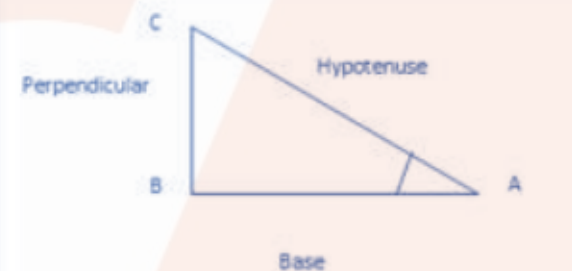
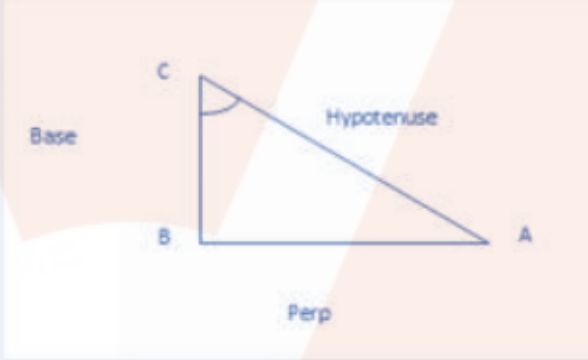


## CHAPTER – 8

### TRIGONOMETRY

S.no	Terms	Descriptions
1	<b>What is Trigonometry</b>	<p>Trigonometry from Greek trigōnon, "triangle" and metron, "measure") is a branch of mathematics that studies relationships involving lengths and angles of triangles. The field emerged during the 3rd century BC from applications of geometry to astronomical studies.</p> <p>Trigonometry is most simply associated with planar right angle triangles (each of which is a two-dimensional triangle with one angle equal to 90 degrees). The applicability to non-right-angle triangles exists, but, since any non-right-angle triangle (on a flat plane) can be bisected to create two right-angle triangles, most problems can be reduced to calculations on right-angle triangles. Thus the majority of applications relate to right-angle triangles</p>
2	<b>Trigonometric Ratio's</b>	<p>In a right angle triangle ABC where <math>B=90^\circ</math></p>  <p>We can define following term for angle A</p> <p><b>Base</b> : Side adjacent to angle</p> <p><b>Perpendicular</b>: Side Opposite of angle</p> <p><b>Hypotenuse</b>: Side opposite to right angle</p> <p>We can define the trigonometric ratios for angle A as</p> <p><math>\sin A = \text{Perpendicular/Hypotenuse} = BC/AC</math></p> <p><math>\operatorname{cosec} A = \text{Hypotenuse/Perpendicular} = AC/BC</math></p> <p><math>\cos A = \text{Base/Hypotenuse} = AB/AC</math></p> <p><math>\sec A = \text{Hypotenuse/Base} = AC/AB</math></p> <p><math>\tan A = \text{Perpendicular/Base} = BC/AB</math></p> <p><math>\cot A = \text{Base/Perpendicular} = AB/BC</math></p> <p>Notice that each ratio in the right-hand column is the inverse, or the reciprocal, of the ratio in the left-hand column.</p>

<b>3</b>	Reciprocal of functions	<p>The reciprocal of <math>\sin A</math> is <math>\operatorname{cosec} A</math> ; and vice-versa.</p> <p>The reciprocal of <math>\cos A</math> is <math>\sec A</math></p> <p>And the reciprocal of <math>\tan A</math> is <math>\cot A</math></p> <p>These are valid for acute angles.</p> <p>We can define <math>\tan A = \sin A / \cos A</math></p> <p>And <math>\cot A = \cos A / \sin A</math></p>
<b>4</b>	Value of $\sin$ and $\cos$	<b>Is always less 1</b>
<b>5</b>	Trigonometric ratios from another angle	<p>We can define the trigonometric ratios for angle C as</p>  <p> <math>\sin C = \text{Perpendicular/Hypotenuse} = AB/AC</math>  <math>\operatorname{cosec} C = \text{Hypotenuse/Perpendicular} = AC/AB</math>  <math>\cos C = \text{Base/Hypotenuse} = BC/AC</math>  <math>\sec C = \text{Hypotenuse/Base} = AC/BC</math>  <math>\tan A = \text{Perpendicular/Base} = AB/BC</math>  <math>\cot A = \text{Base/Perpendicular} = BC/AB</math> </p>
<b>6</b>	Trigonometric ratios of complimentary angles	<p><math>\sin (90-A) = \cos(A)</math></p> <p><math>\cos(90-A) = \sin A</math></p> <p><math>\tan(90-A) = \cot A</math></p> <p><math>\sec(90-A) = \operatorname{cosec} A</math></p> <p><math>\operatorname{Cosec} (90-A) = \sec A</math></p>
<b>7</b>	Trigonometric identities	<p><math>\cot(90- A) = \tan A</math></p> <p><math>\sin^2 A + \cos^2 A = 1</math></p> <p><math>1 + \tan^2 A = \sec^2 A</math></p> <p><math>1 + \cot^2 A = \operatorname{cosec}^2 A</math></p>

**Trigonometric Ratios of common angles:**

We can find the values of trigonometric ratio's various angle

Angles(A)	SinA	Cos A	TanA	Cosec A	Sec A	Cot A
0°	0	1	0	Not defined	1	Not defined
30°	$\frac{1}{2}$	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{3}}$	2	$\frac{2}{\sqrt{3}}$	$\sqrt{3}$
45°	$\frac{1}{\sqrt{2}}$	$\frac{1}{\sqrt{2}}$	1	$\sqrt{2}$	$\sqrt{2}$	1
60°	$\frac{\sqrt{3}}{2}$	$\frac{1}{2}$	$\sqrt{3}$	$\frac{2}{\sqrt{3}}$	2	$\frac{1}{\sqrt{3}}$
90°	1	0	Not defined	1	Not defined	0