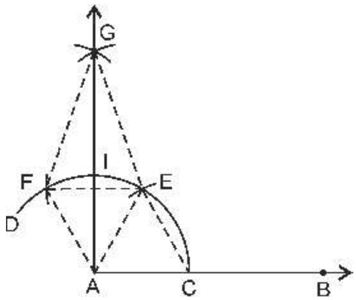
11 CONSTRUCTIONS

EXERCISE 11.1

Q.1. *Construct an angle of* 90° *at the initial point of a given ray and justify the construction.*



Steps of Construction

(i) Let us take a ray AB with initial point A.

(ii) Taking A as centre and some radius, draw an arc of a circle, which intersects AB at C.

(iii) With C as centre and the same radius as before, draw an arc, intersecting the previous arc at E.

(iv) With E as centre and the same radius, as before, draw an arc, which intersects the arc drawn in step (ii) at F.

(v) With E as centre and some radius, draw an arc.

(vi) With F as centre and the same radius as before, draw another arc, intersecting the previous arc at G.

(vii) Draw the ray AG.

Then $\angle BAG$ is the required angle of 90°.

Justification : Join AE, CE, EF, FG and GE

AC = CE = AE [By construction]

$\Rightarrow \Delta ACE$ is an equilateral triangle

$\Rightarrow \angle CAE = 60°$ ... (i)

Similarly, $\angle AEF = 60°$ ... (ii)

From (i) and (ii), FE ∥ AC ... (iii) [Alternate angles are equal]

Also, FG = EG [By construction]

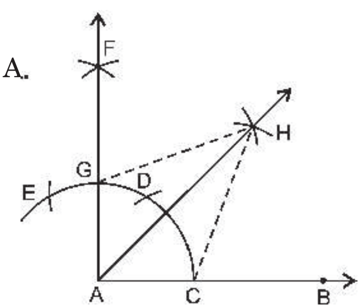
$\Rightarrow$ G lies on the perpendicular bisector of EF

$\Rightarrow \angle GIE = 90°$ ... (iv)

$\therefore \angle GAB = \angle GIE = 90°$ [Corresponding angles]

GF = GE [Arcs of equal radii]

Q.2. *Construct an angle of* 45° *at the initial point of a given ray and justify the construction.*



Steps of Construction

(i) Let us take a ray AB with initial point A.

(ii) Draw $\angle BAF = 90°$, as discussed in Q. 1.

(iii) Taking C as centre and radius more than $\frac{1}{2}$ CG, draw an arc.

(iv) Taking G as centre and the same radius as before, draw another arc, intersecting the previous arc at H.

(v) Draw the ray AH. Then $\angle BAH$ is the required angle of 45°.

Justification : Join GH and CH.

In ΔAHG and ΔAHC, we have

$HG = HC$ [Arcs of equal radii]

$AG = AC$ [Radii of the same arc]

$AH = AH$ [Common]

$\therefore \Delta AHG \cong \Delta AHC$ [SSS congruence]

$\Rightarrow \angle HAG = \angle HAC$ [CPCT] ... (i)

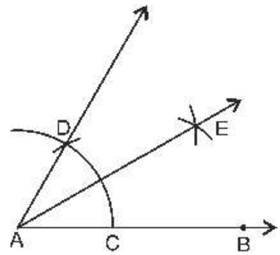
But $\angle HAG + \angle HAC = 90°$ [By construction] ... (ii)

$\Rightarrow \angle HAG = \angle HAC = 45°$ [From (i) and (ii)]

Q.3. *Construct the angles of the following measurements.*

(i) 30° *(ii)* $22\frac{1}{2}°$ *(iii)* 15°

(i) Steps of Construction



(a) Draw a ray AB, with initial point A.

(b) With A as centre and some convenient radius, draw an arc, intersecting AB at C.

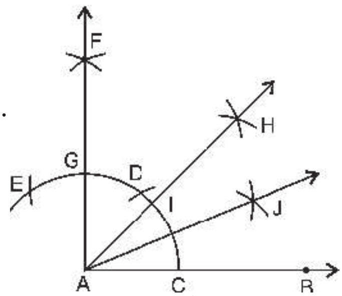
(c) With C as centre and the same radius as before, draw another arc, intersecting the previously drawn arc at D.

(d) Draw ray AD.

(e) Now, taking C and D as centres and with the radius more than $\frac{1}{2}$ DC, draw arcs to intersect each other at E.

(f) Draw ray AE. Then $\angle BAE$ is the required angle of 30°.

(ii) Steps of Construction



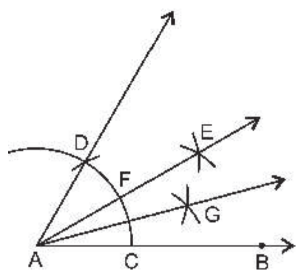
(a) Draw a ray AB with initial point A.

