has unequal counts violating L
Thus L is not regular

Context free: The language L is accepted by a Pushdown Automaton (PDA) shown below which demonstrates its context free nature. The PDA's stack is essential for conducting and comparing the non local dependencies (0's vs 1's)

CPG

Provide a CFG for this language (L)

The grammar must enforce that every 1 is matched by a preceding 0

$$S \rightarrow 0S1S / \epsilon$$

3 Design a PDA and Trace 0011'

PDA Design (M)

M accepts by empty stack, using X to count the excess no. of 0's

Start 0: $\delta(q_0, 0, z_0) = \{(q_0, xz_0)\}$

Push 0: $\delta(q_0, 0, x) = \{(q_0, xx)\}$

Pop 1 (prefix check): $\delta(q_0, 1, x) = \{(q_0, \epsilon)\}$
 (pops only if 0's are in excess)

Accept: $\delta(q_0, \epsilon, z_0) = \{(q_0, \epsilon)\}$

B Trace the acceptance of '0011'

Input	State	Stack (1- ∞)	Transition	Condition
0011	q_0	z_0	push 0	$z \neq 0$
0011	q_0	xz_0	push 0	$z \neq 1$
0011	q_0	xxz_0	pop 1	$z \neq 2$
0011	q_0	xz_0	pop 1	$z = 2$
0011	q_0	ϵ	accept empty	