



Figure 1: TATM2 in plate notation

## 1 Tweet Author-Topic Model (with per-word topics)

The model is shown in Figure 1. The generative process is as follows:

1. For  $k \in 1, \dots, K$ :
  - Draw topic  $\beta_k \sim \text{Dir}_V(\eta)$ .
2. For  $a \in 1, \dots, A$ :
  - Draw author's topic proportions  $\theta_a \sim \text{Dir}_K(\alpha)$ .
3. For each document (tweet)  $d \in 1, \dots, D$ :
  - For each word  $w \in 1, \dots, N$ :
    - Draw topic assignment  $z_{d,n} \sim \text{Mult}_K(\theta_a)$ .
    - Draw word  $w_{d,n} \sim \text{Mult}_V(\beta_{z_{d,n}})$ .

Given the hyperparameters  $\alpha$  and  $\eta$ , the joint distribution of topics  $\beta$ , author-topic mixture  $\theta$ , topic assignments  $\mathbf{z}$  and words  $\mathbf{w}$  is given by:

$$p(\theta, \beta, \mathbf{z}, \mathbf{w} | \alpha, \eta) = p(\theta | \alpha) p(\beta | \eta) \prod_{n=1}^N p(z_n | \theta) p(w_n | z_n, \beta_{z_{d,n}}) \quad (1)$$

### 1.1 Complete conditionals

First, we denote  $\theta_a$  to be the topic proportions of the author  $a$  of document  $d$ , i.e.  $\theta_a = \theta_{a_d}$ .

**Local hidden variables.** The complete conditional of the topic assignment  $z_{d,n}$  is a multinomial,

$$p(z_{d,n} = k | \theta_a, \beta, w_{d,n}) \propto \exp\{\log \theta_{a,k} + \log \beta_{k,w_{d,n}}\} \quad (2)$$

**Global hidden variables.** In contrast with standard LDA, the topic proportions are now a global hidden variable. The complete conditional of the author-topic proportions is a posterior Dirichlet,

$$p(\theta_a|\beta, z_d) \propto \text{Dir}(\alpha + \sum_{d \in D_a} \sum_{n=1}^N z_{d,n}^k), \quad (3)$$

where  $D_a$  is the set of documents whose author is  $a$ .

Finally, the complete conditional for the topic  $\beta_k$  is also a posterior Dirichlet,

$$p(\beta_k|\mathbf{z}, \mathbf{w}) \propto \text{Dir}(\eta + \sum_{d=1}^D \sum_{n=1}^N z_{d,n}^k w_{d,n}) \quad (4)$$

## 1.2 Variational parameters for batch variational inference

The variational parameters are:

- Global per-topic Dirichlets  $\lambda_{1:K}$
- Global per-author Dirichlets  $\gamma_{1:A}$
- Local per-word multinomials  $\phi_{1:D, 1:N}$

Each update of the local variables is defined as

$$\phi_{d,n} \propto \exp\{\Psi(\gamma_a) + \Psi(\lambda_{.,w_{d,n}}) - \Psi(\sum_v \lambda_{.,w_{d,n}})\} \quad (5)$$

Each update of the global variational Dirichlets is defined as

$$\gamma_a = \alpha + \sum_{d \in D_a} \sum_{n=1}^N \phi_{d,n} \quad (6)$$

$$\lambda_k = \eta + \sum_{d=1}^{D_a} \sum_{n=1}^N \phi_{d,n}^k w_{d,n} \quad (7)$$

## 1.3 Stochastic variational inference

Each update of the local variables is defined as

$$\phi_{d,n}^k \propto \exp\{\mathbb{E}[\log \theta_{a,k}] + \mathbb{E}[\log \beta_{k,w_{d,n}}]\} \quad (8)$$

During the updates of local variables, we utilize an intermediate local variable  $\hat{\gamma}_d$ , which serves as an indicator of convergence of  $\phi_d$  during the inner loop of the E-step. Specifically,

$$\hat{\gamma}_d = \sum_{n=1}^N \phi_{d,n} \quad (9)$$

After fitting the local variables, we set the intermediate topics as

$$\hat{\lambda}_k = \eta + D \sum_{d=1}^{D_a} \sum_{n=1}^N \phi_{d,n}^k w_{d,n} \quad (10)$$

Finally, the global topics and the global per-author distributions are updated as

$$\lambda_k^{t+1} = (1 - \rho_t) \lambda^t + \rho_t \hat{\lambda}_k \quad (11)$$

$$\gamma_a^{t+1} = \gamma_a^t + \hat{\gamma}_d \quad (12)$$