

# Paper

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This is Paper1, coming after Calc12.

**Title: Holographic screens in ultraviolet self-complete quantum gravity and large extra dimensions**

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## Abstract

In this paper we study the geometry and the thermodynamics of a *holographic screen* in the framework of the ultraviolet self-complete quantum gravity. Large extra dimensions address the gauge hierarchy problem and allow the effective fundamental scale be not far from 1 TeV. In this paper we show that holographic principles recently presented by Nicolini and Spalucci can be smoothly extended with flat, torodially compactified extra dimensions.

## Sven: Reference Guide

Wesentliche Vorlagen hierfür sind:

- Rizzo2006 [[Riz06](#)]: NC + LXD
- N+Spalucci [[NS14](#),[NS13](#)]: Holographic screens in ultraviolet self-complete quantum gravity stellen jeweils  $h$  und  $h_\alpha$  vor.
- Isi, Mureika, N [[IMN13](#),[IMN14](#)]: GUP, aber als Rahmenvorlage von N definiert
- Bleicher, N 2010: LXD at LHC
- Dickes13: No minimal length necessary

## 1 Introduction

Blablabla warum QG toll ist.

## 1.1 Ultraviolet Protection

Authors of [...] have shown that gravity may be self-complete:

Anfangen mit [IMN13]:

$$r_H = \lambda_C \quad (1)$$

Minimal BH, dann das Holy Grail-Bild (Isi Abb 1)

## 1.2 The large extra-dimensions scenario

Ähnlich BN2010, Rizzo2006

$$M_\star^{(2+k)} = M_P^2 / R^k \quad (2)$$

Schwarzschild-Tangherlini-Metrik ansprechen

## 2 Self-regular black hole solutions

We start from the energy density for a point-particle in spherical coordinates as

$$\rho(r) = \frac{M}{\Omega_{n+2} r^{n+2}} \delta(r) \quad (3)$$

where  $\delta(r)$  is the Dirac delta. The energy distribution implies a black hole for any value of mass  $M$  even for subplanckian values where one expects just particles.

We can express the Dirac delta distribution as the derivative of a Heaviside step-function  $\Theta$ ,

$$\delta(r) = \frac{d\Theta(r)}{dr} \quad (4)$$

We modify the energy distribution (3) in order to overcome the ambiguities of the Schwarzschild-Metrik by considering a "smooth" function  $h(r)$  in place of the Heaviside step

$$\Theta(r) \rightarrow h(r) \quad (5)$$

The new profile is defined through  $h(r)$  by

$$\rho(r) = \frac{M}{\Omega_{n+2} r^{n+2}} \frac{dh(r)}{dr} \equiv T_0^0 \quad (6)$$

By means of the conservation equation  $\nabla_\mu T^{\mu\nu} = 0$  one can determine the remaining components of the stress tensor [Riz06]

$$\text{hier ausführlich machen} \quad (7)$$

One ends up with the metric

$$ds^2 = -(1 - V(r)) dt^2 + (1 - V(r))^{-1} dr^2 + r^{2+n} d\Omega_{2+n} \dots \quad (8)$$

with

$$V(r) = \frac{2}{n+2} \frac{M}{M_\star^{n+2}} \frac{1}{\Omega_{n+2}} \frac{h(r)}{r^{n+1}} \quad (9)$$

Carefully making back the transition  $h \rightarrow \Theta$ , actually  $h \rightarrow 1$  in the  $r > 0$  regime, one ends up with Schwarzschild-Thangerlini.

If we set the mass arbitrarily

$$M = \frac{n+2}{2} \Omega_{n+2} \frac{1}{h(r_H)} \left( \frac{r_H}{L_\star} \right)^{n+1} M_\star \quad (10)$$

$M$  has the physical meaning of a mass for a spherical *holographic screen* with radius  $r_H$ .

Eigenschaften angeben:  $M = \dots$ , Ereignishorizonte  $r_h = \dots$

### 3 Thermodynamics, area quantization and mass spectrum

Temp-Plot.  $T_H$ ,  $C$  und ganz wichtig Logarithmische Entropie-Korrektur  $S$ .

Area Quantization: Nachfragen ob ich das auch machen soll. Ist vermutlich schnell gemacht.

### 4 Conclusions

Kurzum: Nichts neues passiert.

We showed that the idea of holography is compatible with the concept of extra dimensions in space-time.

Oder

We showed that the holographic principle is invariant under extension of spacial dimensions.

### 5 Self-regular

### References

- [IMN13] M. Isi, J. Mureika and P. Nicolini, *Self-Completeness and the Generalized Uncertainty Principle*, JHEP **1311**, 139 (2013), 1310.8153.
- [IMN14] M. Isi, J. Mureika and P. Nicolini, *Self-Completeness in Alternative Theories of Gravity*, (2014), 1402.3342.
- [NS13] P. Nicolini and E. Spallucci, *Holographic screens in ultraviolet self-complete quantum gravity*, 2013.
- [NS14] P. Nicolini and E. Spallucci, *Holographic screens in ultraviolet self-complete quantum gravity*, Adv.High Energy Phys. **2014**, 805684 (2014), 1210.0015.
- [Riz06] T. G. Rizzo, *Noncommutative Inspired Black Holes in Extra Dimensions*, JHEP **0609**, 021 (2006), hep-ph/0606051.