(b) Draw $\angle BAH = 45°$ as discussed in Q. 2.

(c) Taking I and C as centres and with the radius more than $\frac{1}{2}$ CI, draw arcs to intersect each other at J.

(d) Draw ray AJ. Then $\angle BAJ$ is the required angle of $22\frac{1}{2}°$.

(iii) Steps of Construction



(a) Draw $\angle BAE = 30°$ as discussed in part (i).

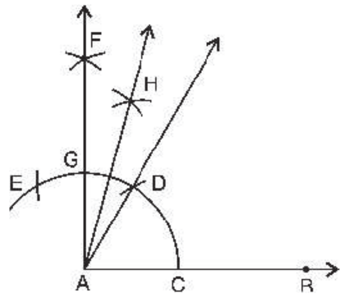
(b) Taking C and F as centres and with the radius more than $\frac{1}{2}$ CF, draw arcs to intersect each other at G.

(c) Draw ray AG. Then $\angle BAG$ is the required angle of 15°.

Q.4. *Construct the following angles and verify by measuring them by a protractor.*

(i) 75° *(ii)* 105° *(iii)* 135°

(i) Steps of Construction



(a) Draw a ray AB with initial point A.

(b) With A as centre and any convenient radius, draw an arc, intersecting AB at C.

(c) With C as centre and the same radius, draw an arc, cutting the previous arc at D.

(d) With D as centre and the same radius, draw another arc, cutting the arc drawn in step (b) at E.

(e) With D and E as centres and some radius, draw arcs to intersect each other at F.

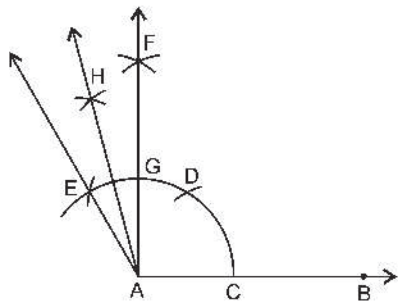
(f) Draw ray AF and AD.

(g) With D and G as centres, and radius more than $\frac{1}{2}$GD, draw arcs to intersect. each other at H.

(h) Draw ray AH. Then $\angle$BAH is the required angle of 75°.

On measuring using a protractor, we find that $\angle$BAH = 75°.

(ii) Steps of Construction



(a) At A, draw an $\angle$BAF = 90°, as discussed in Q. 1.

(b) With A as centre and some convenient radius, draw an arc, intersecting AB at C.

(c) With C as centre and the same radius, draw an arc, which cuts the precious arc at D.

(d) With D as centre and the same radius, draw an arc, which cuts the arc drawn in step (b) at E.

(e) Draw ray AE.

(f) With G and E as centres and radius more than $\frac{1}{2}$GE, draw arcs to intersect each other at H.

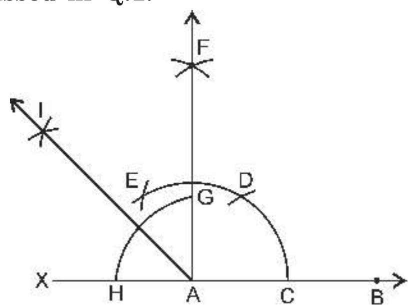
(g) Join AH. Then $\angle$BAH is the required angle of 105°.

On measuring using a protractor, we find that $\angle$BAH = 105°.

(iii) Steps of Construction

(a) At A, draw angle BAF = 90°, as discussed in Q.1.

(b) Produce BA to X.



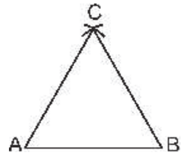
(c) With A as centre and some convenient radius, draw an arc, which cuts AF and AX at G and H respectively.

(d) With G and H as centres and radius more than $\frac{1}{2}$GH, draw arcs to intersect each other at I.

(e) Draw ray AI. Then $\angle$BAI is the required angle of 135°.

On measuring using a protractor, we find that $\angle$BAI = 135°.

Q.5. *Construct an equilateral triangle, given its side and justify the construction.*



(i) Steps of Construction

(i) Draw a line segment AB of given length.

(ii) With A and B as centres and radius equal to AB, draw arcs to intersect each other at C.

(iii) Join AC and BC. Then ABC is the required equilateral triangle.

Justification : AB = AC [By construction]

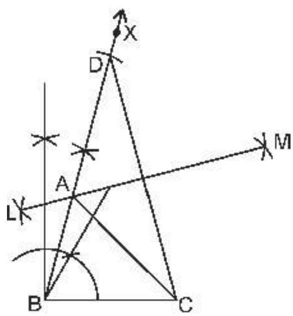
AB = BC [By construction]

$\Rightarrow$ AB = AC = BC

Hence, ΔABC is an equilateral triangle.

EXERCISE 11.2

Q.1. *Construct a triangle ABC in which BC = 7 cm, $\angle B$ = 75° and AB + AC = 13 cm.*



Steps of Construction

(i) Draw a line segment BC = 7 cm.

