

Decomposition - Class 2

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- We decompose to better understand aggregate measures changes/differences
- Decomposition methods improve on existing standardisation methods

Decomposing a crude rate into

- Difference in rates
- Difference in population composition
 - can be along any categorical dimension
 - age, marital status, gender, education

Quiz time!

What about other measures?

- Kitagawa: analytical decomposition of a crude rate
- One can do that with more aggregate measures
- For example, life expectancy

- Spanish-born, Argentinian and US demographer, worked in US and Argentinian universities
- Mostly worked on mortality, also fertility, population change and urbanisation
- Focus on Latin America
- *Measuring and explaining the change in life expectancies*, 1984
→ similar approaches developed by other researchers at the same time



Arriaga decomposition

Decompose difference in life expectancy by age

Total change is the sum of age-specific changes:

$$\Delta LE = \sum_x ({}_n\Delta_x)$$

Arriaga decomposition

$${}_n\Delta_x = \underbrace{\frac{l_x^1}{l_0^1} \left(\frac{{}_nL_x^2}{l_x^2} - \frac{{}_nL_x^1}{l_x^1} \right)}_{\text{Direct effect}} + \underbrace{\frac{T_{x+n}^2}{l_0^1} \left(\frac{l_x^1}{l_x^2} - \frac{l_{x+n}^1}{l_{x+n}^2} \right)}_{\text{Indirect and interaction effects}}$$

Change in mortality rates between ages x and $x + n$ affects

- Number of years lived between ages x and $x + n \rightarrow$ direct effect
- Number of years lived after age $x + n$ by new survivors \rightarrow indirect and interaction effect

Arriaga decomposition

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- Number of years lived between ages x and $x+n \rightarrow$ direct effect
- Number of years lived after age $x+n$ by new survivors \rightarrow indirect and interaction effect

For open-ended age-group there is only a direct effect:

$${}_{\infty}\Delta_x = \frac{l_x^1}{l_0^1} \left(\frac{T_x^2}{l_x^2} - \frac{T_x^1}{l_x^1} \right)$$






RESEARCH ARTICLE

DEMOGRAPHY

 OPEN ACCESS



Significant impacts of the COVID-19 pandemic on race/ethnic differences in US mortality

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Let's try ourselves

Arriaga decomposition by causes of death

We can extend this method to account for contributions from different causes of death i :

$$\begin{aligned} {}_n\Delta_x^i &= {}_n\Delta_x \frac{{}_nm_{x,i}^2 - {}_nm_{x,i}^1}{{}_nm_x^2 - {}_nm_x^1} \\ &= {}_n\Delta_x \frac{{}_nR_{x,i}^2({}_nm_x^2) - {}_nR_{x,i}^1({}_nm_x^1)}{{}_nm_x^2 - {}_nm_x^1} \end{aligned}$$

Where

- ${}_nR_{x,i}^t$ is the proportion of deaths from cause i in ages x to $x + n$ and population t
- ${}_n\Delta_x$ is the contribution of all-cause mortality differences in the same age group
- ${}_nm_x^t$ is the mortality rate in the same age group of population t

Arriaga decomposition by causes of death

All-cause contribution, weighted by the change in cause-specific mortality as a proportion of change in all-cause mortality

Back to R!

Could the Arriaga decomposition be useful for your research? What if you could modify it?

References

E.E. Arriaga (1984). "Measuring and explaining the change in life expectancies", *Demography*, 21(1): 83–96.