(ii) At B, draw $\angle$CBX = 75°.

(iii) Cut a line segment BD = 13 cm from BX.

(iv) Join DC

(v) Draw the perpendicular bisector LM of CD, which intersects BD at A.

(vi) Join AC. Then ABC is the required triangle.

Justification : In ΔACD, we have

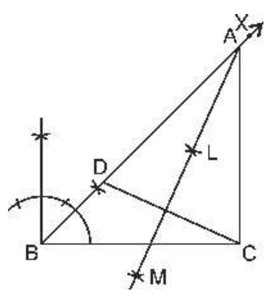
AC = AD [A lies on the perpendicular bisector of DC.]

AB = BD – AD

= BD – AC

$\Rightarrow$ AB + AC = BD

Q.2. *Construct a triangle ABC, in which BC = 8 cm, $\angle B$ = 45° and AB – AC = 3.5 cm.*



Steps of Construction

(i) Draw a line segment BC = 3.5 cm

(ii) At B, draw $\angle$CBX = 45°.

(iii) From BX, cut off BD = 3.5 cm.

(iv) Join DC.

(v) Draw the perpendicular bisector LM of DC, which intersects BX at A. (vi) Join AC. Then ABC is the required triangle.

Justification : In ΔADC,

AD = AC [A lies on the perpendicular bisector of DC]

BD = AB – AD

$\Rightarrow$ BD = AB – AC

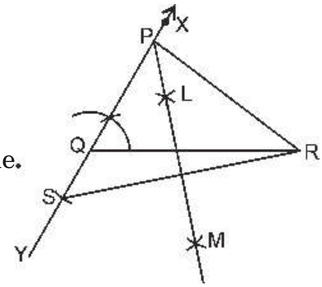
Q.3. *Construct a triangle PQR in which QR = 6 cm, $\angle$Q = 60° and PR – PQ = 2 cm.*

Steps of Construction

(i) Draw a line segment QR = 6 cm

(ii) At Q, draw $\angle$RQX = 60°.

(iii) Produce XQ to Y.
(iv) Cut off QS = 2 cm from QY.
(v) Join SR.
(vi) Draw the perpendicular bisector LM of SR, which intersect QX at P.
(vii) Join PR. Then PQR is the required triangle.



Justification : In ΔPSR, we have

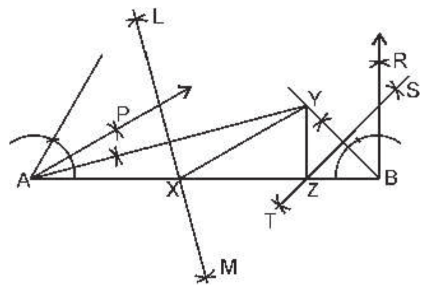
$SP = PR$ [P lies on the perpendicular bisector of SR]

$QS = PS - PQ$
$= PR - PQ$

Q.4. *Construct a* ΔXYZ *in which* $\angle X = 30°$, $\angle Z = 90°$ *and* $XY + YZ + ZX = 11$ *cm.*

Steps of Construction

(i) Draw a line segment AB = 11 cm
(ii) At A, draw $\angle BAP = 30°$ and at B, draw $\angle ABR = 90°$
(iii) Draw the bisector of $\angle BAP$ and $\angle ABR$, which intersect each other at Y.
(iv) Join AY and BY.
(v) Draw the perpendicular bisectors LM and ST of AY and BY respectively. LM and ST intersect AB at X and Z respectively.
(vi) Join XY and YZ. Then XYZ is the required triangle.



Justification : In ΔAXY, we have

$AX = XY$ [X lies on the perpendicular bisector of AY] ...(i)

Similarly, $ZB = YZ$ ... (ii)

$\therefore XY + YZ + ZX = AX + ZB + ZX$ [From (i) and (ii)]
$= AB$

From (i), $AX = AY$

$\Rightarrow \angle XAY = \angle XYA$ [Angles opposite to equal sides are equal] ... (iii)

In ΔAXY, $\angle YXZ = \angle XAY + \angle XYA$ [Exterior angle is equal to sum of interior opposite angles]

$\Rightarrow \angle YXZ = 2\angle XAY$ [From (iii)]

$\Rightarrow \angle YXZ = \angle XAP$ [$\because$ AY bisects $\angle XAP$]

Similarly, $\angle YZX = \angle ZBR$.

Q.5. *Construct a right triangle whose base is* 12 *cm and sum of its hypotenuse and other side is* 18 *cm.*

Steps of Construction

(i) Draw a line segment AB = 12 cm.
(ii) At A, draw $\angle BAX = 90°$.
(iii) From AX, cut off AD = 18 cm.
(iv) Join DB.
(v) Draw the perpendicular bisector LM of BD, which intersects AD at C.
(vi) Join BC. Then ΔABC is the required triangle.